### Pattern recognition

Classification/Clustering GW – Chapter 12 (some concepts)

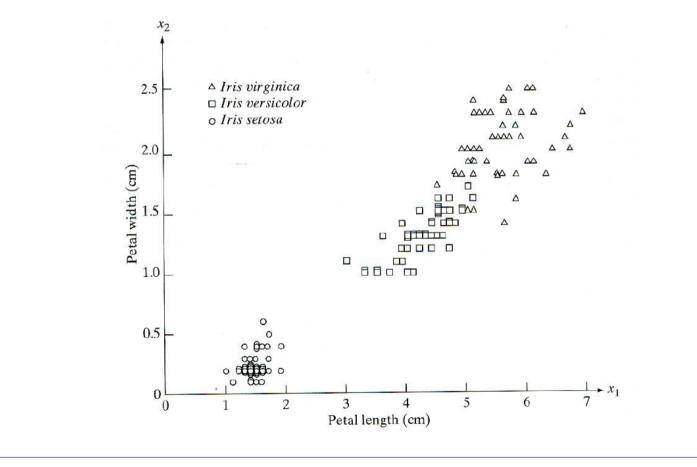
Textures

### Patterns and pattern classes

- Pattern: arrangement of descriptors
- Descriptors: features
- Patten class: family of patterns that share common properties denoted by  $\omega_1, \omega_2, \omega_3, ..., \omega_n$
- Pattern recognition: assigning patterns to the respective classes
- Patterns are represented by vectors of descriptors called feature vectors
- $FV = [x_1, x_2, ..., x_n]^T$
- The nature of the features depends on the problem

### Patterns and pattern classes

• Task: distinguish flowers based on the length and width of petals



# Feature selection problem

- Identify the features that lead to the maximum separability among classes
- Features vary both within and between classes. Classes are separable if istances of the same classes have features that are more similar among them then to the features of objects belonging to different classes. In this case, a boundary can be identified in the feature space separating objects belonging to different classes
- Goal of feature selection: minimize variability within classes and maximize separation among classes

# Choose the good features!









# Color







# Number of hears







# Choice of the features

- First statistical moments could be used as features
- Implies the use of a neighborhood which limits the resolution
- Typical for region-based processing
  - Texture features

# PR based on decision theoretic methods

- Based on the use of a discriminant function
- Let x be a FV and ω<sub>1</sub>, ω<sub>2</sub>, ω<sub>3</sub>, ..., ω<sub>n</sub> be n pattern classes. The basic problem consists in finding n decision functions di(x) with the property that if pattern x belongs to the class ωi then

$$d_i(x) > d_j(x) \quad i, j = 1, \dots, n \quad i \neq j$$

- The decision boundary separating  $\omega_i$  from  $\omega_j$  is given by the values of x for which

 $d_i(x) = d_j(x)$ 

### PR based on decision theoretic methods

Common practice consists in identifying decision boundaries by the single function

$$d_{i,j}(x) = d_i(x) - d_j(x)$$

#### • Thus

 $d_{ij}(x) > 0$  For objects belonging to  $\omega i$ 

$$d_{ii}(x) < 0$$
 For objects belonging to  $\omega_{j}$ 

# Classification

- Problem statement
  - Given a set of classes  $\{\omega_i, i=1,...N\}$  and a set of observations  $\{x_{i,k}, k=1,...M\}$  determine the most probable class, given the observations. This is the class that maximizes the conditional probability:

$$\omega_{winner} = \max_{k} P(\omega_i | x_k)$$

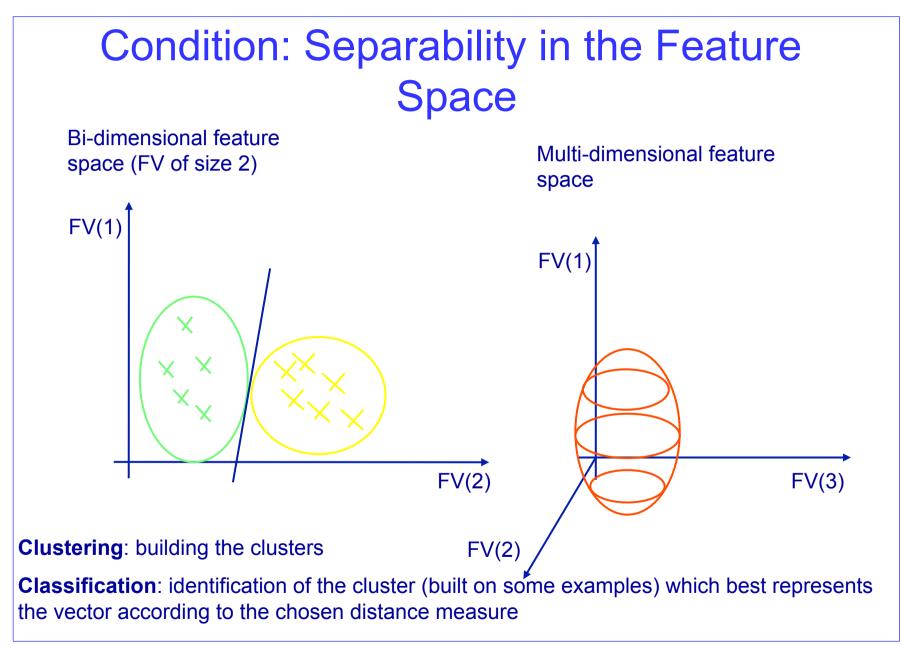
### **Clustering and Classification**

- Clustering
  - Putting together (aggregating) feature vectors based on a minimum distance criterion
  - Self-contained: no need to refer to other images or data samples

- Classification
  - Identification of the class a given feature vector belongs to based on a minimum distance criterion and based on a set of available "examples"
  - Uses a reference database of example images that identify the different classes

Hypothesis: the classes (textures) are separated in the feature space

Both result in a segmentation map associating one class to each pixel

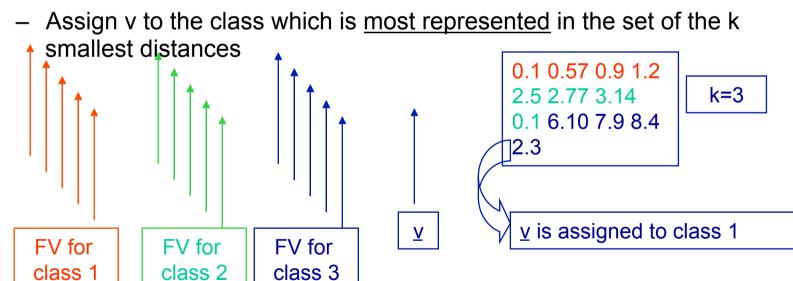


# Types of PR algorithms

- Measuring the distance among a <u>class</u> and a <u>vector</u>
  - Each class (set of vectors) is represented by the <u>mean (m)</u> vector and the vector of the <u>variances</u> (s) of its components ⇒ the training set is used to build <u>m</u> and <u>s</u>
  - The distance is taken between the test vector and the <u>m</u> vector of each class
  - The test vector is assigned to the class to which it is closest
    - Euclidean classifier
    - Weighted Euclidean classifier
  - Example: k-means clustering
- Measuring the distance among of vectors
  - One vector belongs to the training set and the other is the one we are testing
  - Example: kNN classification

