



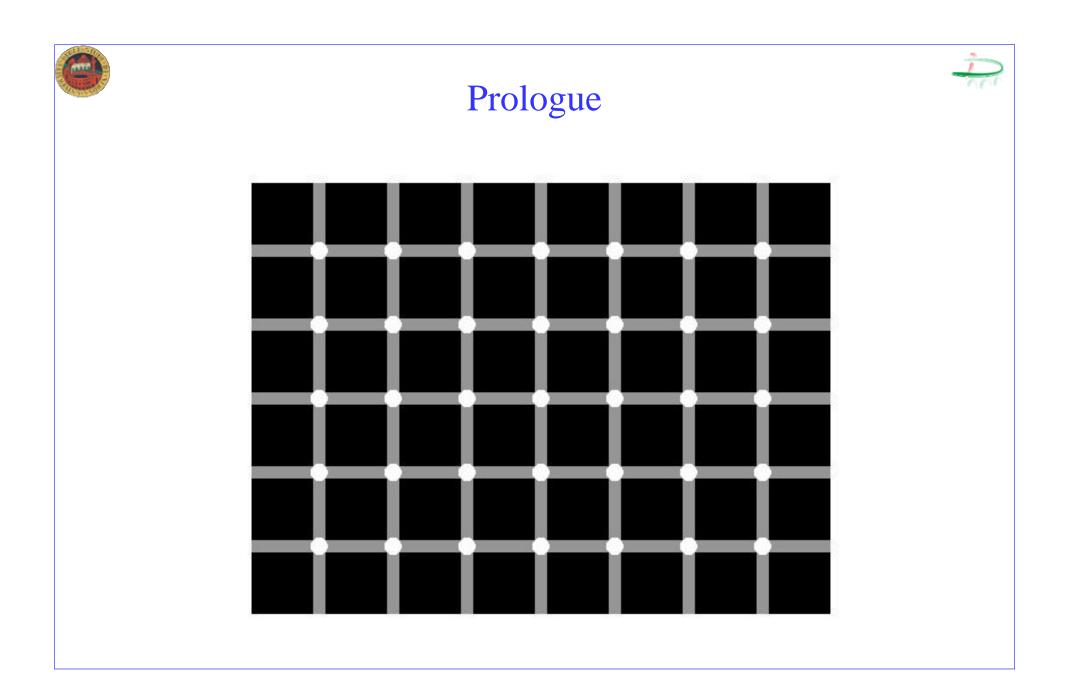


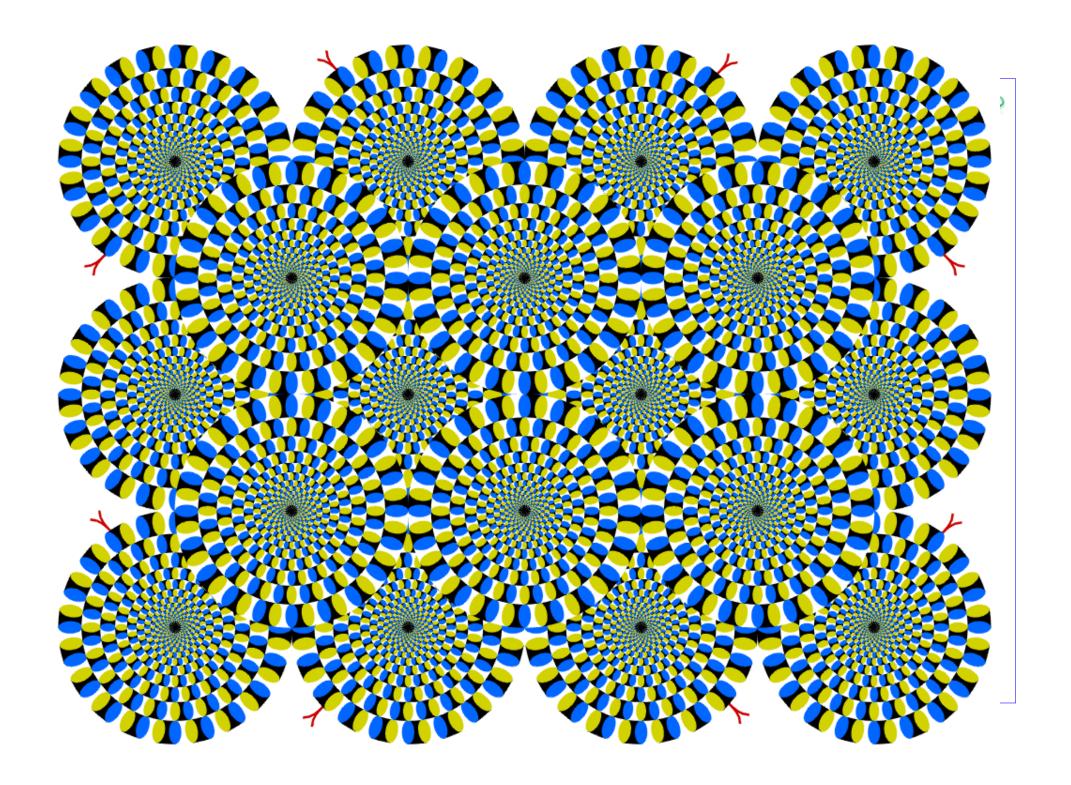
Multimedia communications

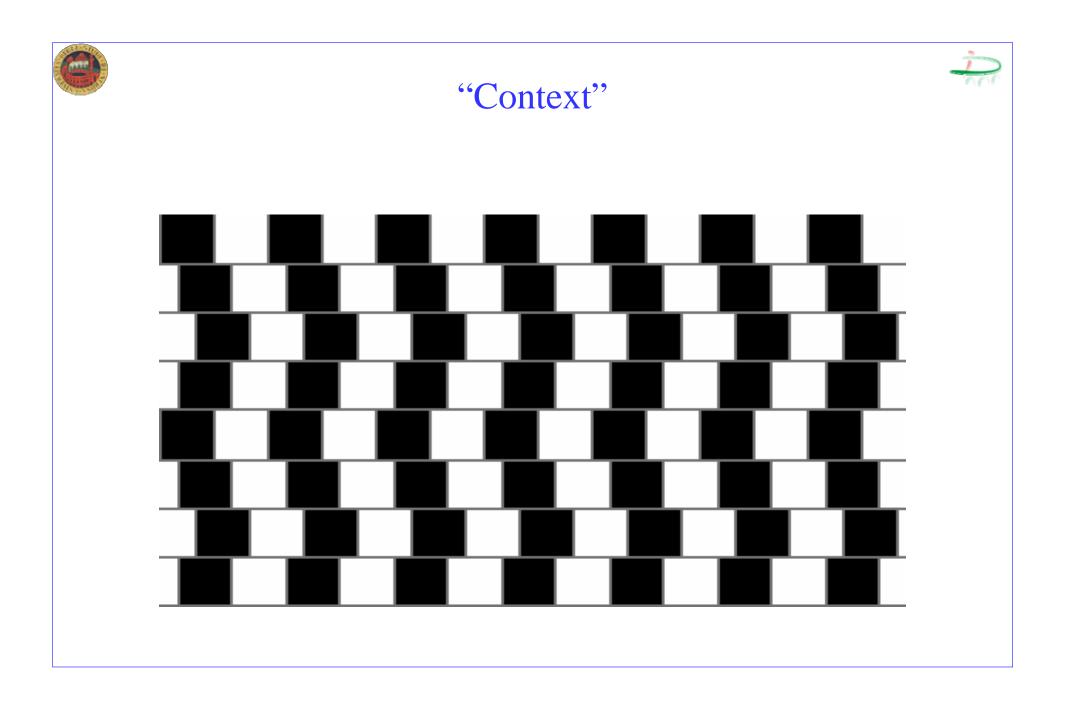
Comunicazione multimediale

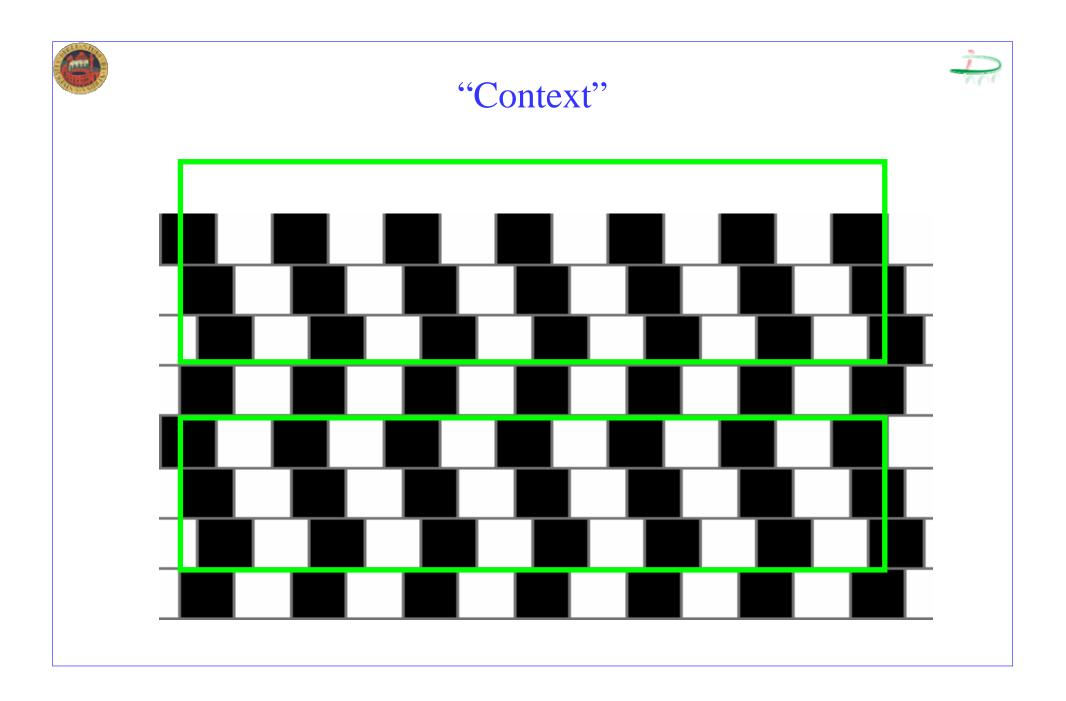
G. Menegaz

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Course overview

(AP)



• Goal

- The course is about wavelets and multiresolution
 - Theory: 4 hours per week
 - Tuesday 10.30-13.30 (10.30-12.00 + 12.45-13.30)
 - Wed. 9.30-10.30
 - Laboratory
 - Wed. 14.30-16.30 (Lab. Gamma)
- Contents
 - Review of Fourier theory
 - Wavelets and multiresolution
 - Review of Information theoretic concepts
 - Applications
 - Image coding (JPEG2000)
 - Feature extraction and signal/image analysis



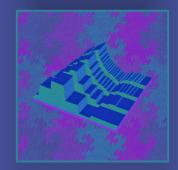




Stéphane Mallat



Wavelets and Subband Coding

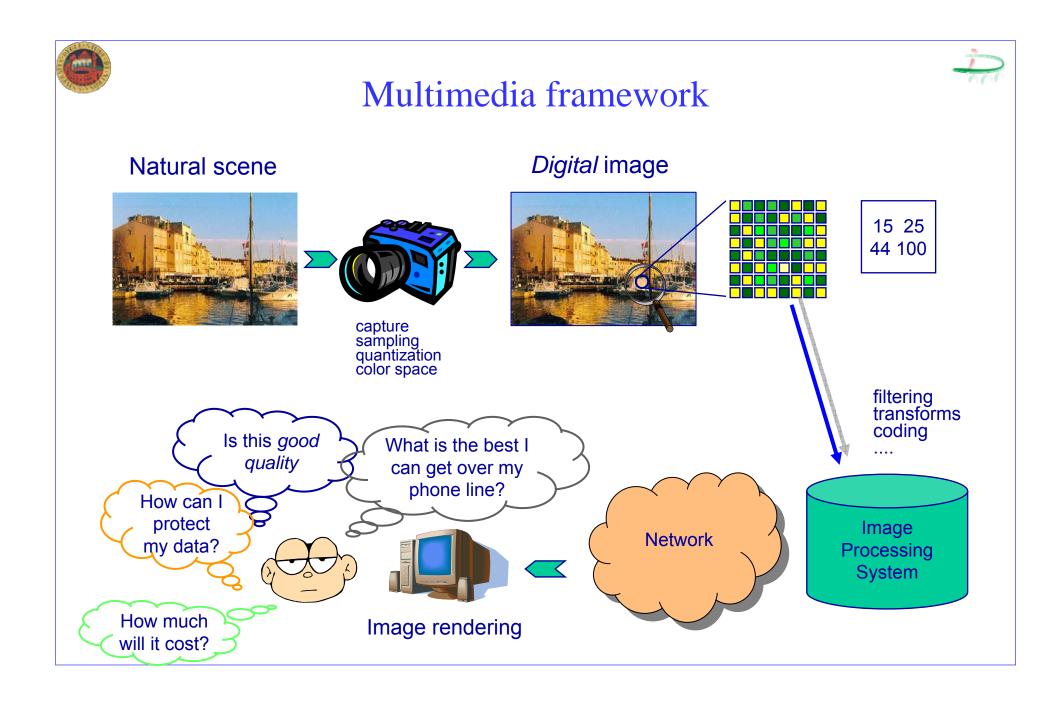


Martin Vetterli & Jelena Kovačević



Next 2 weeks scheduling

- Tue. March 9: moved to Thu. March 11 14.30-16.30, Room B
- Wed. March 17: moved from 10.30-11.30 to 16.30-17.30 (or 18.30), Room H





Telecommunications for Multimedia

Good news

- It is fun!
- Get in touch with the state-of-the-art technology
- Convince yourself that the time spent on maths&stats was not wasted
