

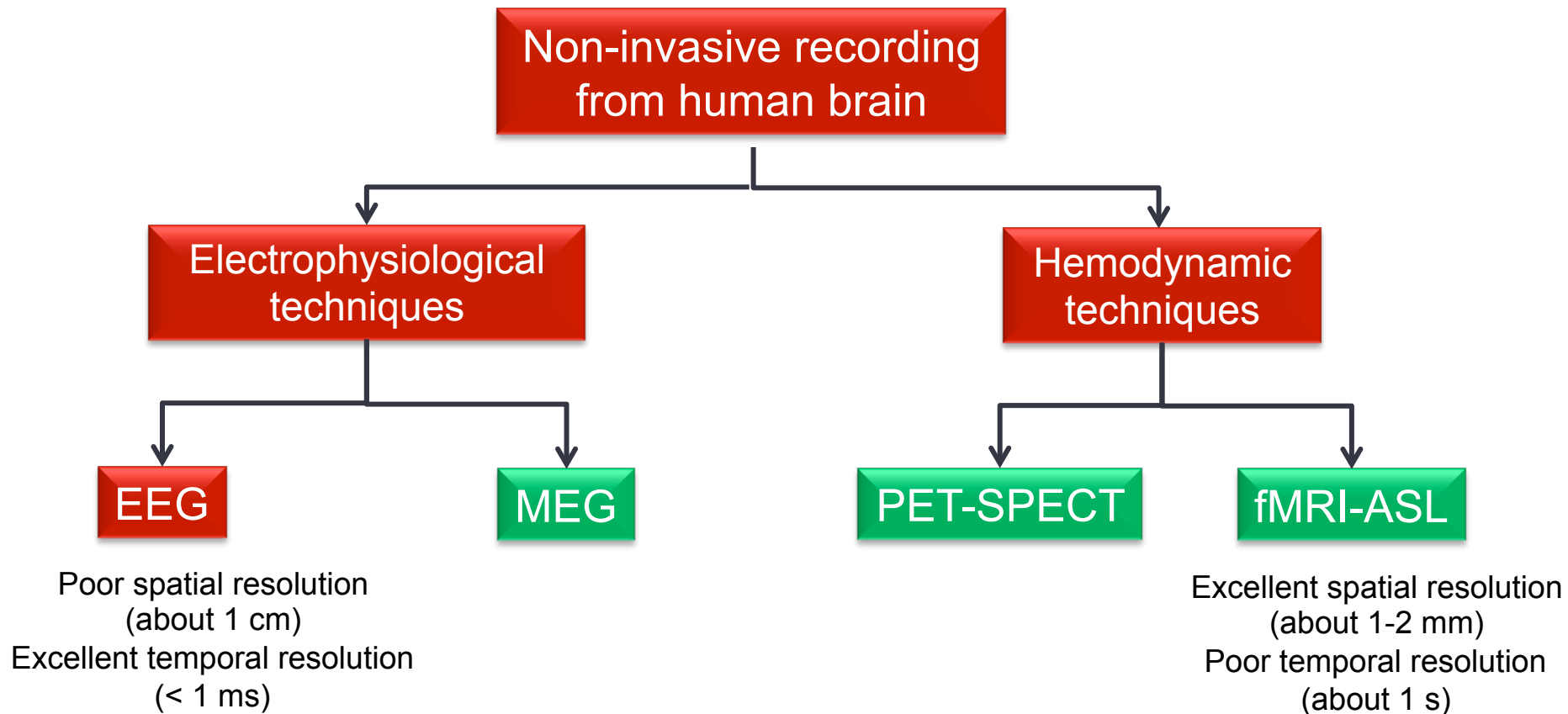
EEG SIGNAL PROCESSING

3. Electrical Source Imaging

Silvia F. Storti

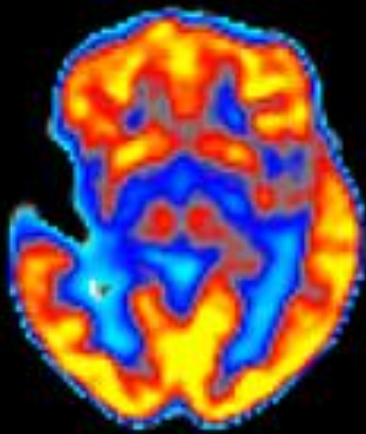
silviafrancesca.storti@univr.it

Measuring Neural Activity



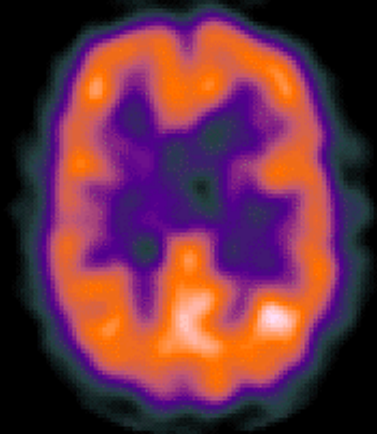
Non-invasive imaging techniques

Measuring hemodynamic activity



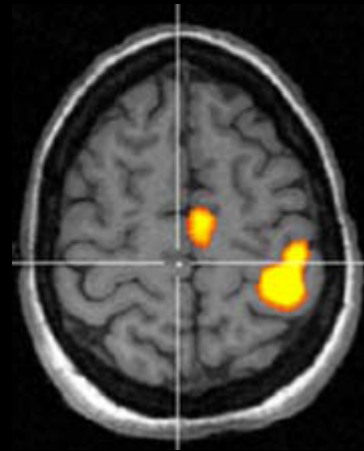
PET

(positron emission
tomography)



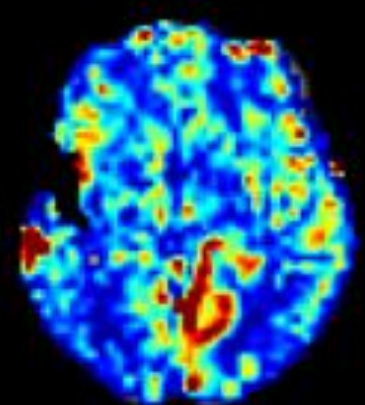
SPECT

(single photon emission
computed tomography)



fMRI

(functional magnetic
resonance imaging)



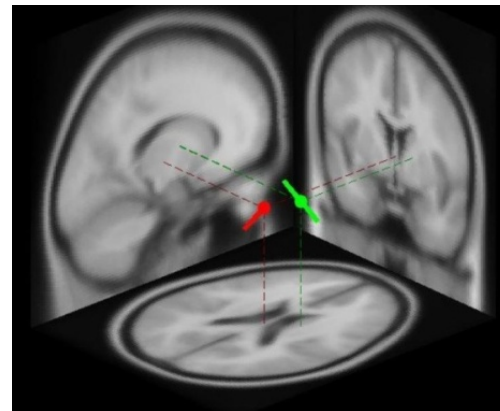
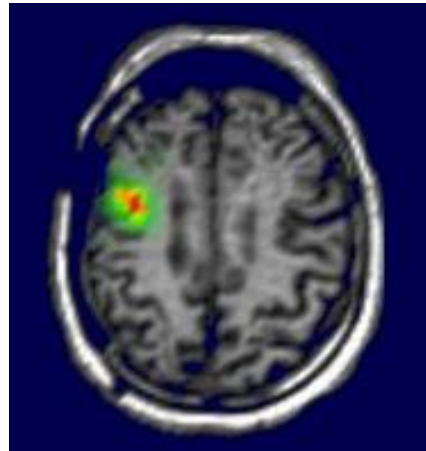
ASL

(arterial spin
labelling)