# kNN

- Given a vector  $\underline{v}$  of the test set
  - Take the distance between the vector  $\underline{v}$  and ALL the vectors of the training set
  - (while calculating) keep the k smallest distances and keep track of the class they correspond to

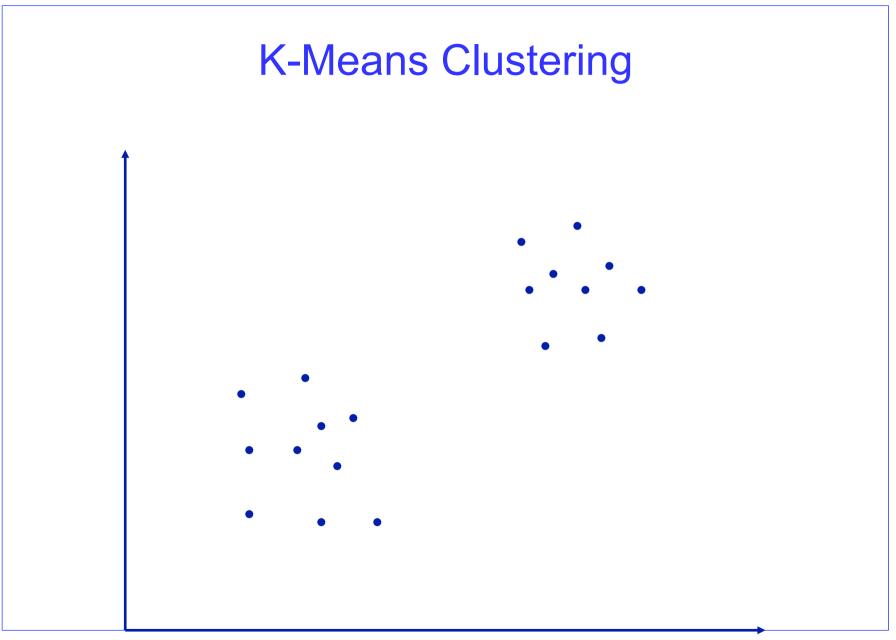


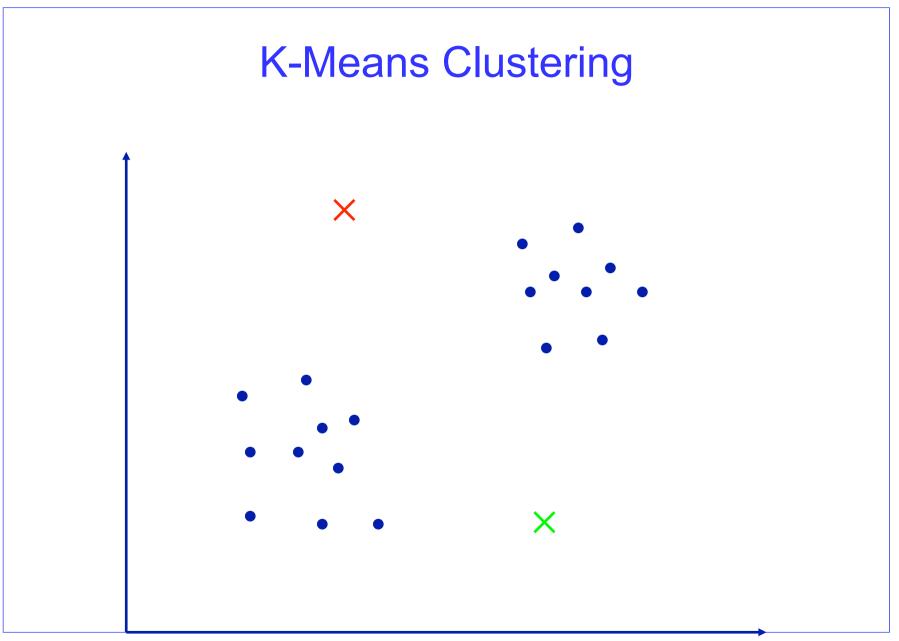
# **Confusion matrix**

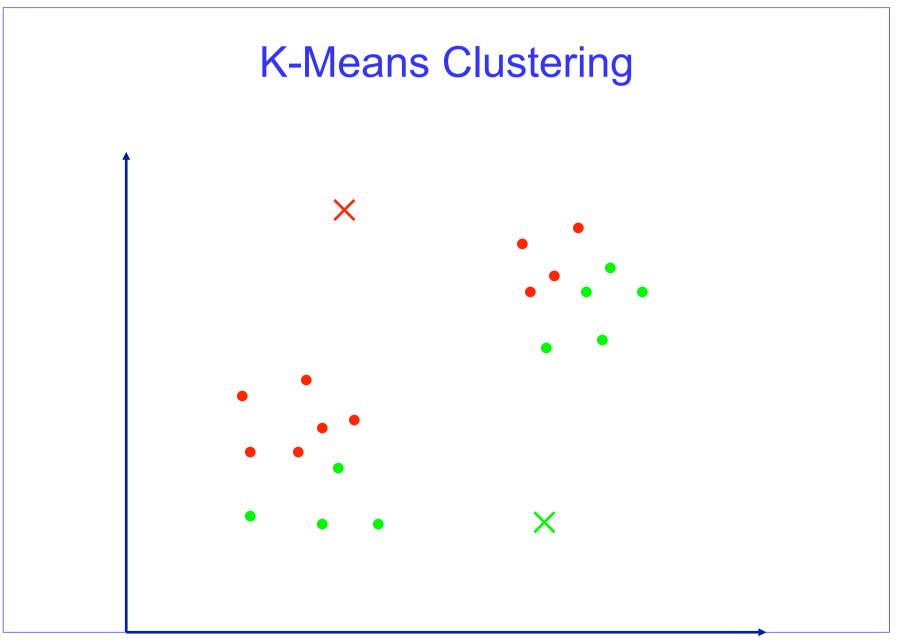
textures	1	2	3	4	5	6	7	8	9	10	% correct
1	841	0	0	0	0	0	0	0	0	0	100.00%
2	0	840	1	0	0	0	0	0	0	0	99.88%
3	2	0	839	0	0	0	0	0	0	0	99.76%
4	0	0	0	841	0	0	0	0	0	0	100.00%
5	0	0	88	0	753	0	0	0	0	0	89.54%
6	0	0	134	0	0	707	0	0	0	0	84.07%
7	0	66	284	0	0	0	491	0	0	0	58.38%
8	0	0	58	0	0	0	0	783	0	0	93.10%
9	0	0	71	0	0	0	0	0	770	0	91.56%
10	0	4	4	0	0	0	0	0	0	833	99.05%
				Average recognition rate							<b>91.53%</b>