- Learn how to map theories into applications
- Acquiring the tools for doing good research!

Bad news

- Some theoretical background is unavoidable
 - Mathematics
 - Fourier transform
 - Linear operators
 - Digital filters
 - Wavelet transform
 - (some) Information theory



Issues in mulitmedia systems

- Broadcasting needs high information carrying capacity
 - Efficient data representation
 - Projection into suitable (perception based?) spaces
 - Color processing
 - Efficient encoding
 - Reduction of redundancy
 - Classical information theoretical principles (entropy based)
 - Novel approaches based on visual perception (perception based)

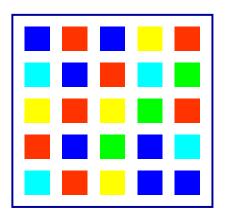
• Standardization

- Openness
 - Ability to adapt to new technologies
- Flexibility
 - Ability to interact with different media
- JPEG2000, MPEG4, MPEG7



Digital images acquisition

- Analog camera+A/D converter
- Digital cameras
 - CCDs (Charge Coupled Devices)
 - CMOS technology
- In both cases: optics
 - lenses, diaphrams



Matrices of photo sensors collecting photons of given wavelength



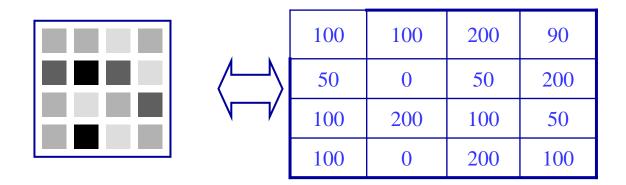
Features of the capture devices:

- Size and number of photosites
- Noise
- Transfer function of the optical filter