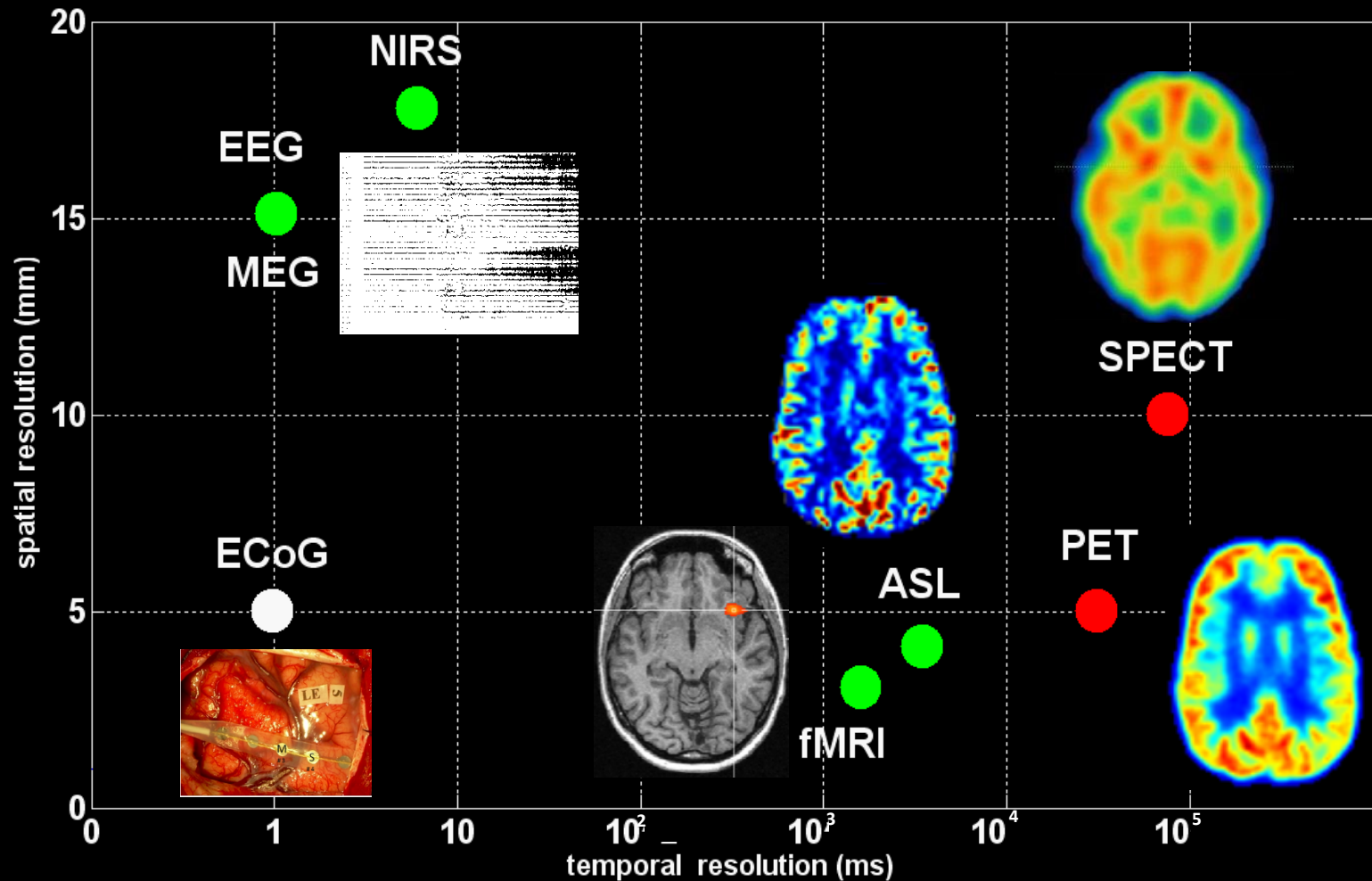
Non-invasive imaging techniques



Imaging techniques

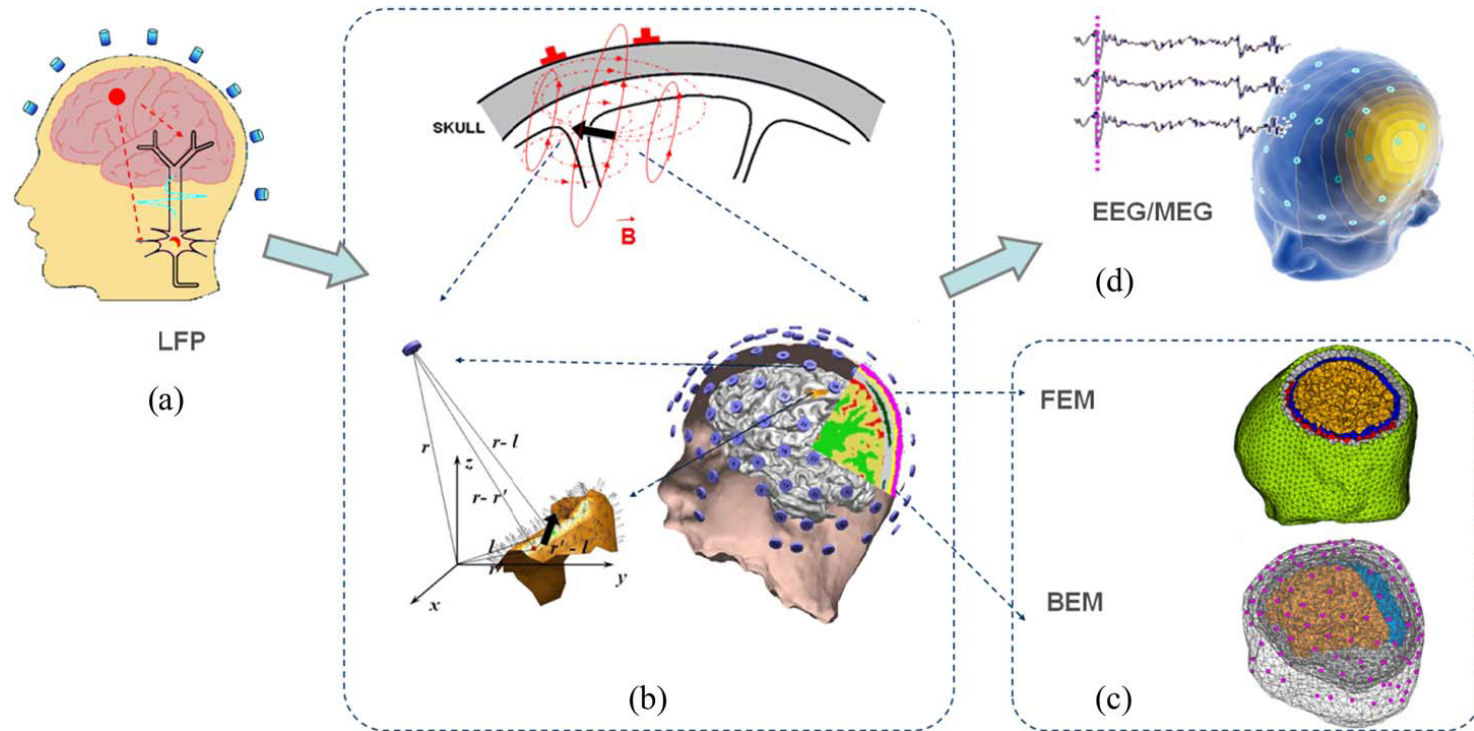


Temporal and Spatial resolution



Electrical Source Imaging

Electrophysiological imaging of brain activity



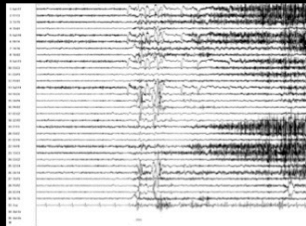
EEG/MEG signals are mainly generated from synchronized activation of cortical pyramidal neurons located within the cortical gray matter.

When pyramidal neurons are excited, the synaptic currents flowing across the cell membranes induce local excitatory postsynaptic potentials as well as magnetic fluxes, which collectively form the sources for EEG and MEG, respectively. When cortical neurons in columnar vicinity are in synchronized activation, the synaptic current flow, at a macroscopic level, approximates a **current dipole** located on cortical surface and oriented perpendicular to the local cortical surface.

The configuration (e.g. **location, magnitude, and orientation**) of such current dipole can be related with EEG or MEG signals through the modeling of head volume conduction.

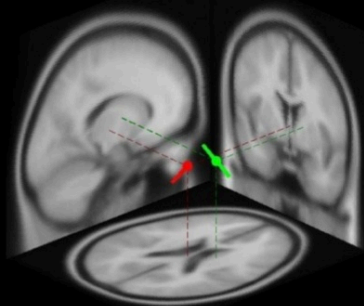
Electrical Source Imaging (ESI)

Scalp
electric field



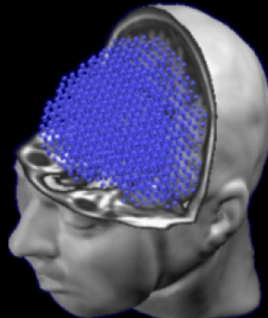
SOURCE MODEL

Dipole



ECD assumes the underlying neuronal sources to be focal

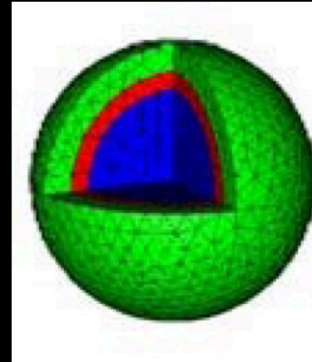
Distributed



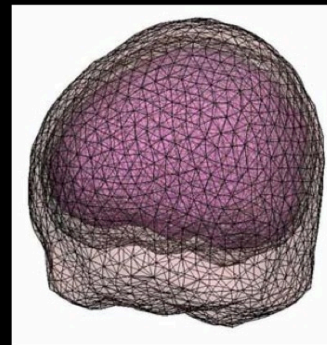
The 3D grid of solution points is considered as a possible location of a brain activity source

HEAD MODEL

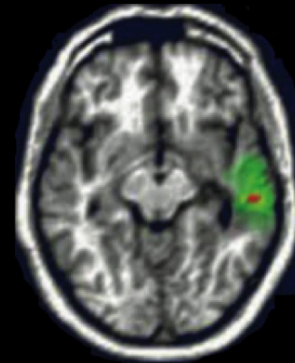
Spherical



Realistic



Source



Electrical Source Imaging (ESI)

Electrophysiological source imaging (ESI) is a model-based approach for imaging electrical sources associated with brain activation from noninvasive EEG or MEG measurements.