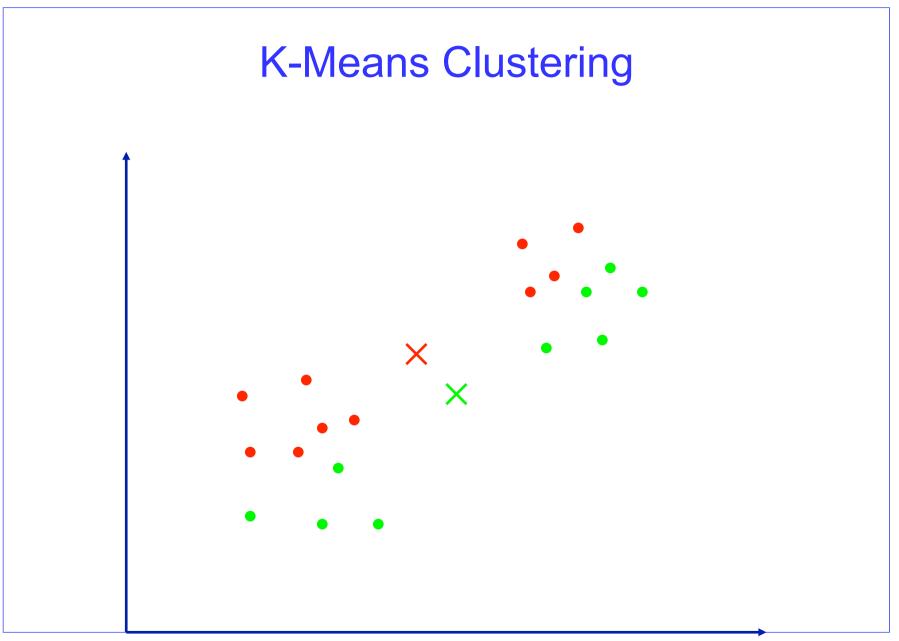
# **K-Means Clustering**

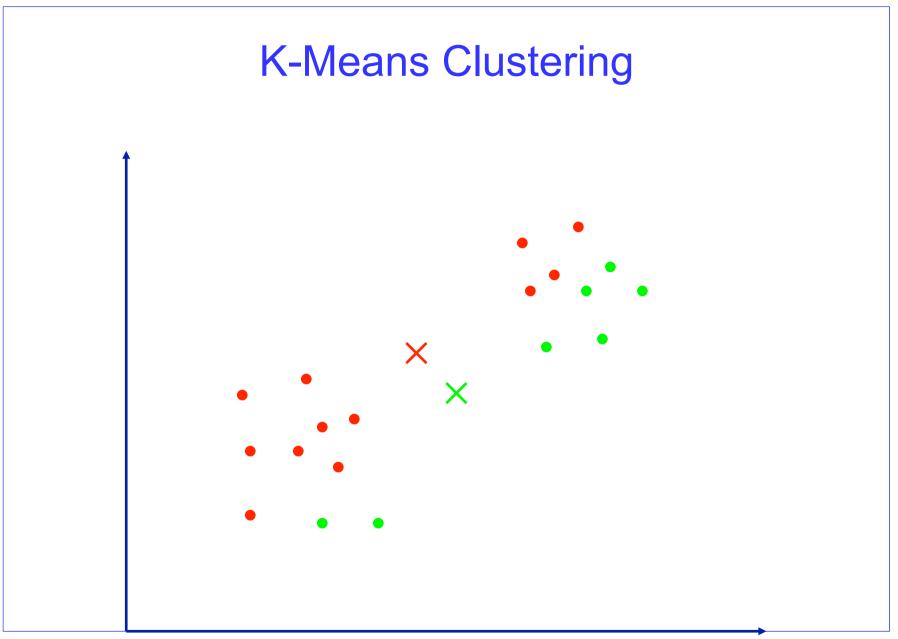
- 1. Partition the data points into K clusters randomly. Find the centroids of each cluster.
- 2. For each data point:
  - Calculate the distance from the data point to each cluster.
  - Assign the data point to the closest cluster.
- 3. Recompute the centroid of each cluster.
- 4. Repeat steps 2 and 3 until there is no further change in the assignment of data points (or in the centroids).