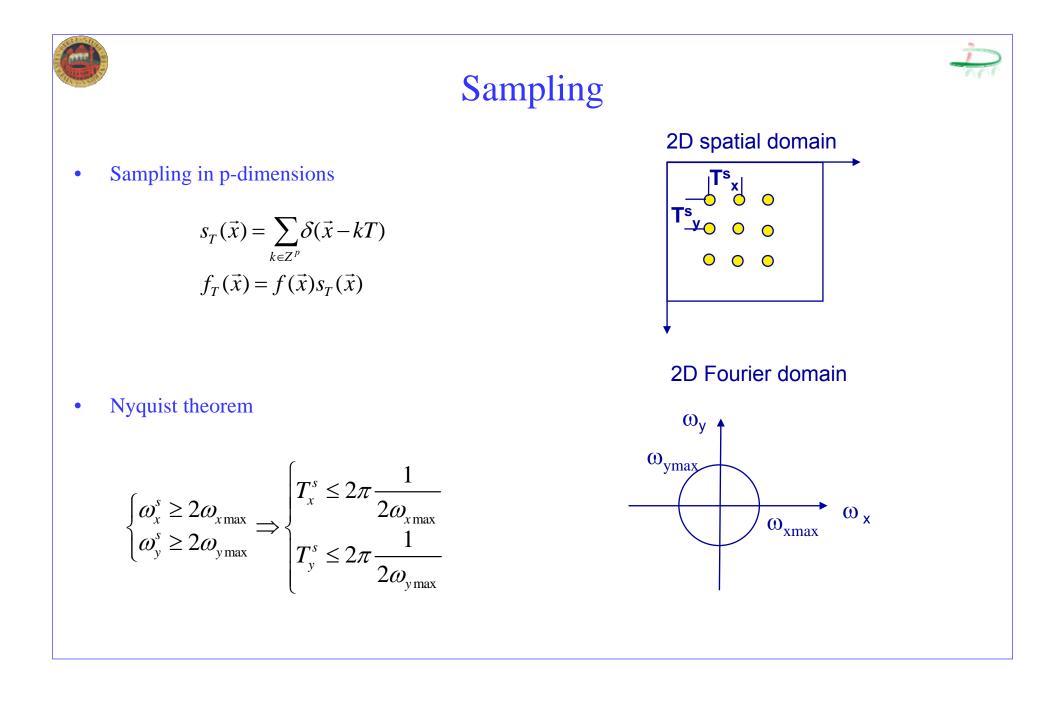


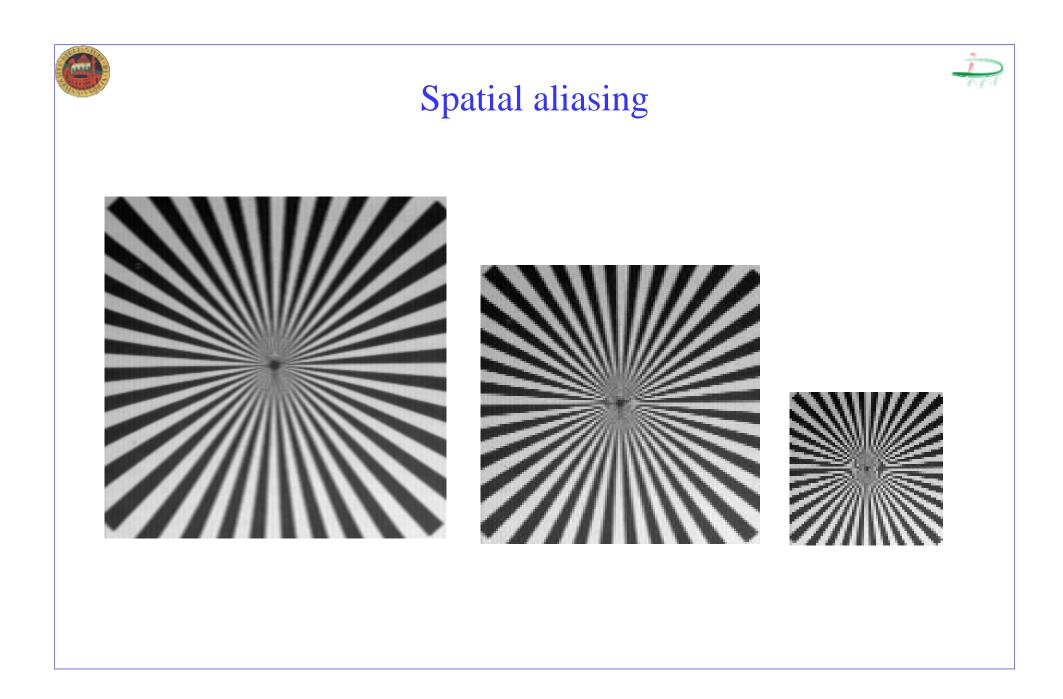


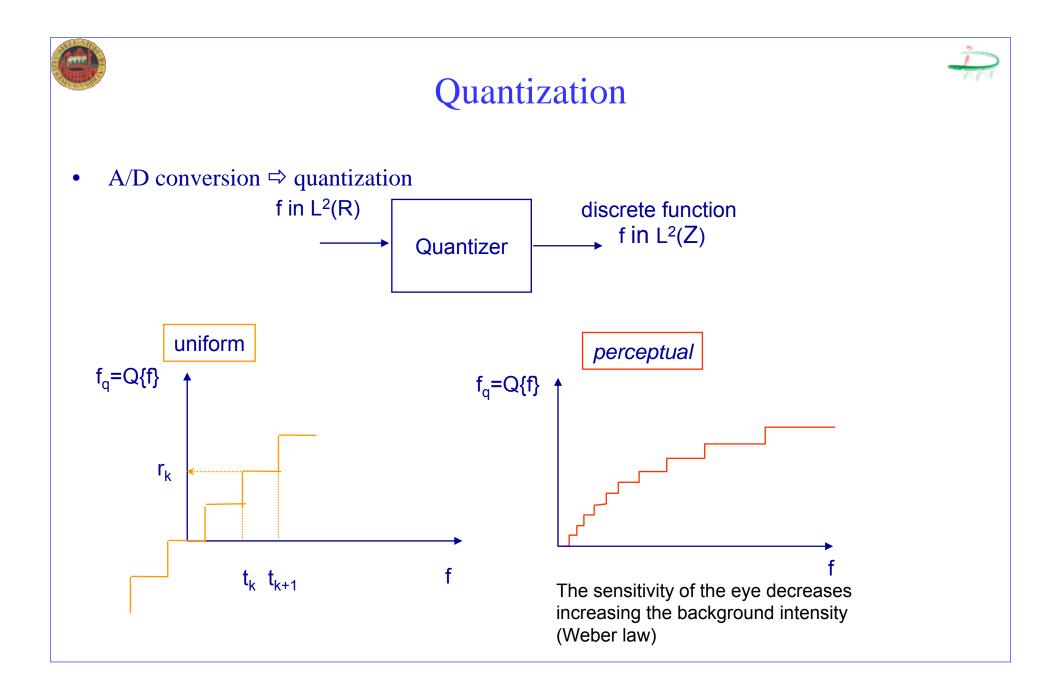
Basics: graylevel images

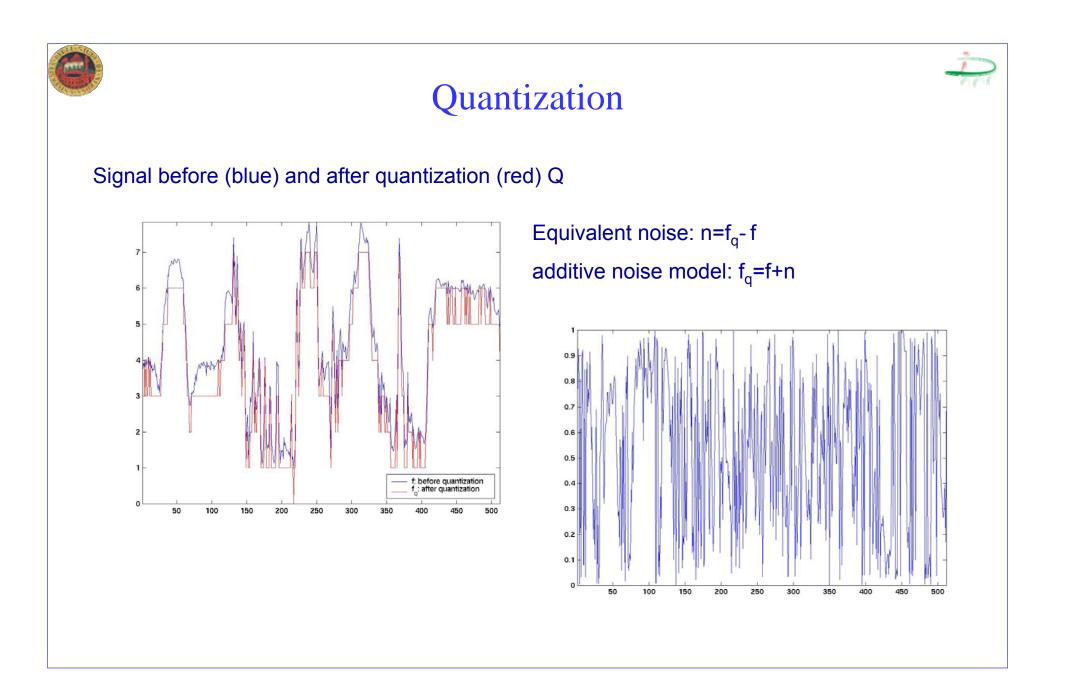


Images : Matrices of numbers Image processing : Operations among numbers bit depth : number of bits/pixel *N* bit/pixel : 2^{N-1} shades of gray (typically N=8)