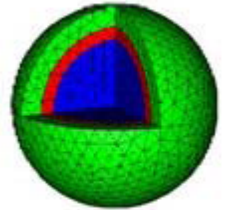
ESI entails:

- 1) **forward modeling** of brain sources and head volume conduction to establish a linear source-to-measurement relationship.
- 2) **inverse imaging** of brain electrical sources from measured EEG, via various strategies, most commonly dipole localization and distributed source imaging.

Head models

1. Sphere-shaped head models

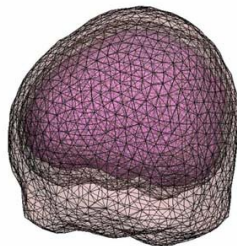
(uniform conductivity) → computationally efficient



2. Realistic Head Model: these numerical models allow incorporating the realistic geometry of the head and brain after reconstruction of the anatomical structure from individual or standardized MRI data sets.

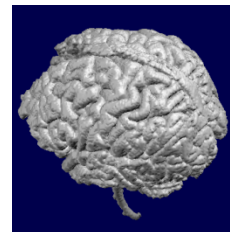
Boundary Element Method (BEM):

gathers a more realistic shape of brain compartments of isotropic and homogeneous conductivities by using closed triangle meshes



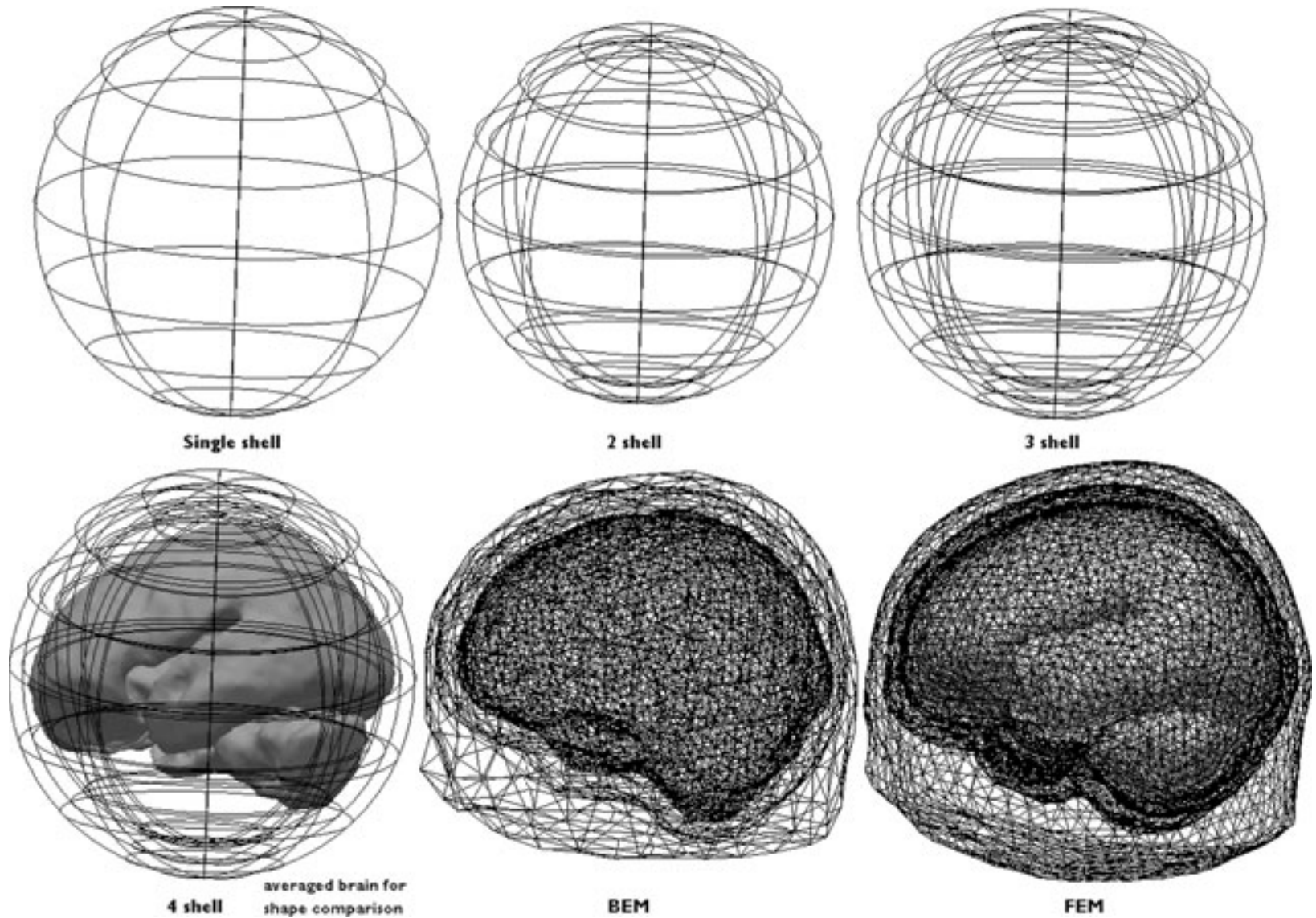
Meijs et al., 1987

Finite-Element Method (FEM): allow better accuracy than the BEM because they allow a better representation of the cortical structures



Bertrand et al., 1991, Awada et al., 1997

Head models

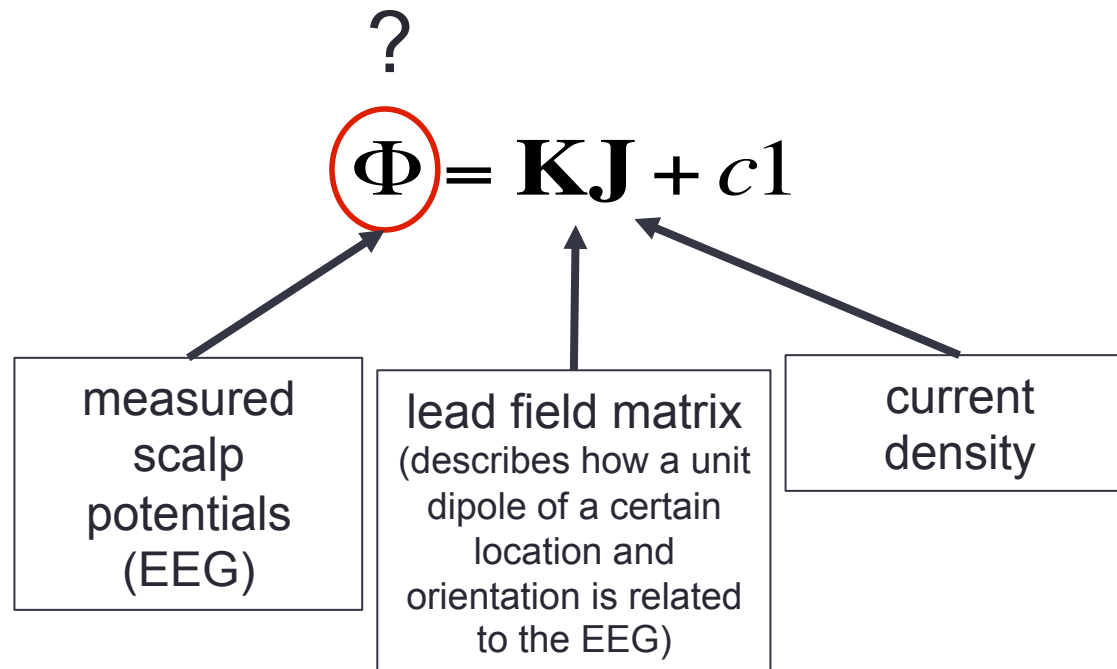


Realistic shape – (BEM isotropic, FEM anisotropic)

Plummer et al., Epilepsia, 2008

Forward Problem

EEG forward problem describes the distribution of electric potentials for given source locations, orientations, and signals. The relationship between EEG signals (Φ) and cortical current source dipoles (J) can be represented by a linear system:

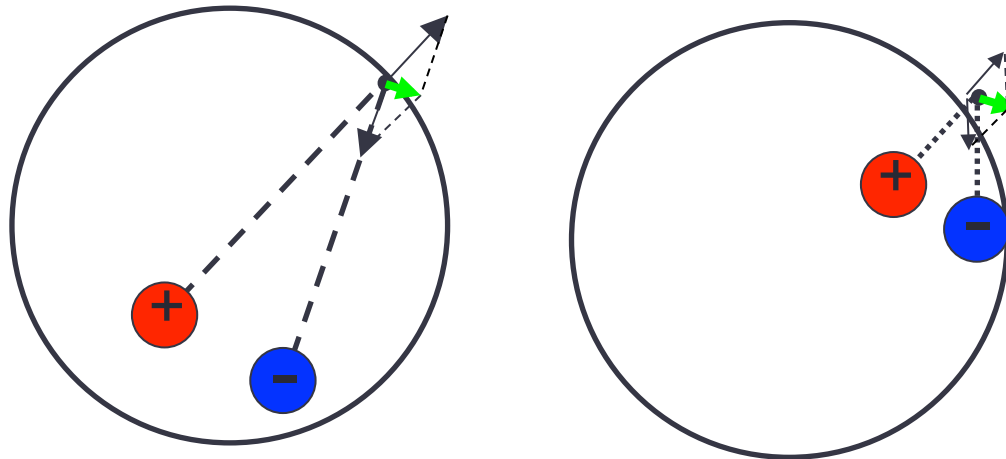


Inverse Problem

The inverse problem is used to convert measured electric potentials (EEG) into current densities of the sources.