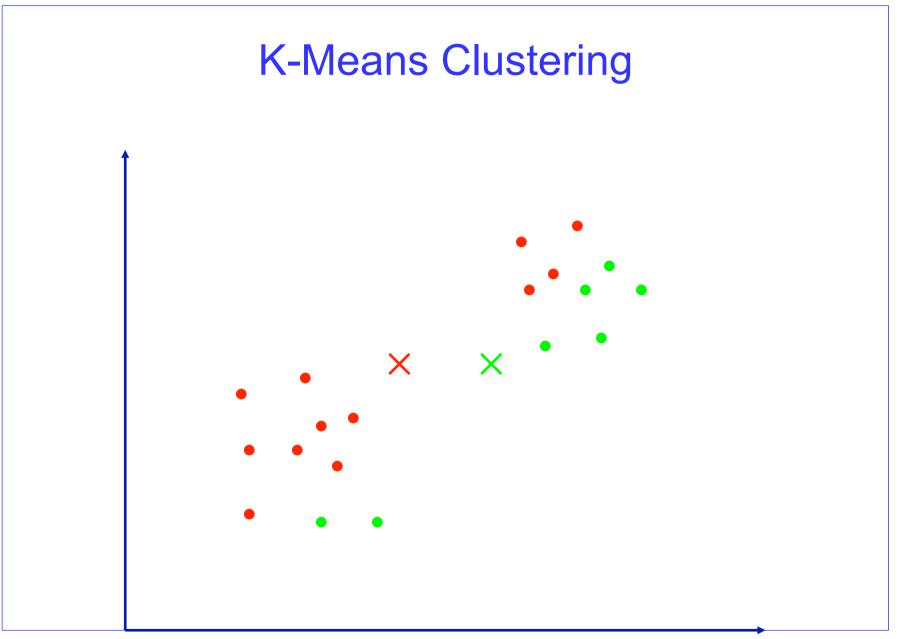


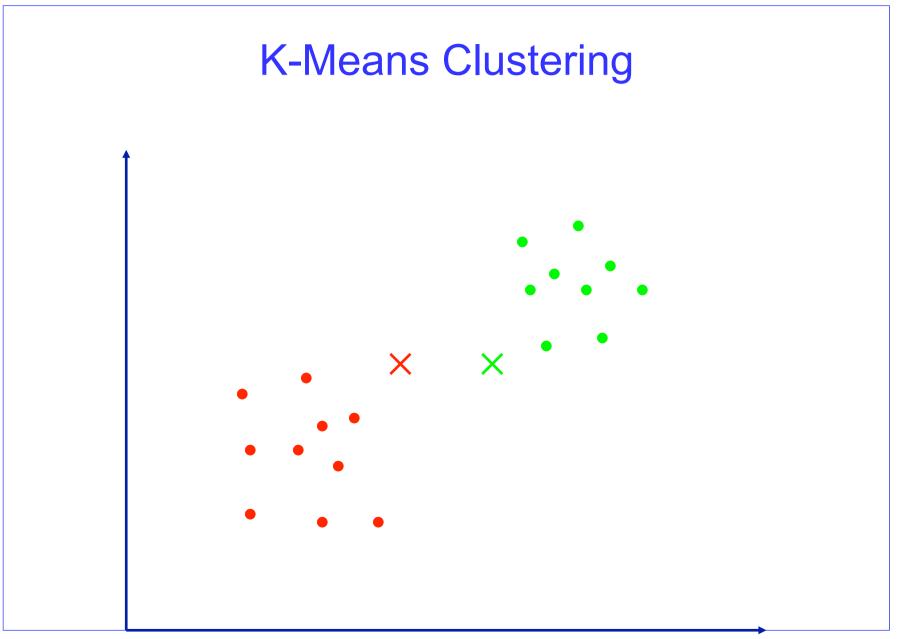


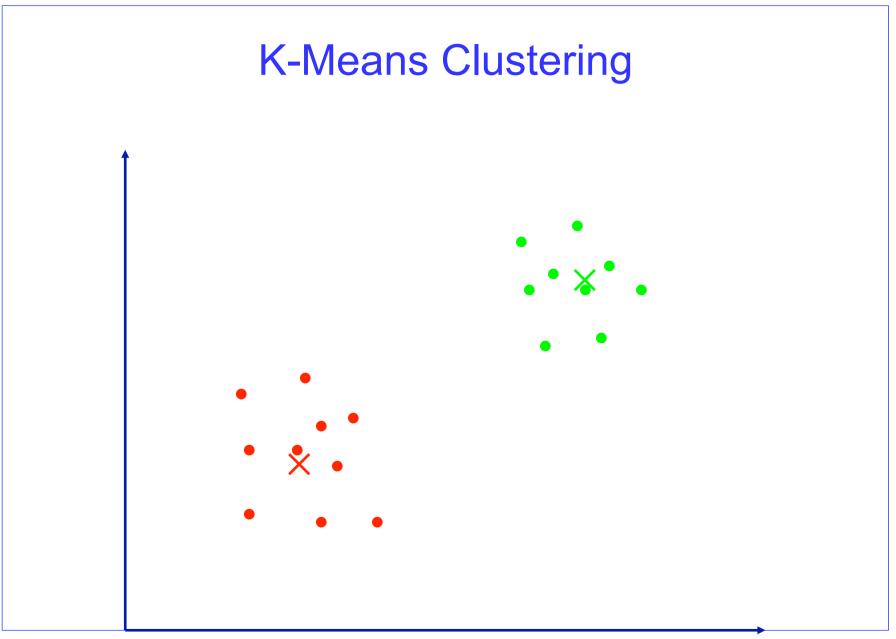


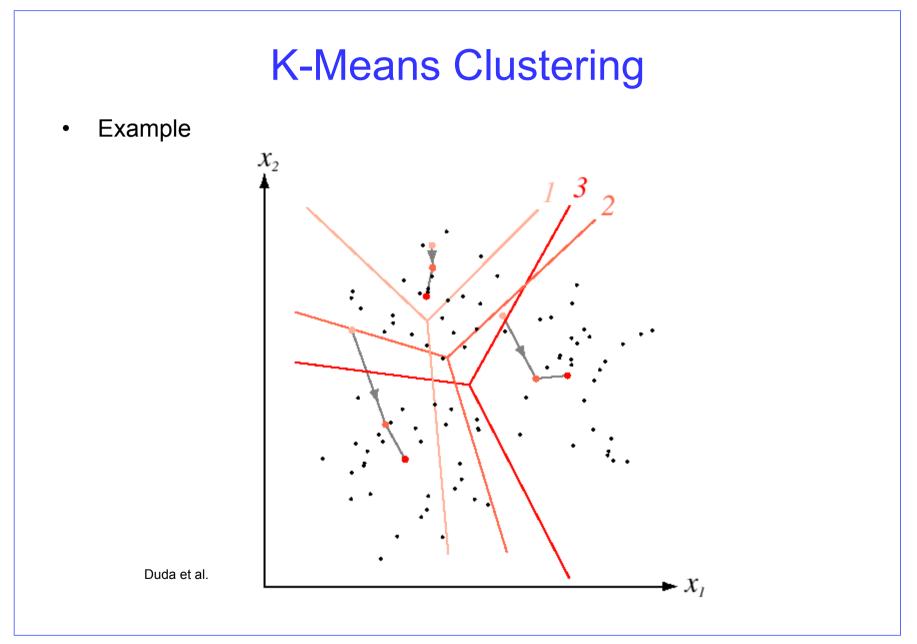


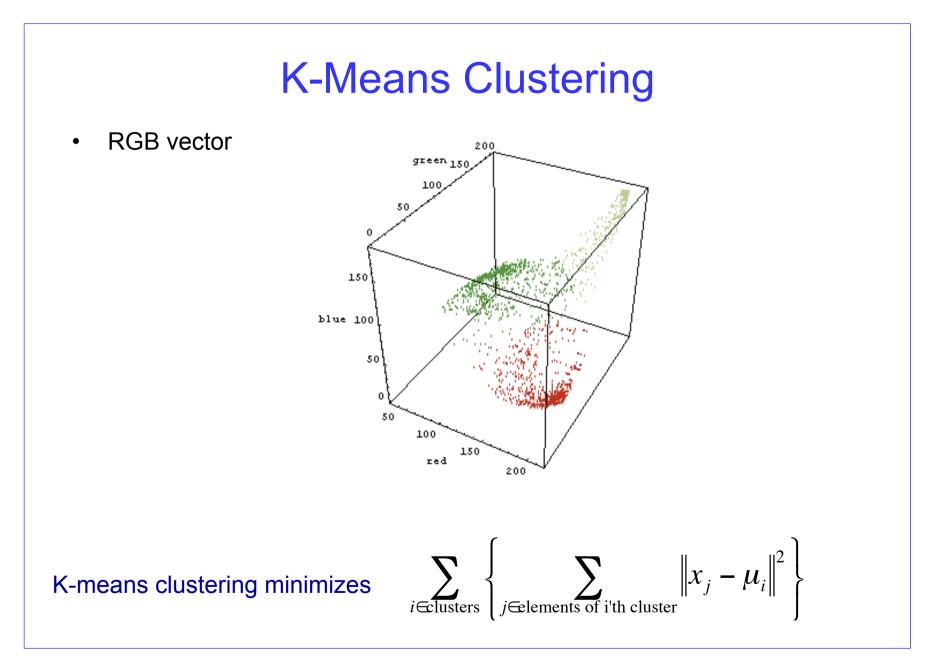


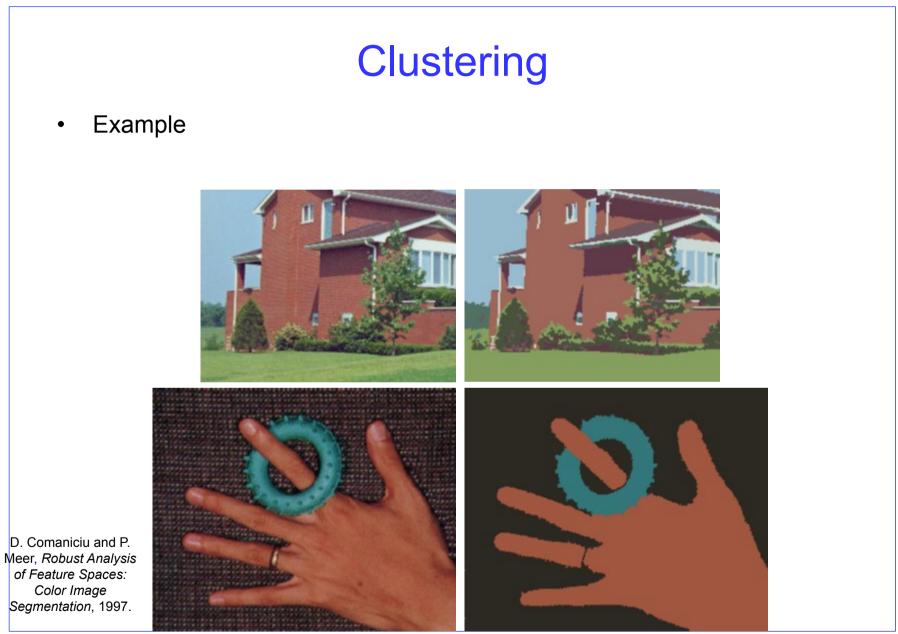






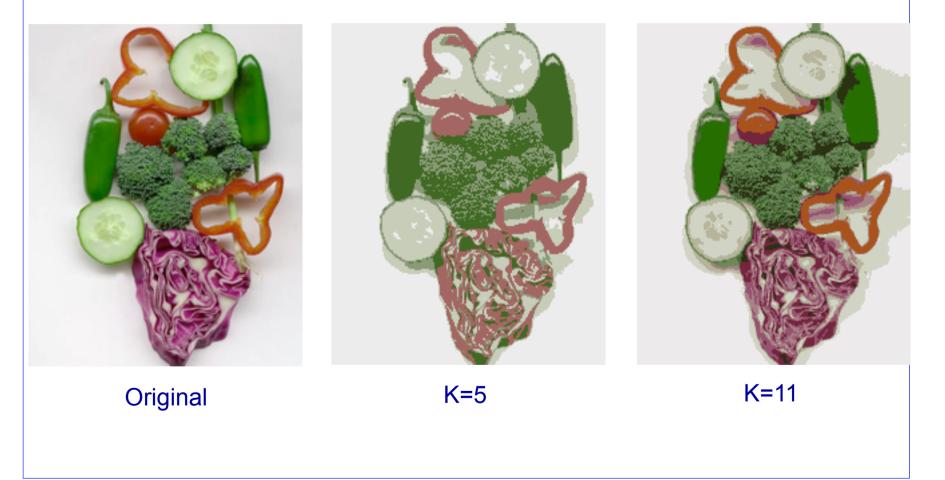