Distortion measure

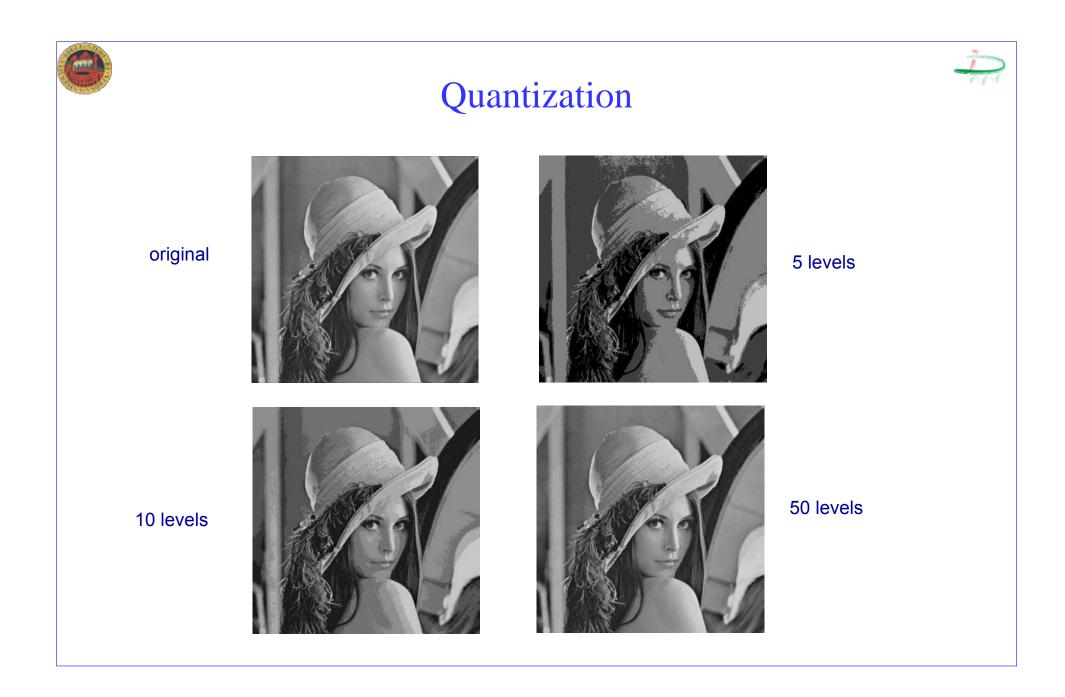


• Distortion measure

$$D = E\left[\left(f_Q - f\right)^2\right] = \sum_{k=0}^{K} \int_{t_k}^{t_{k+1}} (f_Q - f)^2 p(f) df$$

- The distortion is measured as the expectation of the mean square error (MSE) difference between the original and quantized signals.
- Lack of correlation with perceived image quality
 - Even though this is a very natural way for the quantification of the quantization artifacts, it is not representative of the *visual annoyance* due to the majority of common artifacts.









Mathematical tools



Introduction



- Such representations can be constructed by decomposing signals over elementary waveforms chosen in a family called a *dictionary*.
- An orthogonal basis is a dictionary of minimum size that can yield a sparse representation if designed to concentrate the signal energy over a set of few vectors. This set gives a *geometric* signal description.
 - Signal compression and noise reduction
- Dictionaries of vectors that are larger than bases are needed to build sparse representations of complex signals. But choosing is difficult and requires more complex algorithms.
 - Sparse representations in redundant dictionaries can improve pattern recognition, compression, and noise reduction
- Basic ingredients: Fourier and Wavelet transforms
 - They decompose signals over oscillatory waveforms that reveal many signal properties and provide a path to sparse representations



Signals as functions

- CT analogue signals (real valued functions of continuous independent variables)
 - 1D: f=f(t)
 - 2D: f = f(x, y) x, y
 - Real world signals (audio, ECG, pictures taken with an analog camera)
- DT analogue signals (real valued functions of discrete variables)
 - 1D: *f*=*f*[*k*]
 - 2D: *f*=*f*[*i*,*j*]
 - *Sampled* signals
- Digital signals (discrete valued functions of DT variables)
 - 1D: y = y[k]
 - 2D: *y*=*y*[*i*,*j*]
 - Sampled and discretized signals



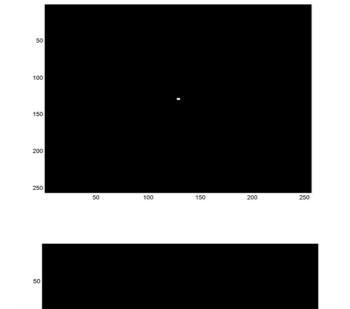
Images as functions

- Gray scale images: 2D functions
 - Domain of the functions: set of (x, y) values for which f(x, y) is defined : 2D lattice [i, j] defining the pixel locations
 - Set of values taken by the function : gray levels
- Digital images can be seen as functions defined over a discrete domain $\{i, j: 0 < i < I, 0 < j < J\}$
 - *I,J:* number of rows (columns) of the matrix corresponding to the image
 - *f=f[i,j]:* gray level in position [*i,j*]

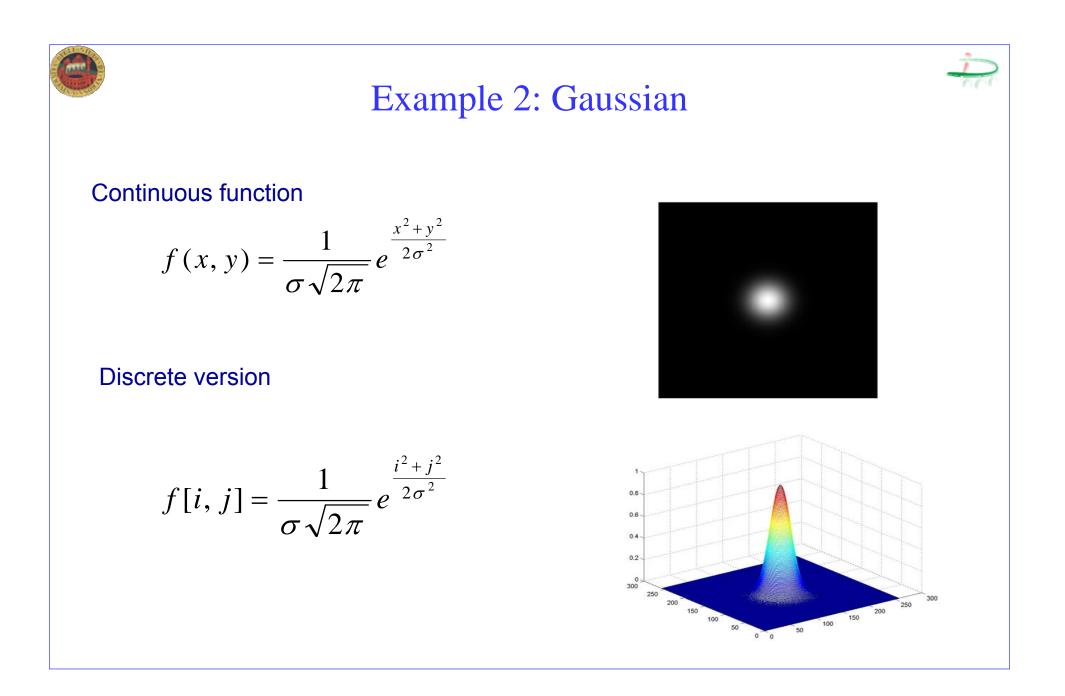


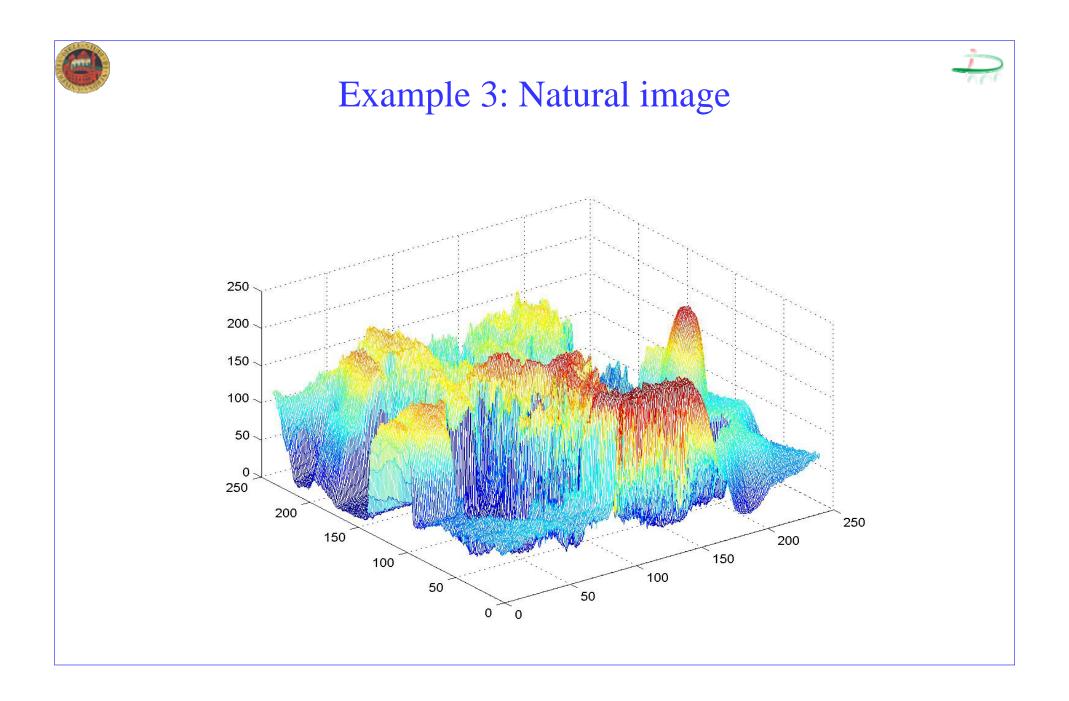
Example 1: δ function

$$\delta[i, j] = \begin{cases} 1 & i = j = 0\\ 0 & i, j \neq 0; i \neq j \end{cases}$$