The inverse problem is **ill-posed** because an infinity of different source configurations can produce the same EEG scalp distribution

Nurez and Srinivasan, 2006

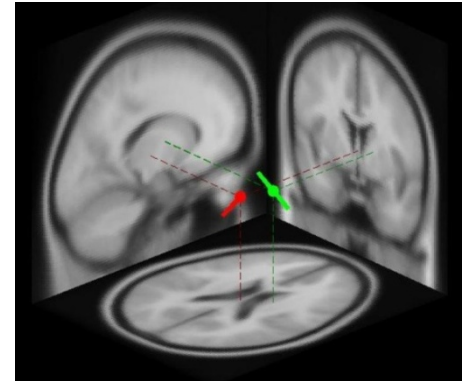


Inverse solutions

1. DISCRETE

Equivalent current dipole (ECD) approach

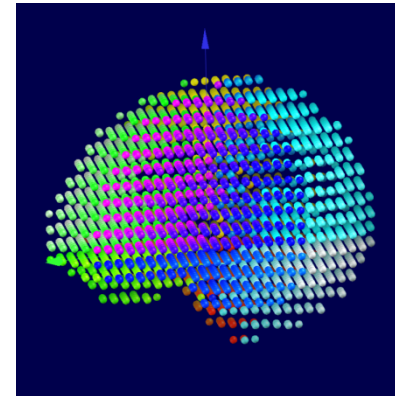
where the signals are assumed to be generated by few focal sources.



2. DISTRIBUTED

Linear distributed (LD) approaches

which consider that the dipoles are regularly distributed in cerebral volume according to a 3D grid and where all possible source locations are considered simultaneously.



Inverse Problem → Inverse solutions

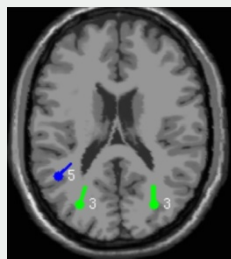
Equivalent current dipole approach

ECD assumes the underlying neuronal sources to be focal

Number of sources < number of sensors
OVERDETERMINED PROBLEM

The lead field matrix has more rows (number of sensors) than columns (number of sources)

Source model and source waveforms



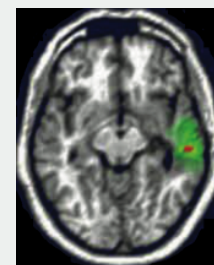
Linear distributed

The 3D grid of solution points is considered as a possible location of a brain activity source

Number of sources >> number of sensors
UNDERDETERMINED PROBLEM

The lead field matrix has more columns than rows

3D volume image for each time point



Equivalent current dipole

Parameter Estimates

To determine the best location of the sources, the squared error between the surface electric potential map generated by dipoles using a certain forward model and the actual measured potential map is calculated.

Methods

- Dipole fitting methods [Scherg, 1990]
- linear constrained minimum variance (LCMV) beamformers [Van Veen et al., 1997]
- the multiple signal classification (MUSIC) [Mosher and Leahy, 1998]
- ...

Limitations

ECD models have some limits in estimating in advance the number of dipoles and localizing extended sources.

The center of mass of the cortical activity is localized, but the distribution and the extension of the activity remain to be determined [He et al., 2011].

Linear distributed approaches

The estimation of the dipole source configuration \mathbf{J} is provided by the solution of the linear system:

$$\Phi = \mathbf{K} \mathbf{J} + c \mathbf{1}$$

$\Phi \in \mathbb{R}^{N_E \times 1}$ with $\Phi = (\Phi_1, \Phi_2, \dots, \Phi_{N_E})^T$: is a $N_E \times 1$ known matrix of measurements of scalp electric potential differences

N_E : number of electrodes

$\mathbf{1} \in \mathbb{R}^{N_E \times 1}$: is a vector of ones

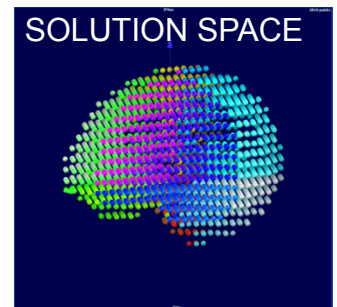
$\mathbf{J} \in \mathbb{R}^{(3N_V \times 1)}$: matrix of current densities at N_V points within the brain volume

c : accounts for the physical nature of electric potential

$\mathbf{K} \in \mathbb{R}^{N_E \times (3N_V)}$: transfer matrix or lead field matrix

$$\mathbf{K} = \begin{pmatrix} \mathbf{k}_{1,1}^T & \mathbf{k}_{1,2}^T & \cdots & \mathbf{k}_{1,N_V}^T \\ \mathbf{k}_{2,1}^T & \mathbf{k}_{2,2}^T & \cdots & \mathbf{k}_{2,N_V}^T \\ \cdots & & & \\ \mathbf{k}_{N_E,1}^T & \mathbf{k}_{N_E,2}^T & \cdots & \mathbf{k}_{N_E,N_V}^T \end{pmatrix}$$

$\mathbf{k}_{e,v} \in \mathbb{R}^{3 \times 1}$: are determined by all proprieties of the head, i.e. geometry and conductivity profile.



Particular inverse solutions

Minimum norm least square (MN) solution

$$\min_{\mathbf{J}, c} \Psi \quad \text{with} \quad \Psi = \|\Phi - \mathbf{KJ} - c\mathbf{1}\|^2 + \lambda \mathbf{J}^T \mathbf{J}$$

[Hamalainen and Ilmoniemi, 1984]

$$\text{Solution: } \hat{\mathbf{J}} = \mathbf{T}\Phi \quad \text{with} \quad \mathbf{T} = \mathbf{K}^T \mathbf{H} (\mathbf{H} \mathbf{K} \mathbf{K}^T \mathbf{H} + \lambda \mathbf{H})^+$$

$\mathbf{H} = \mathbf{I} - \frac{1}{N_E} \mathbf{1}\mathbf{1}^T$: denotes the $N_E \times N_E$ average reference operator

λ : Tikhonov regularization parameter

“+” denotes the Moore–Penrose generalized inverse

\mathbf{I} : $N_E \times N_E$ identity matrix

$\mathbf{1}$: $N \times 1$ matrix comprised of ones

N_E : number of electrodes

Minimum norm solutions favors superficial sources and misplaces deep sources

Weighted minimum-norm least squares (WMN) solution

$$\min_{\mathbf{J}, c} \Psi_D \quad \text{with} \quad \Psi_D = \|\Phi - \mathbf{KJ} - c\mathbf{1}\|^2 + \lambda \mathbf{J}^T \mathbf{D} \mathbf{J}$$

[Pascual-Marqui et al., 1994,
Gorodnitsky et al., 1995,
Grave de Peralta and Gonzalez,
1998]

$$\text{Solution: } \hat{\mathbf{J}}_D = \mathbf{T}_D \Phi \quad \text{with} \quad \mathbf{T}_D = \mathbf{D}^{-1} \mathbf{K}^T \mathbf{H} (\mathbf{H} \mathbf{K} \mathbf{D}^{-1} \mathbf{K}^T \mathbf{H} + \lambda \mathbf{H})^+$$

\mathbf{D} is used to "re-weight" the solution, i.e. to incorporate some prior knowledge about the spatial distribution of the source activity

Particular inverse solutions

Low-resolution electromagnetic tomography algorithm (LORETA)

$$\min_{\mathbf{J}, c} \Psi_W \quad \text{with} \quad \Psi_W = \|\Phi - \mathbf{KJ} - c\mathbf{1}\|^2 + \lambda \mathbf{J}^T \mathbf{WJ} \quad [\text{Pascual-Marqui et al., 1994, 1999}]$$

$$\text{Solution: } \hat{\mathbf{J}}_W = \mathbf{T}_W \Phi \quad \text{with} \quad \mathbf{T}_W = \mathbf{W}^{-1} \mathbf{K}^T \mathbf{H} (\mathbf{H} \mathbf{K} \mathbf{W}^{-1} \mathbf{K}^T \mathbf{H} + \lambda \mathbf{H})^+$$

$$\mathbf{J}^T \mathbf{WJ} = \sum_v \|\mathbf{j}_v - \text{AveNeighb}(\mathbf{j}_v)\|^2 \quad \text{AveNeighb} : \text{average of current densities in the immediate neighborhood of point } v, \text{ excluding point } v$$