# **K-Means Clustering**

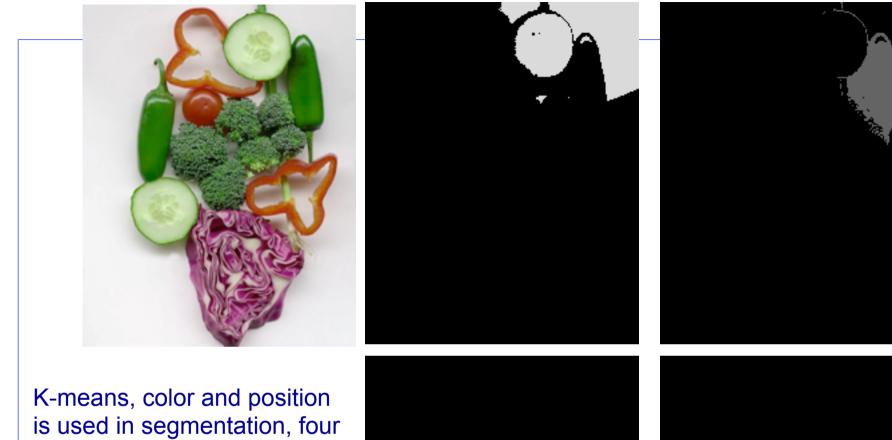
• Example







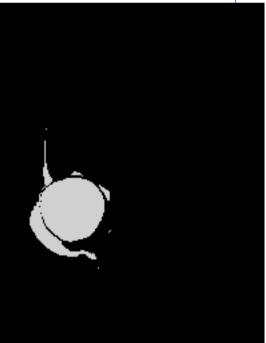




K-means, color and position is used in segmentation, four clusters (out of 20) are shown here.

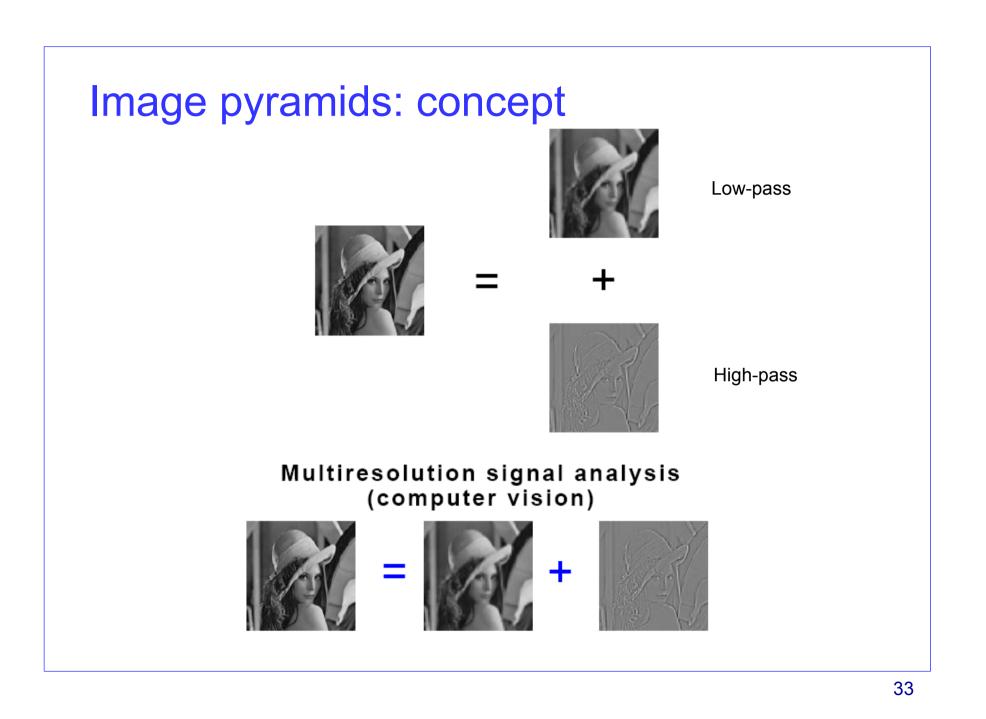
Each vector is (R,G,B,x,y).