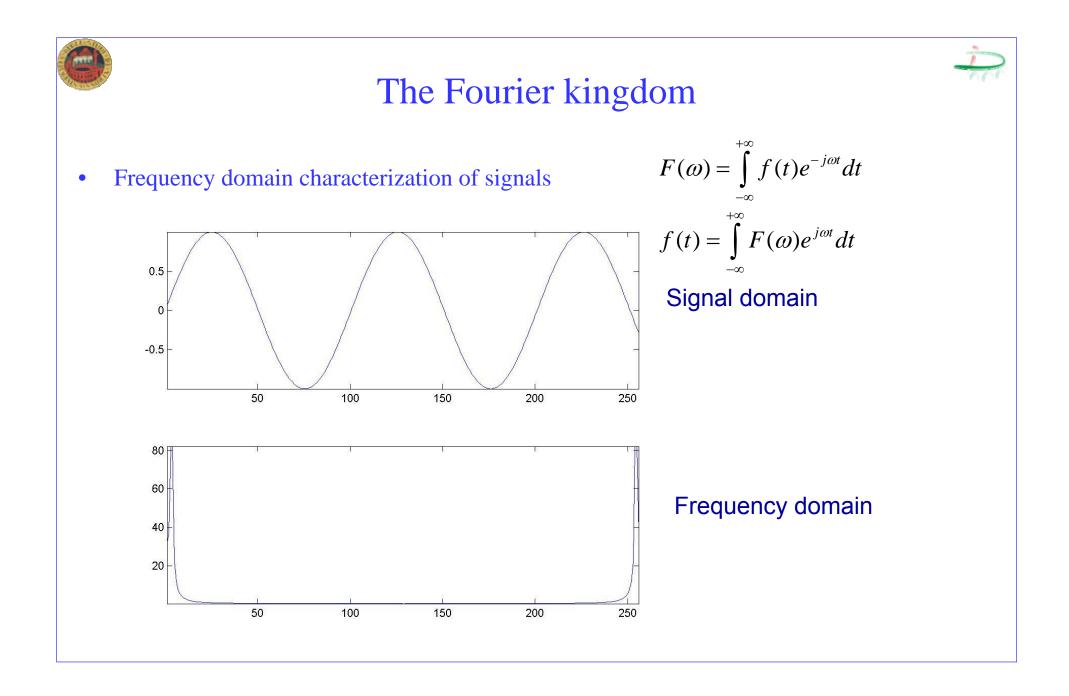


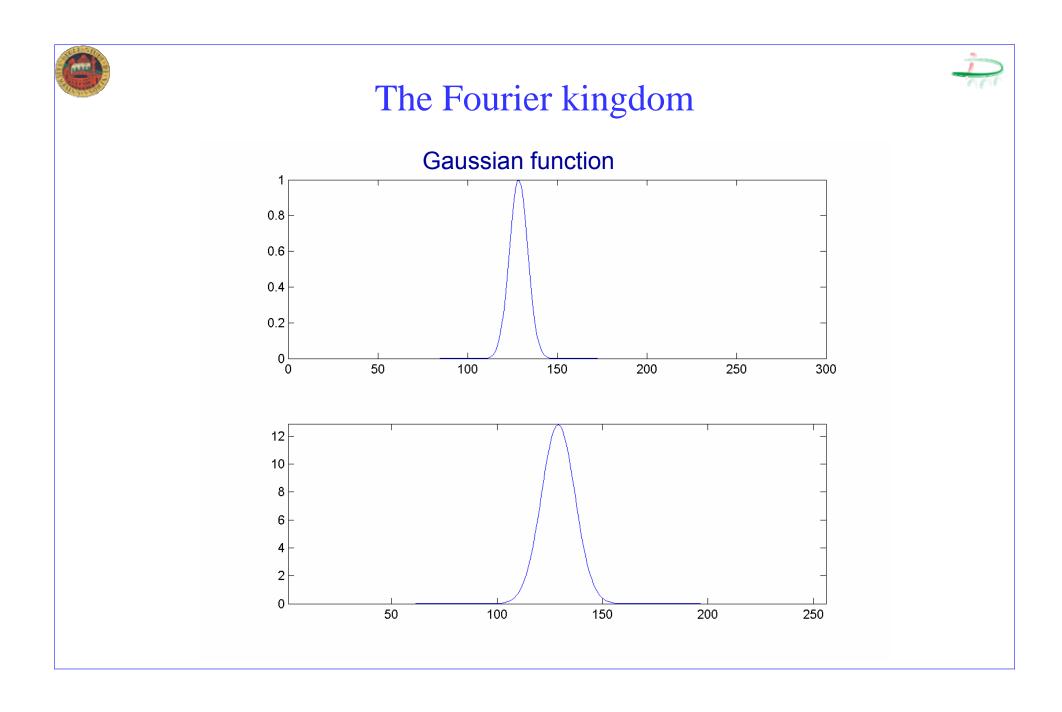
$$\delta[i, j-J] = \begin{cases} 1 & i = 0; j = J \\ 0 & otherwise \end{cases}$$