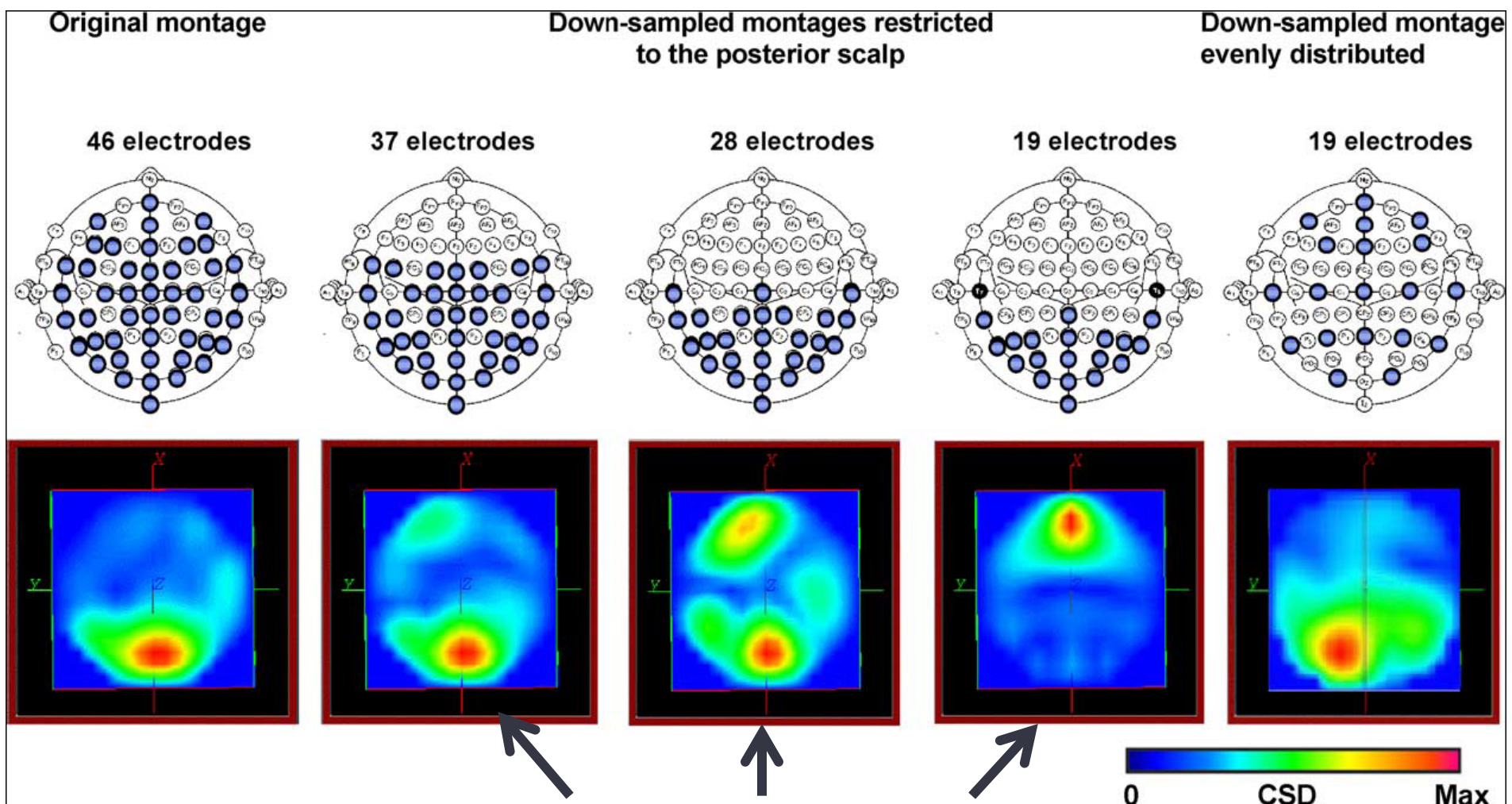
LORETA minimizes the squared norm of the Laplacian of the weighted 3D current-density vector field. It incorporates the "smoothness assumption" selecting the inverse solution of the measured data with the smoothest distribution in space.

Local Autoregressive Average (LAURA)

$$\mathbf{J}^T \mathbf{W}_{\text{Laura}} \mathbf{J} = \sum_v \|\mathbf{j}_v - \text{WeightedAveNeighb}(\mathbf{j}_v)\|^2 \quad [\text{Grave de Peralta and Gonzalez, 2002}]$$

The estimated activity at one point depends on the activity at neighboring points according to electromagnetic laws (i.e. the strength of the source declines with the inverse of the squared distance of the potential field).

Effect of the electrode distribution on the estimation of the source

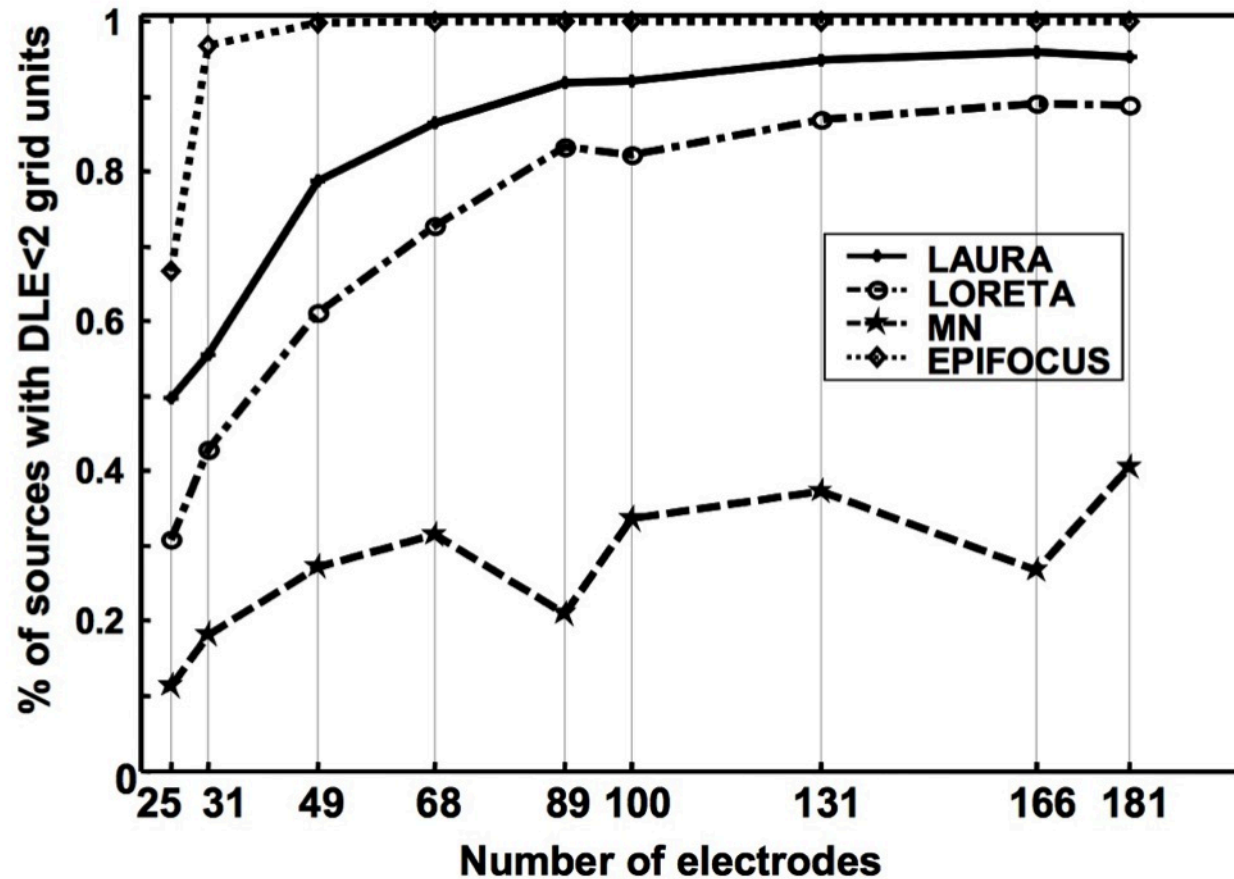


LORETA, visual EP
→ Occipital activation

Frontal electrodes excluded

Michel et al., Clinical Neurophysiol 2004

Effect of the number of electrodes on source localization



Electrical Source Imaging: clinical applications

Electrical Source Imaging: clinical applications

Identification of spontaneous EEG activity:

1. **Interictal activity** of epileptic patients
2. **Brain rhythm** in resting state (e.g. alpha rhythm)
3. **Sleep waves** (spindle)

And evoked:

4. **Evoked potential (EP)**

Electrical Source Imaging: clinical applications

Identification of spontaneous EEG activity:

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Drug resistant focal epilepsy

The feature of partial seizures is the presence of **abnormal electrical activity** that originates from an epileptic foci.

Seizures prevent healthy development and may cause brain damage.