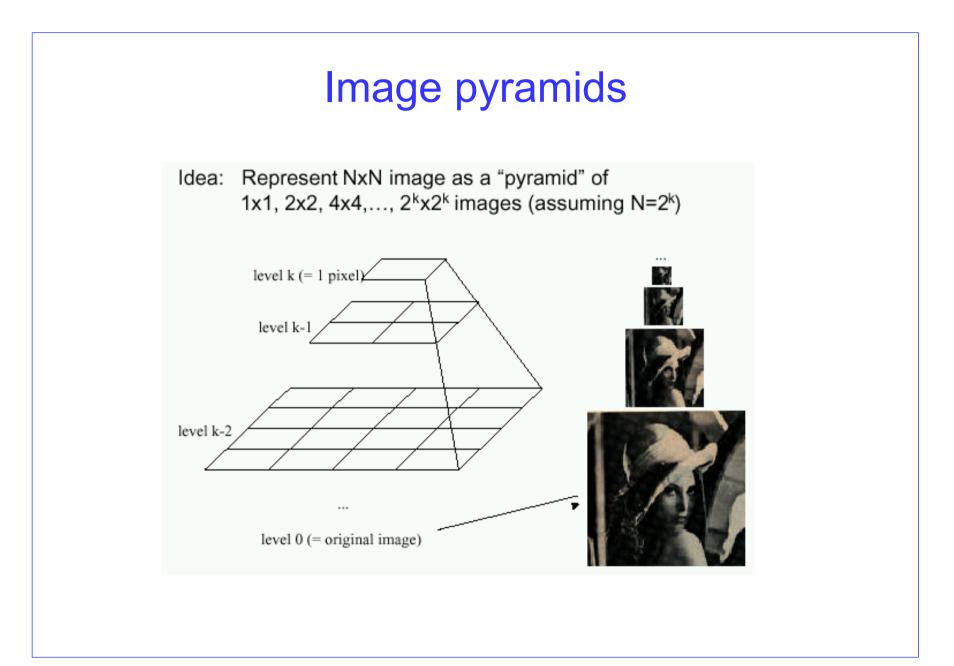


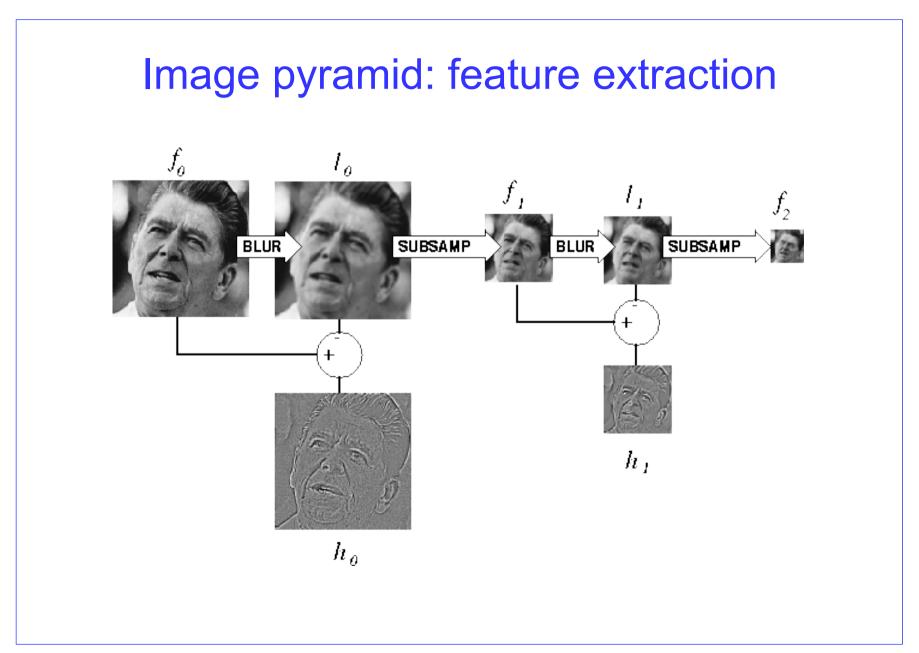


# K-Means Clustering: Axis Scaling

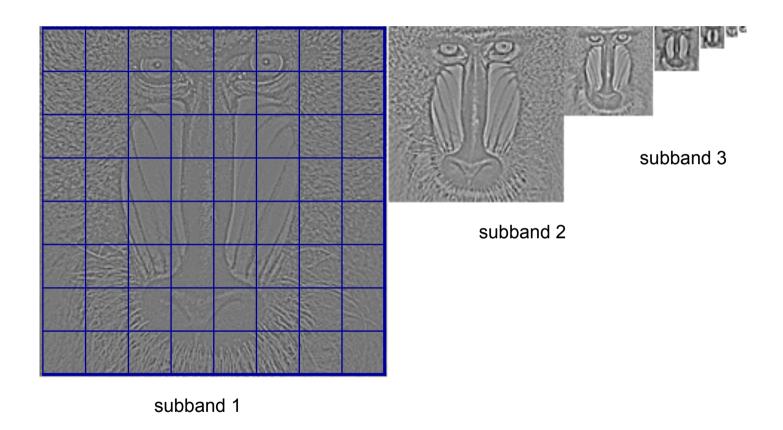
- Features of different types may have different scales.
  - For example, pixel coordinates on a 100x100 image vs. RGB color values in the range [0,1].
- Problem: Features with larger scales dominate clustering.
- Solution: Scale the features.