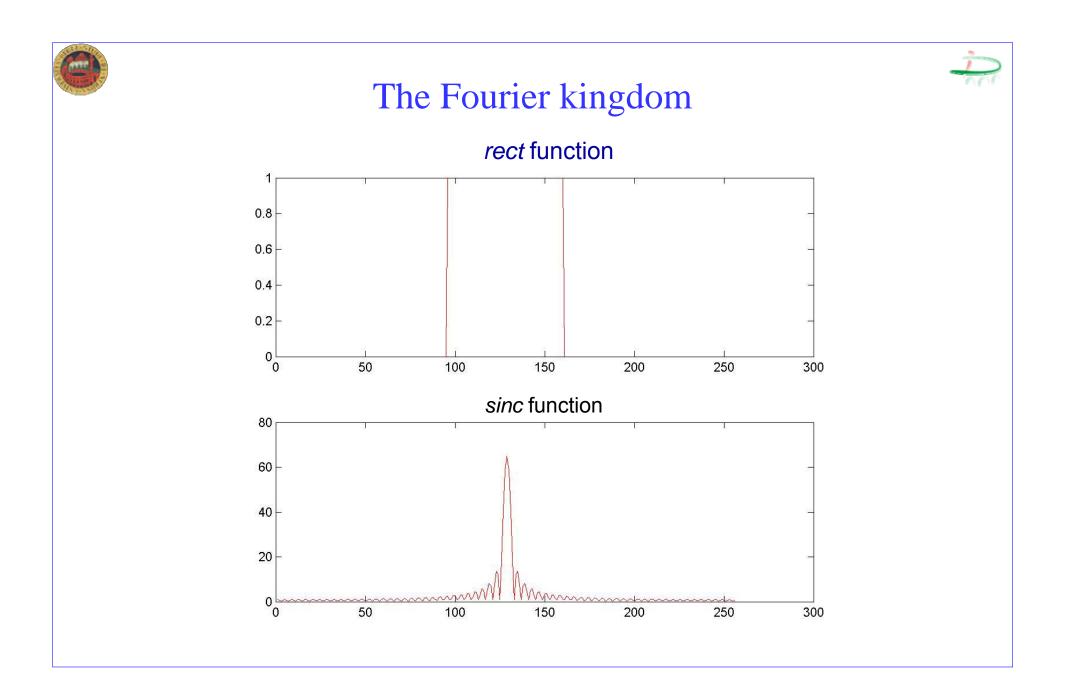


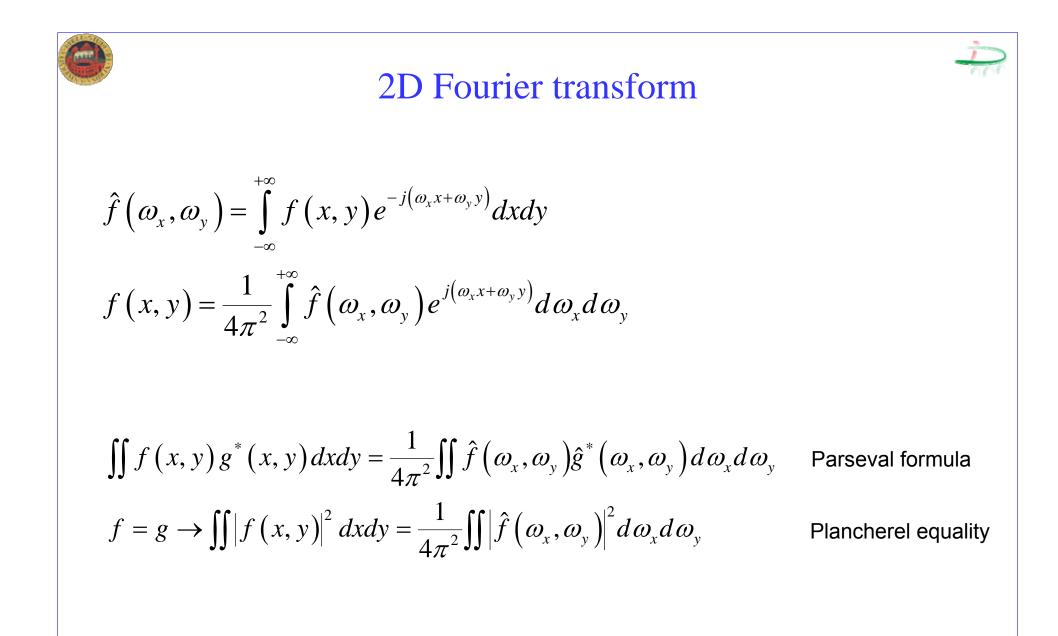


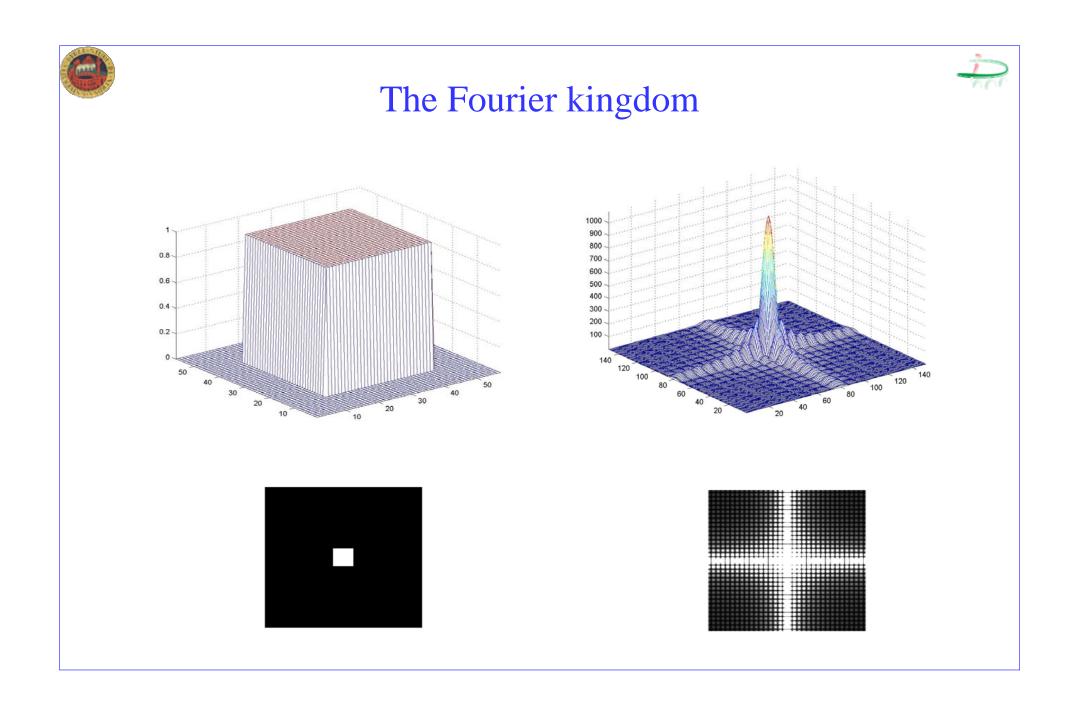






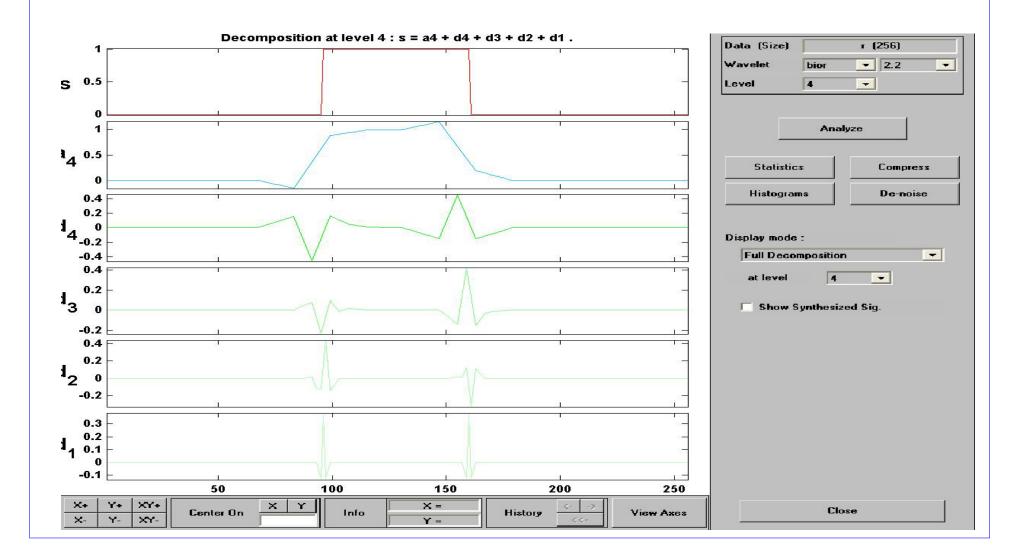


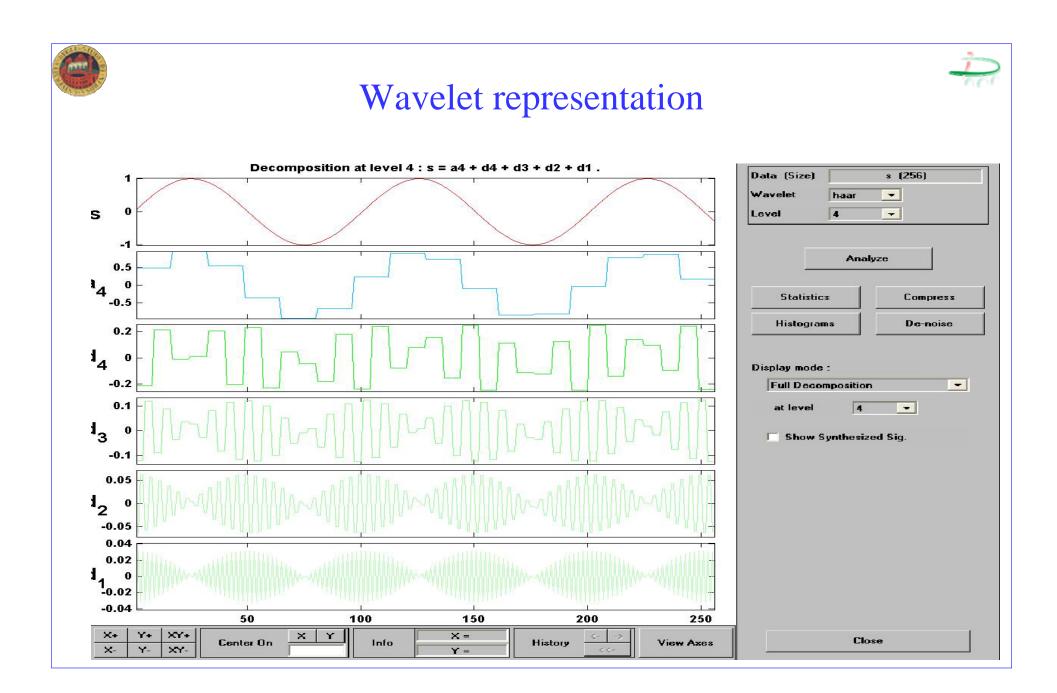