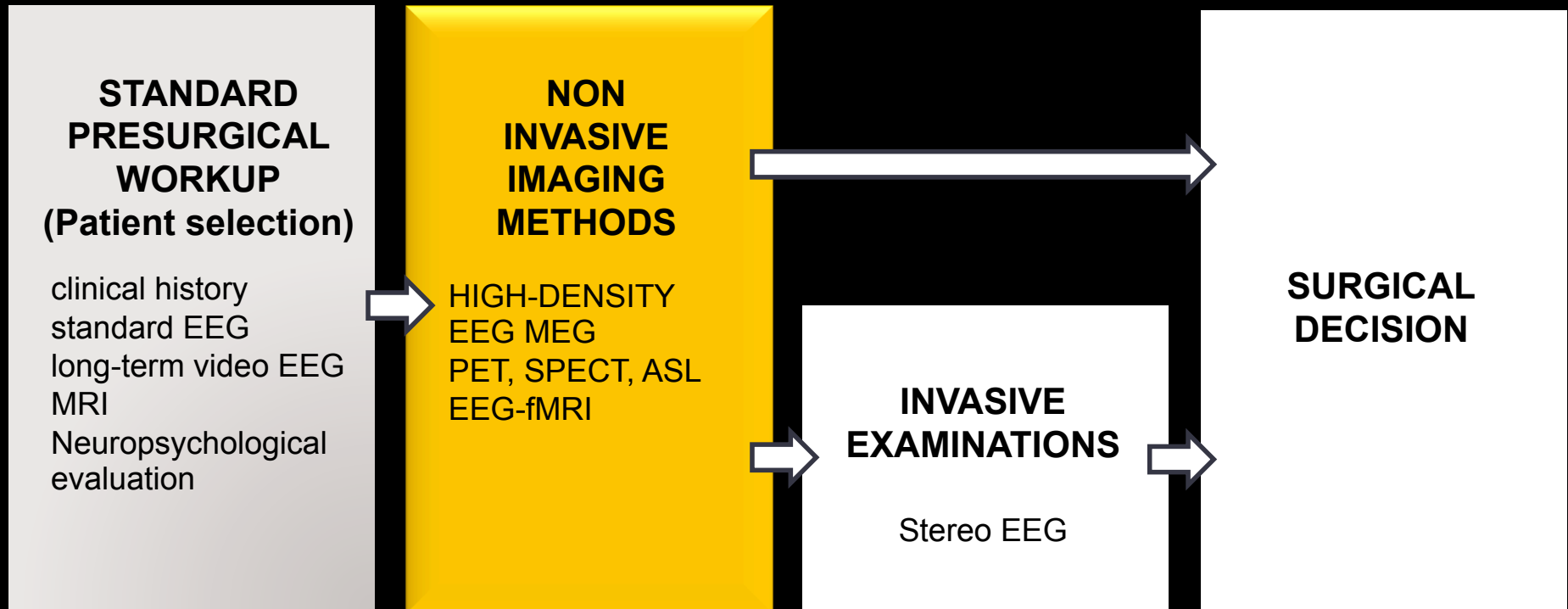
Treatment

35% of focal epilepsy patients do not respond to medication, and must undergo surgical resection of the epileptic focal points.

Surgery requires accurate localization of the foci.

Candidate for epilepsy surgery

- Persistent seizures despite appropriate pharmacological treatment
- Impairment of quality of life due to ongoing seizures

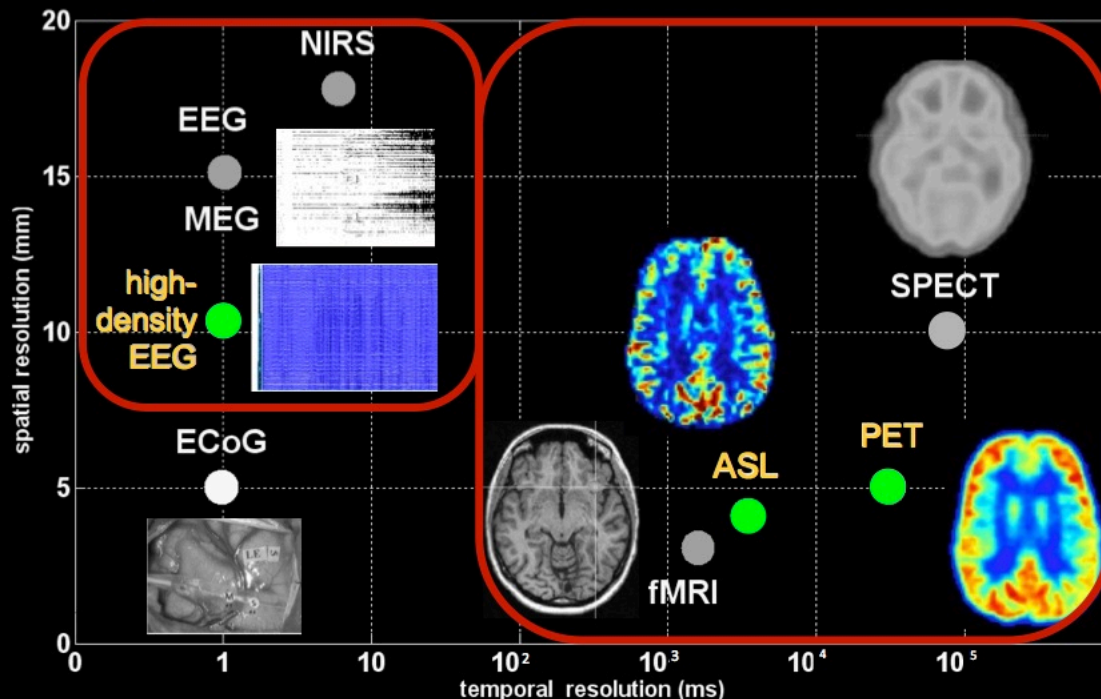


They do not always
provide the localizing
accuracy required for
surgical planning

Candidate for epilepsy surgery

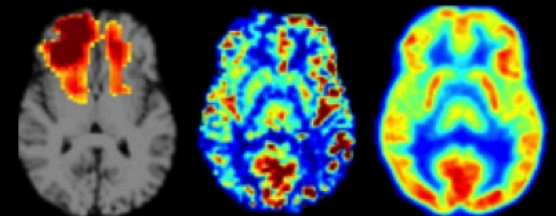
- Standard presurgical workup does not always provide the localizing accuracy and precision required for surgical planning
- Non-invasive imaging methods are useful to correctly identify the activity before the surgery treatment

NON-INVASIVE IMAGING TECHNIQUES IN EPILEPSY



MULTIMODAL APPROACH

Each bears limitations that can be partly overcome by combining their results!



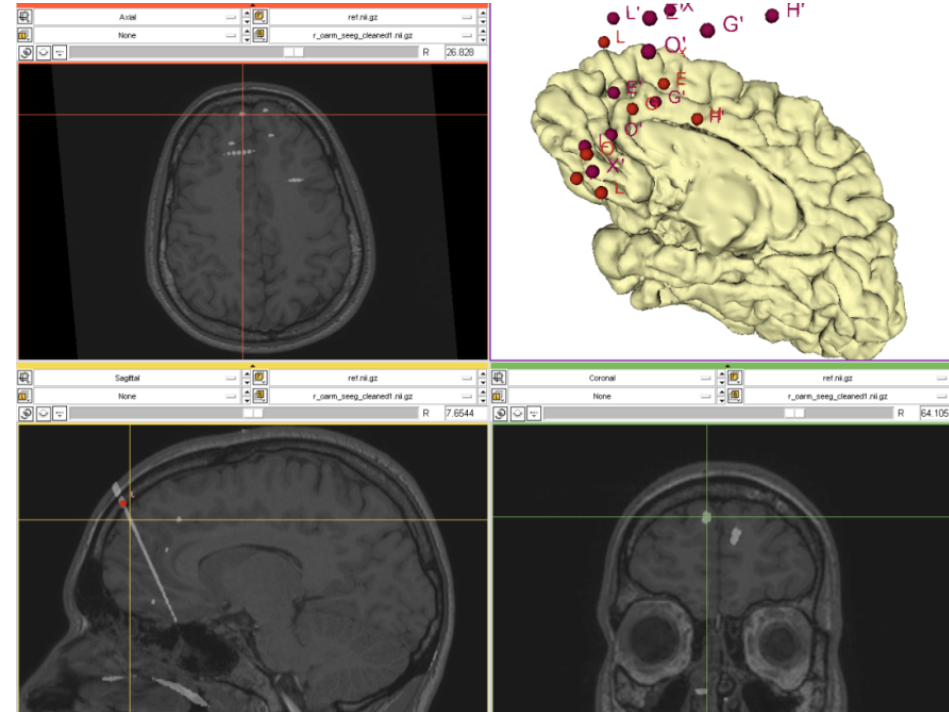
Bagshaw et al., 2006; Brodbeck et al., 2010; Groening et al., 2009; Storti et al., 2012; Vulliemmoz et al., 2010ab