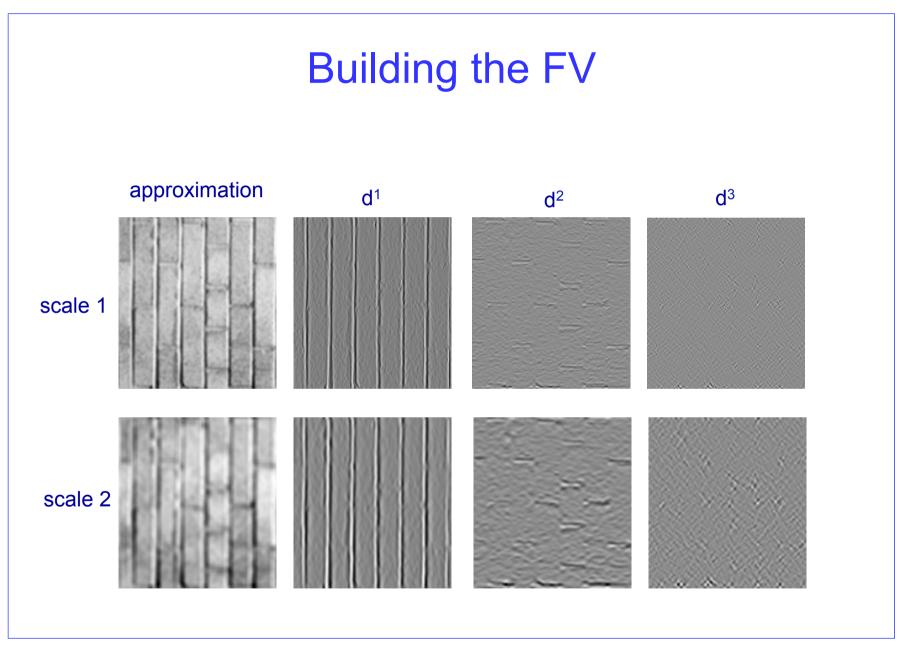


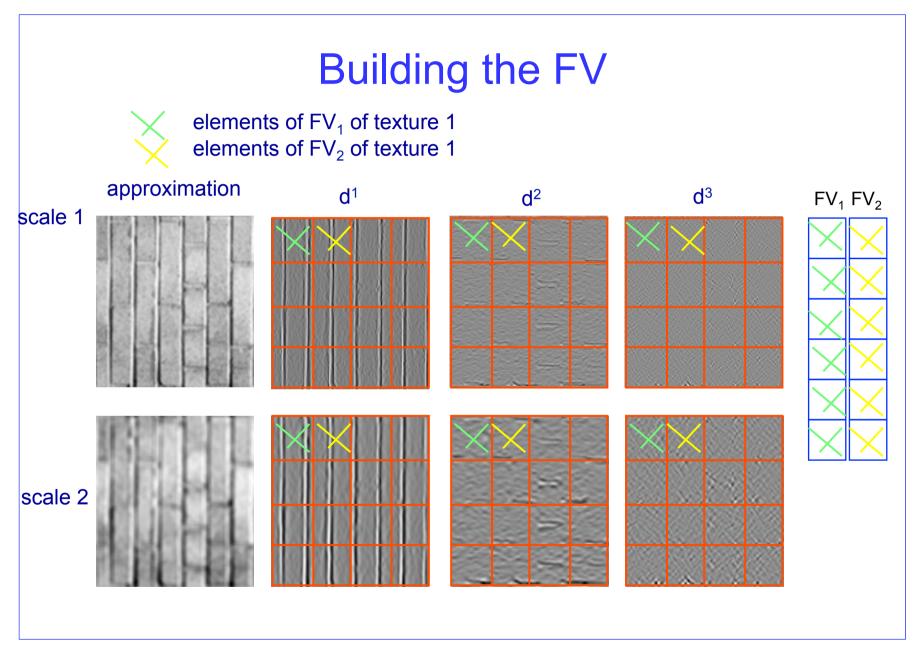


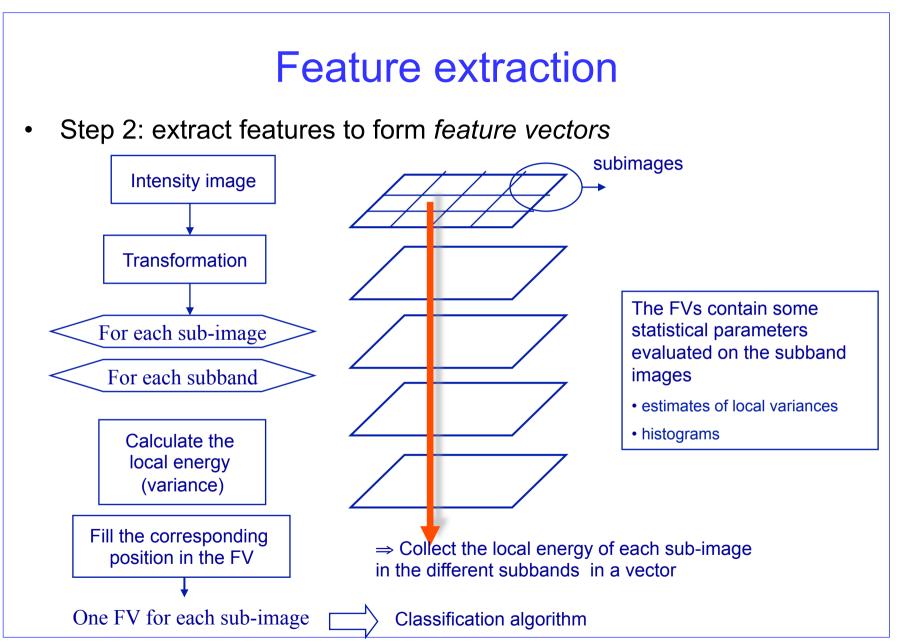
### Image pyramid: feature extraction



Texture features are claculated over the blocks and gathered into feature vectors.

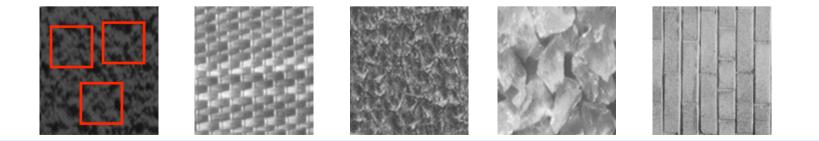






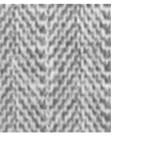
### **Texture features**

- No agreed reference definition
  - Texture is property of areas
  - Involves spatial distributions of grey levels
  - A region is perceived as a texture if the number of primitives in the field of view is sufficiently high
  - Invariance to translations
  - Macroscopic visual attributes
    - uniformity, roughness, coarseness, regularity, directionality, frequency [Rao-96]
  - Sliding window paradigm

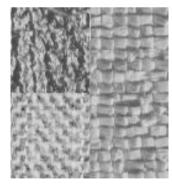


## **Texture analysis**

- Texture segmentation
  - Spatial localization of the different textures that are present in an image
  - Does not imply texture recognition (classification)
  - The textures do not need to be *structurally* different
  - Apparent edges
    - Do not correspond to a discontinuity in the luminance function
    - Texture segmentation ↔ Texture segregation

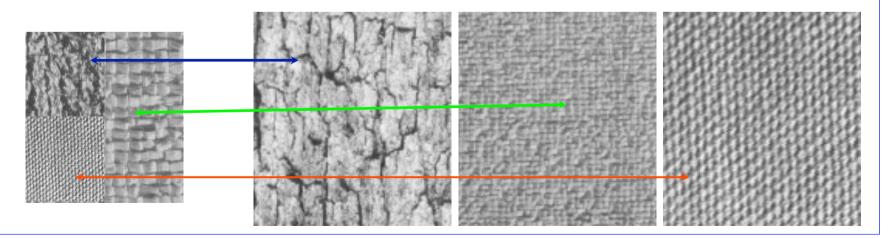






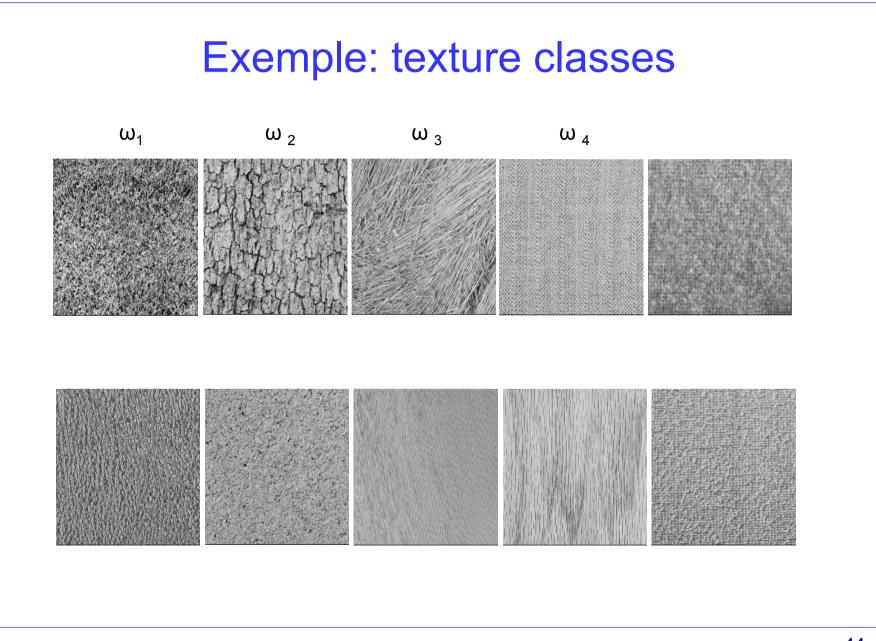
### **Texture analysis**

- Texture classification (recognition)
  - Hypothesis: textures pertaining to the same class have the same visual appearance → the same perceptual features
  - Identification of the class the considered texture belongs to within a given set of classes
  - Implies texture recognition
  - The classification of different textures within a composite image results in a segmentation map