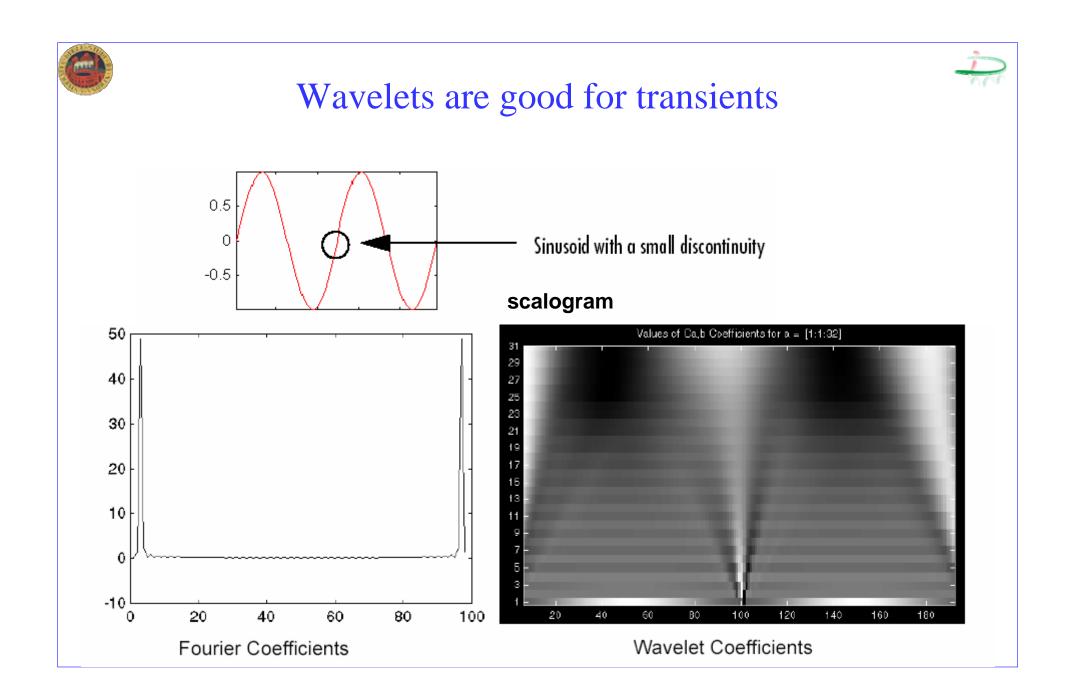


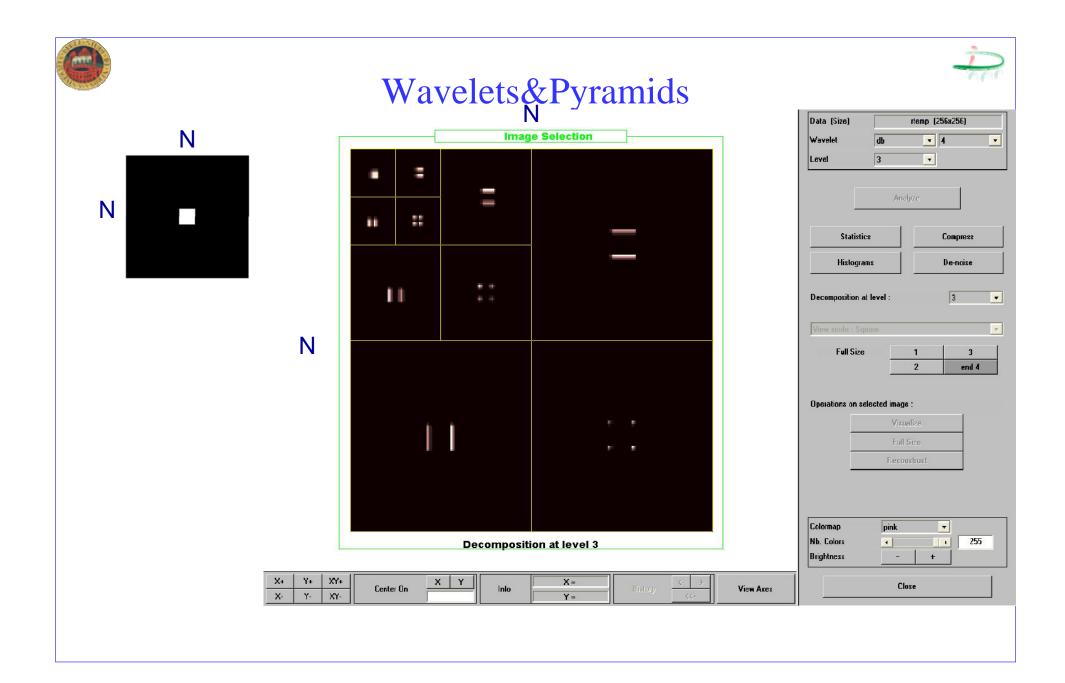
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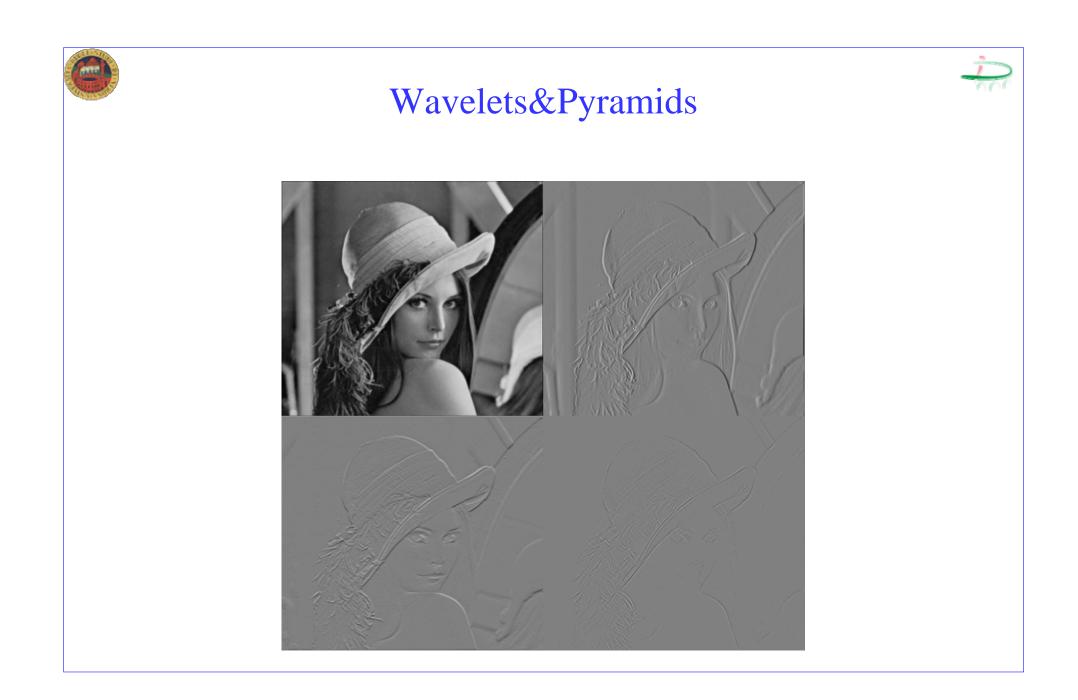
Wavelet representation