Invasive examinations

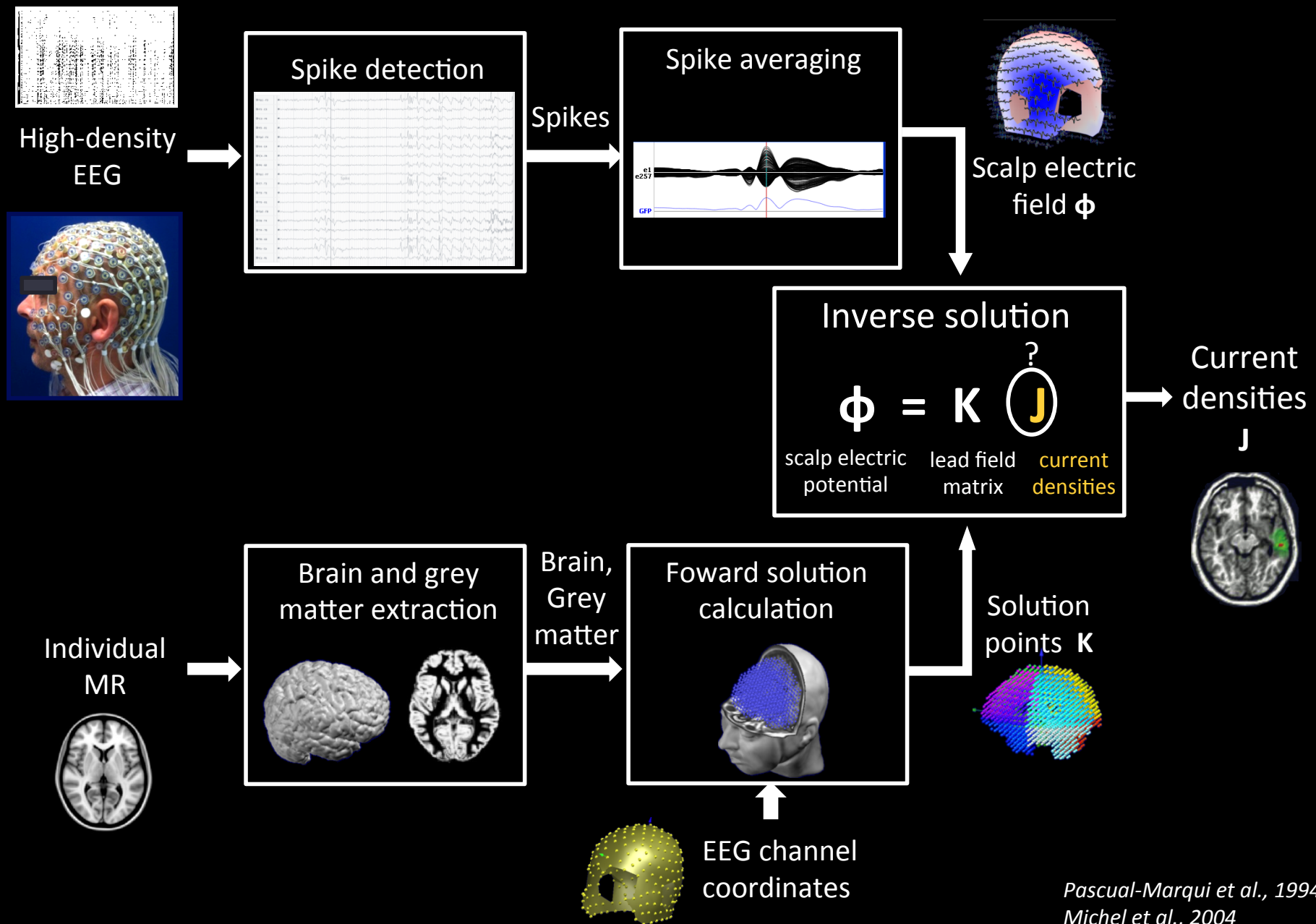
Stereo EEG

Intracerebral electrodes are implanted into the selected brain area to record the electrical activity during epileptic seizures, thus contributing to define with accuracy the boundaries of the epileptogenic zone, i.e. the area of brain generating the seizures which should be eventually surgically resected to achieve freedom from epileptic attacks.

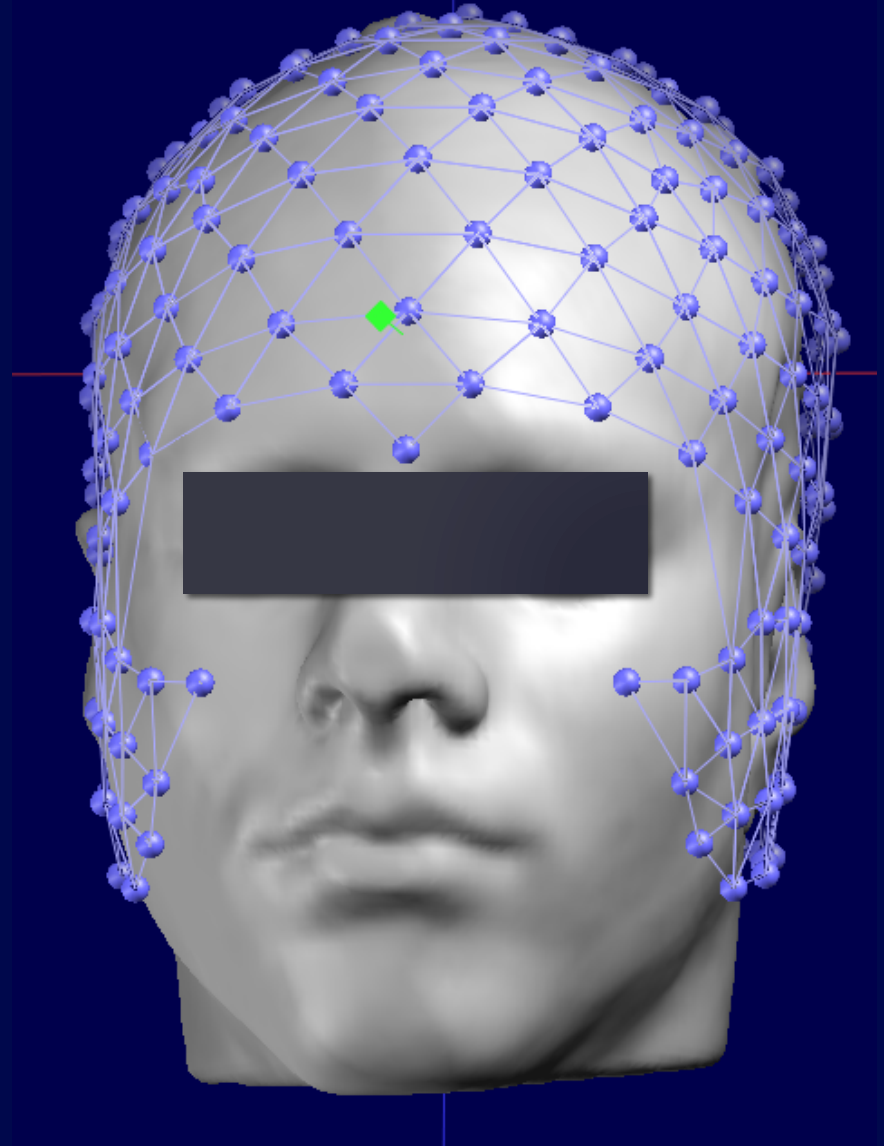
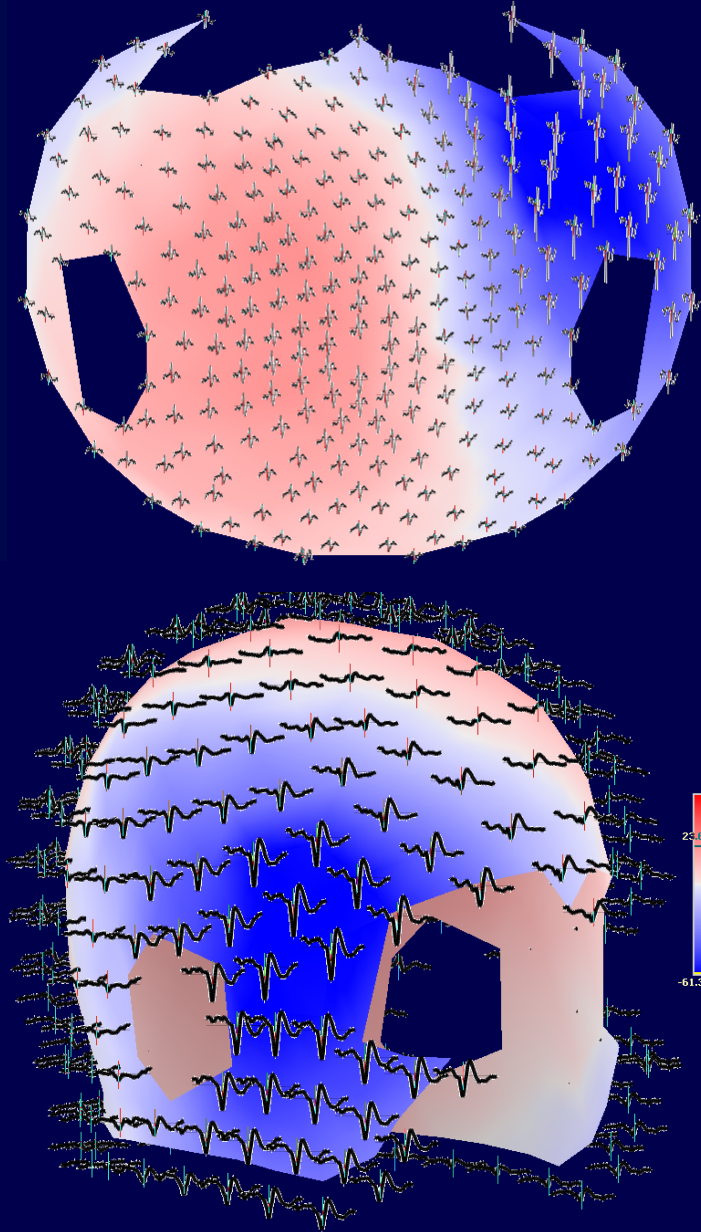
- The implantation of intracerebral electrodes is carried out on the basis of non-invasive examinations.
- It is used in patients with epilepsy not responding to drug treatment, and who are potential candidates to receive brain surgery in order to control seizures.