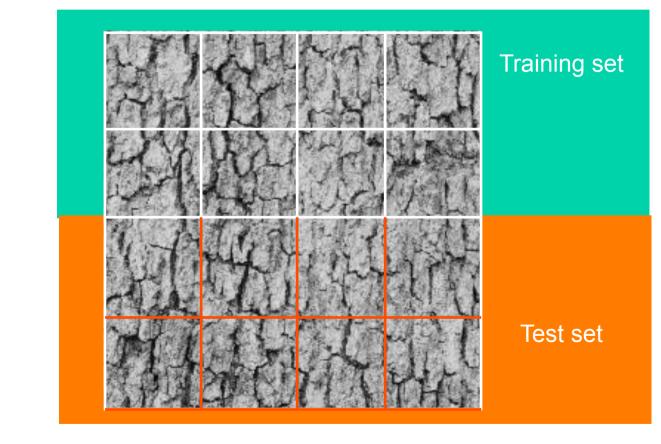
## **Texture classification**

- Method
  - Describe the texture by some *features* which are related to its appearance
    - Texture  $\rightarrow$  class  $\rightarrow \omega_k$
    - Descriptors  $\rightarrow$  Feature Vectors (FV)  $\rightarrow x_{i,k}$
  - Define a distance measure for FV
  - Choose a classification rule
    - Recipe for comparing FV and choose 'the winner class'
  - Assign the considered texture sample to the class which is the *closest* in the feature space



# **FV** extraction

• Step 1: create independent texture instances



### **Co-occurrence** matrix

- A co-occurrence matrix, also referred to as a co-occurrence distribution, is defined over an image to be the *distribution of co-occurring values at a given offset*.
- Mathematically, a co-occurrence matrix C<sub>k,l</sub>[i,j] is defined over an NxM image I, parameterized by an offset (k,I), as:

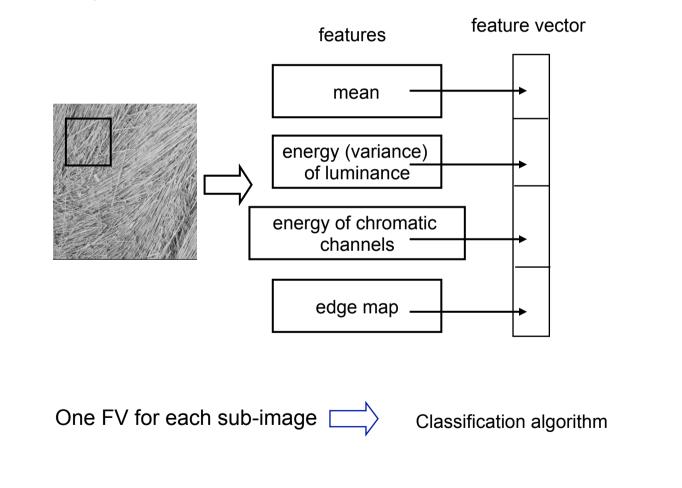
gray level values

$$C_{k,k}[i,j] = \sum_{p=1}^{N} \sum_{q=1}^{M} \begin{cases} 1, \text{ if } I(p,q) = i \text{ and } I(p+k,q+l) = j \\ 0, \text{ otherwise} \end{cases}$$

 The co-occurrence matrix depends on (k,l), so we can define as many as we want

### **Feature extraction**

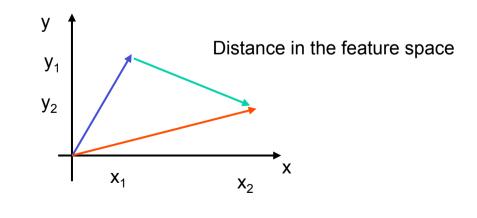
• Step 2: extract features to form *feature vectors* 



#### Feature vector distance

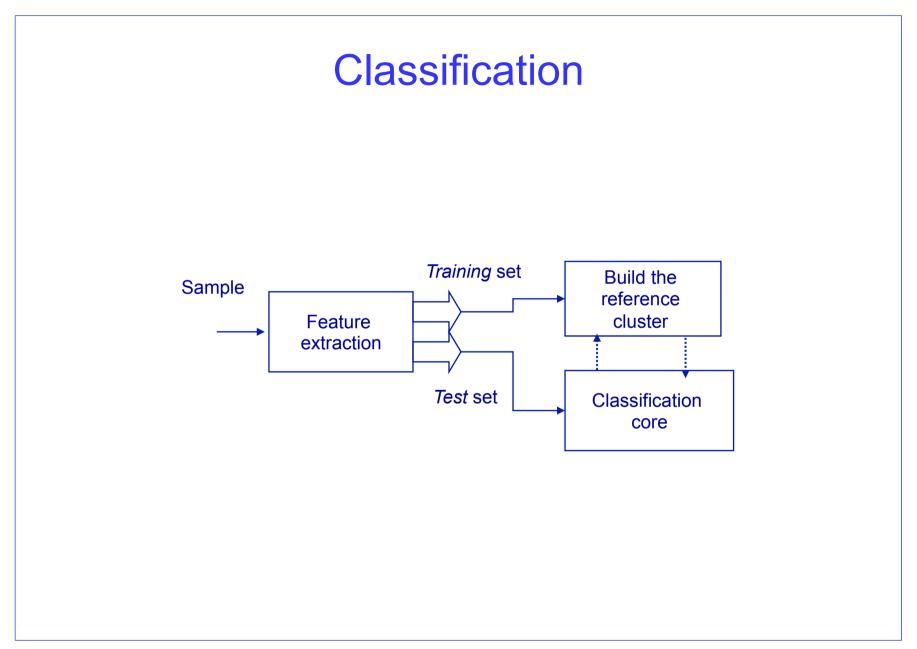
- Step 3: definition of a distance measure for feature vectors
  - Euclidean distance

$$d(\vec{v}_1, \vec{v}_2) = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2 + \dots + (z_1 - z_2)^2}$$
  
$$\vec{v}_1 = \{x_1, y_1, \dots, z_1\}$$
  
$$\vec{v}_2 = \{x_2, y_2, \dots, z_2\}$$



## **Classification steps**

- Step 4: Classification
  - Phase 1: Training
    - The classification algorithm is provided with many examples of each texture class in order to build clusters in the feature space which are representative of each class
    - Examples are sets of FV for each texture class
    - Clusters are formed by aggregating vectors according to their "distance"
  - Phase 2: Testing
    - The algorithm is fed with an example of texture ω<sub>i</sub> (vector x<sub>i,k</sub>) and determines which class it belongs to as the one to which it is "closest" in the feature space



### Conclusions

- No golden rule exists for clustering/classification
- Major issues:
  - Feature selection
  - Definition of a metric for measuring distances
  - Definition of a representative training set
  - Choice of the classification/clustering strategy
- Possible solution: classifier fusion
  - Consider a set of different classifiers and combine their results