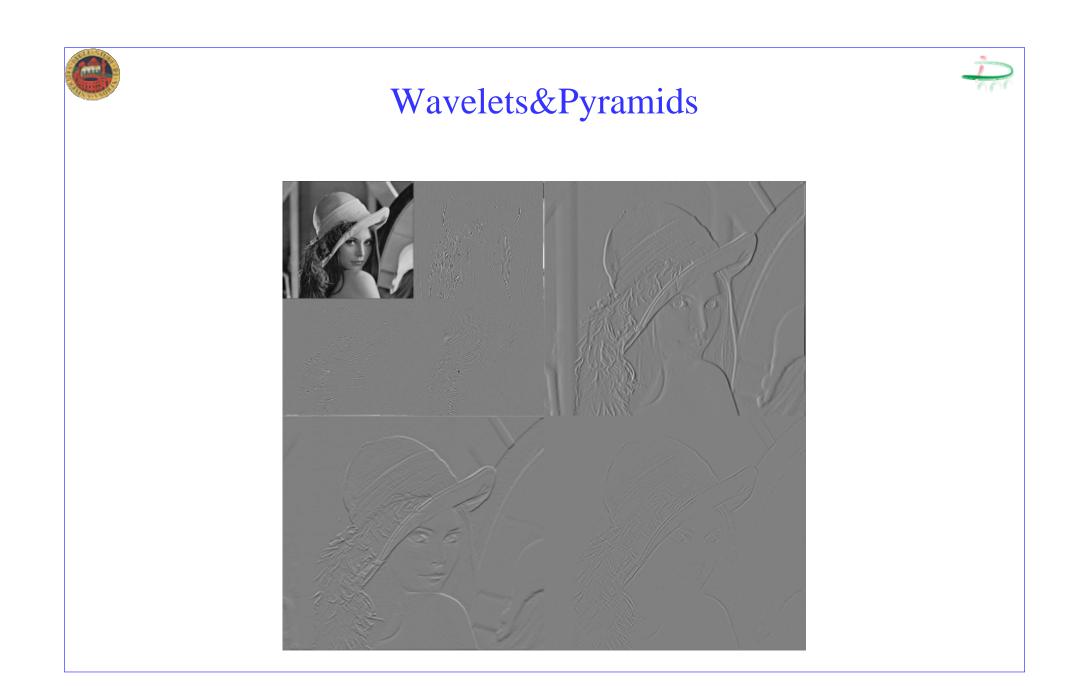


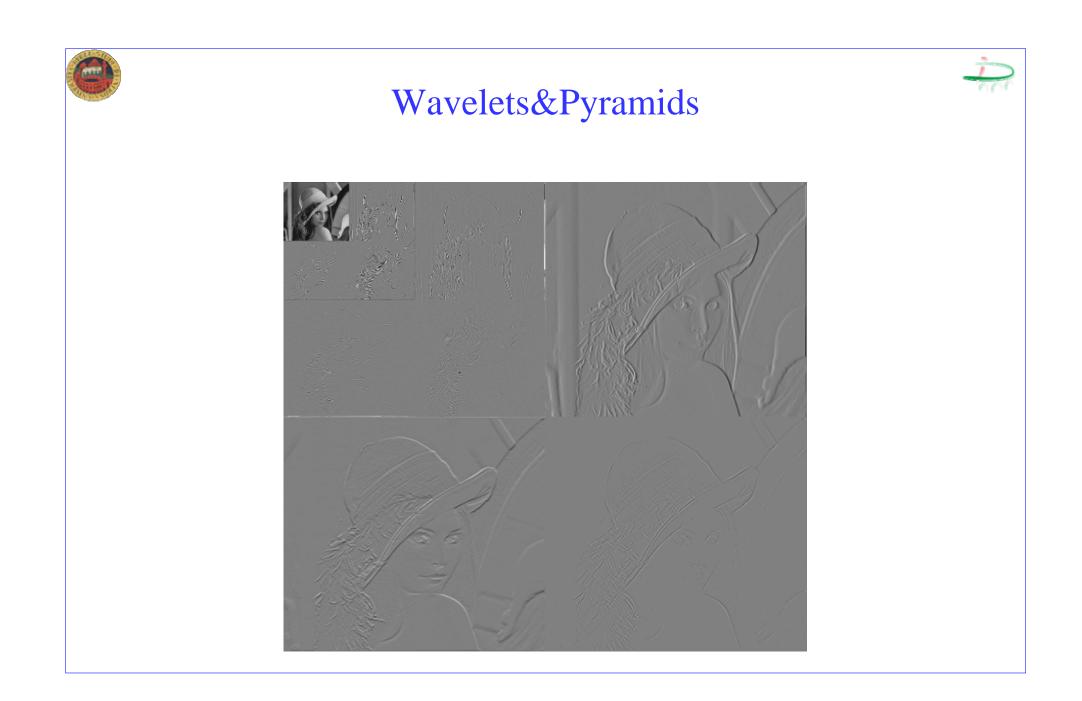


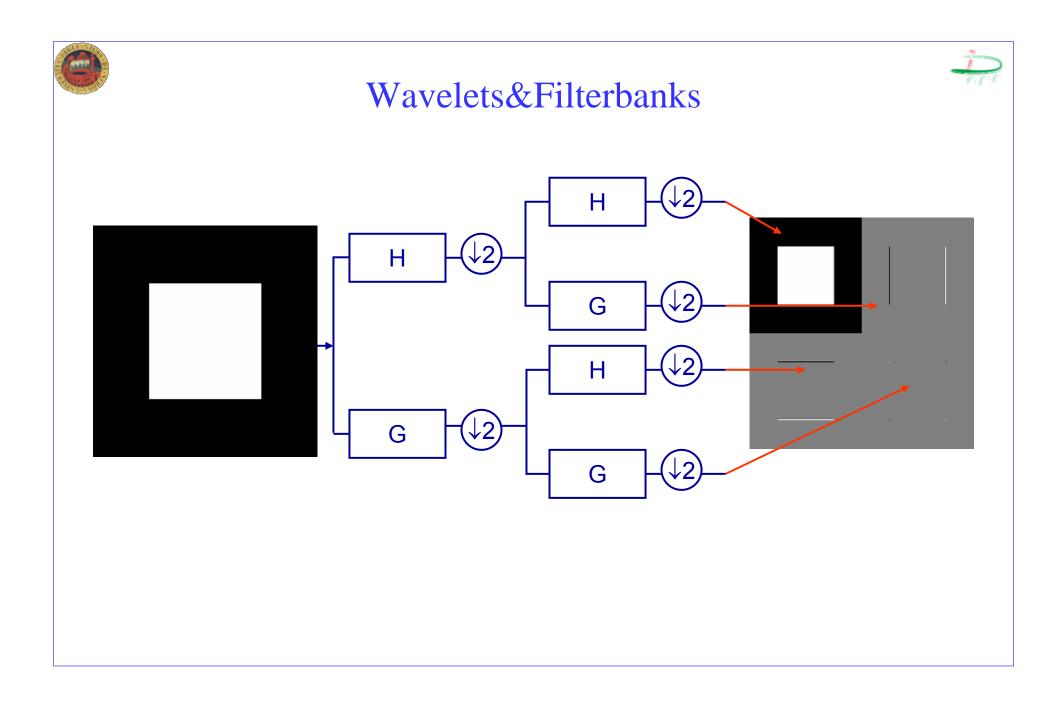


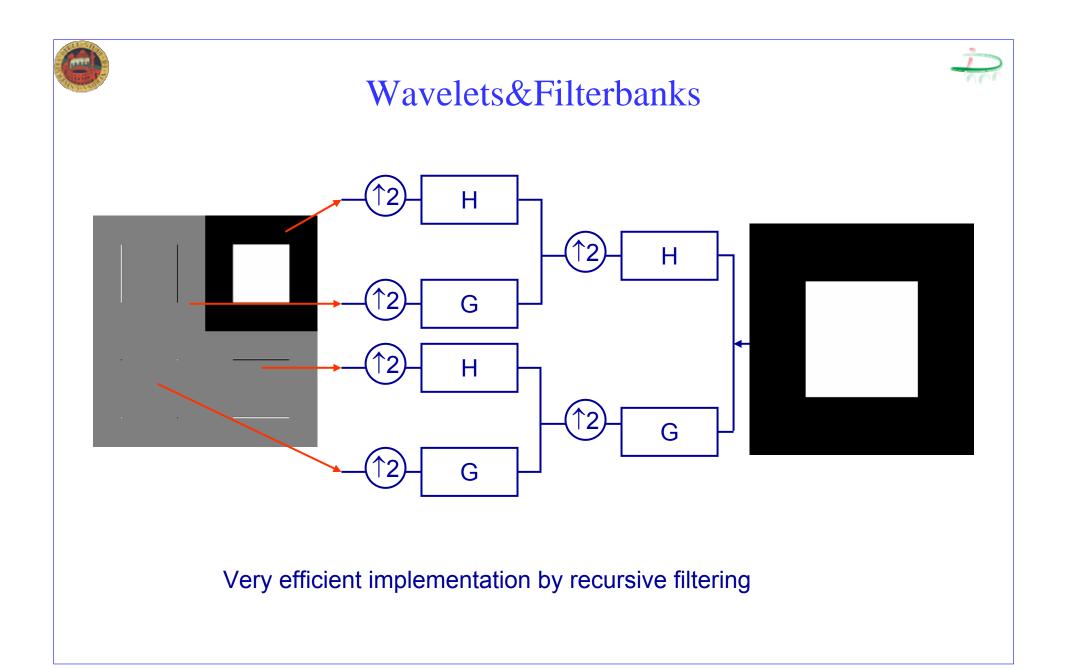














Fourier versus Wavelets

Fourier

- Basis functions are sinusoids
 - More in general, complex exponentials
- Switching from signal domain t to frequency domain f
 - Either spatial or temporal
- Good localization either in time or in frequency
 - Transformed domain: Information on the sharpness of the transient but not on its position
- Good for stationary signals but unsuitable for transient phenomena

Wavelets

- Different families of basis functions are possible
 - Haar, Daubechies', biorthogonal
- Switching from the signal domain to a *multiresolution* representation
- Good localization in time and frequency
 - Information on *both* the *sharpness* of the transient and the *point* where it happens
- Good for any type of signal