High-density EEG and ESI



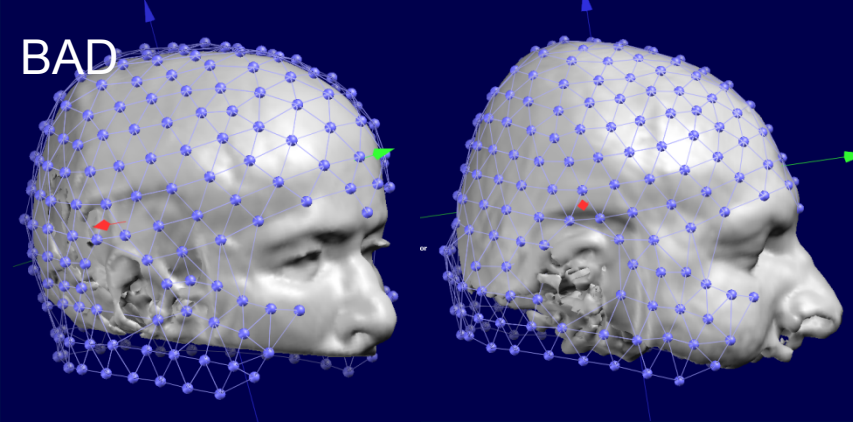
Electrodes registration



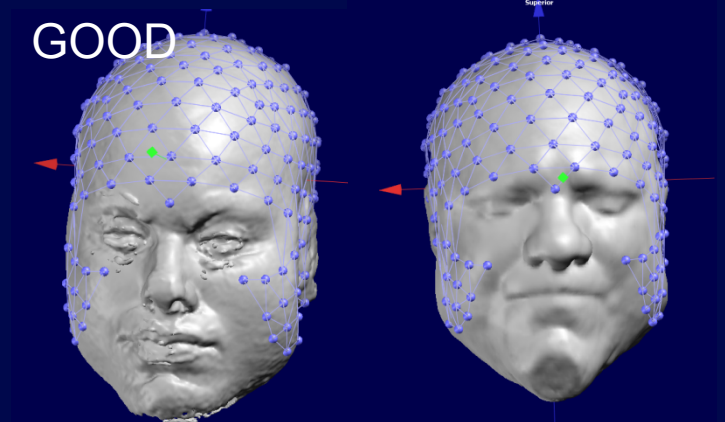
Electrodes registration : practical issues

1. Electrodes floating in the air below the MRI cut

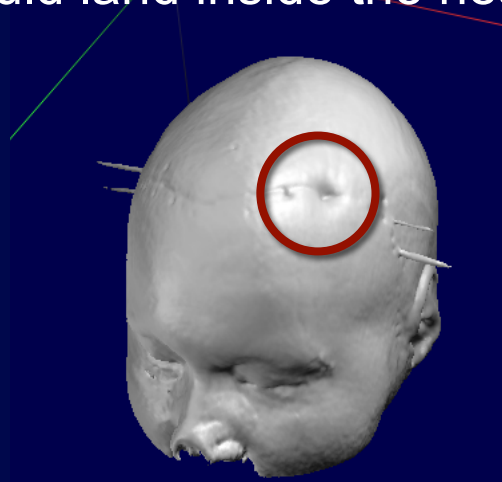
BAD



GOOD

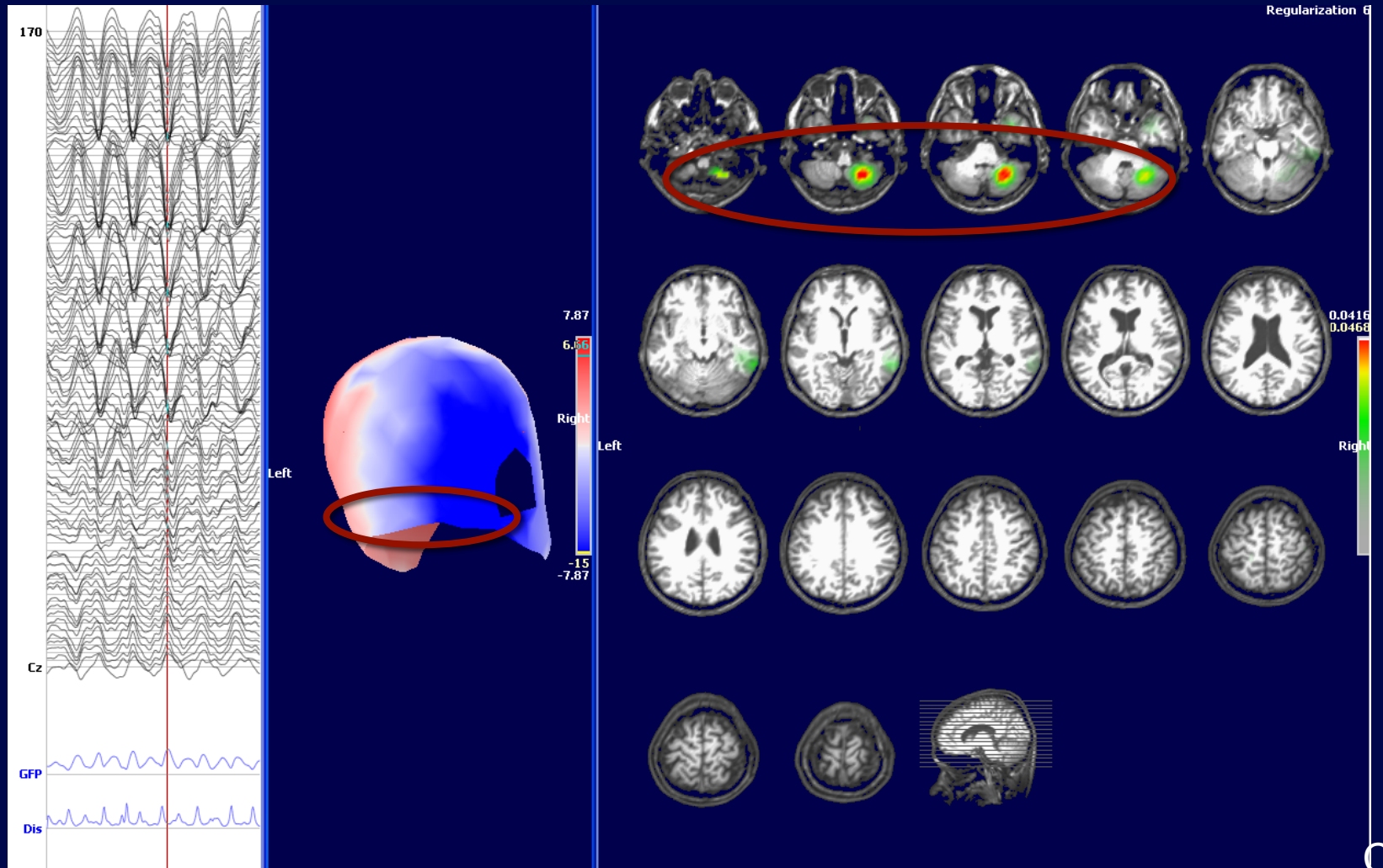


2. Registering electrodes to a corrupted MRI (irregular surface) → some electrodes could land inside the head



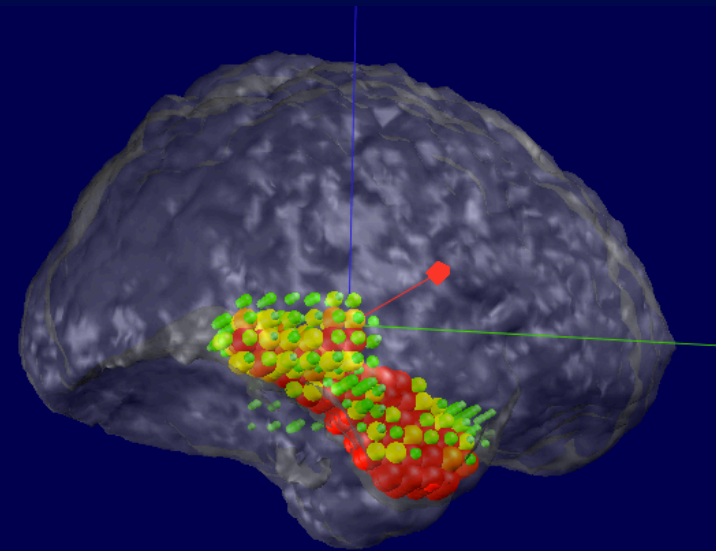
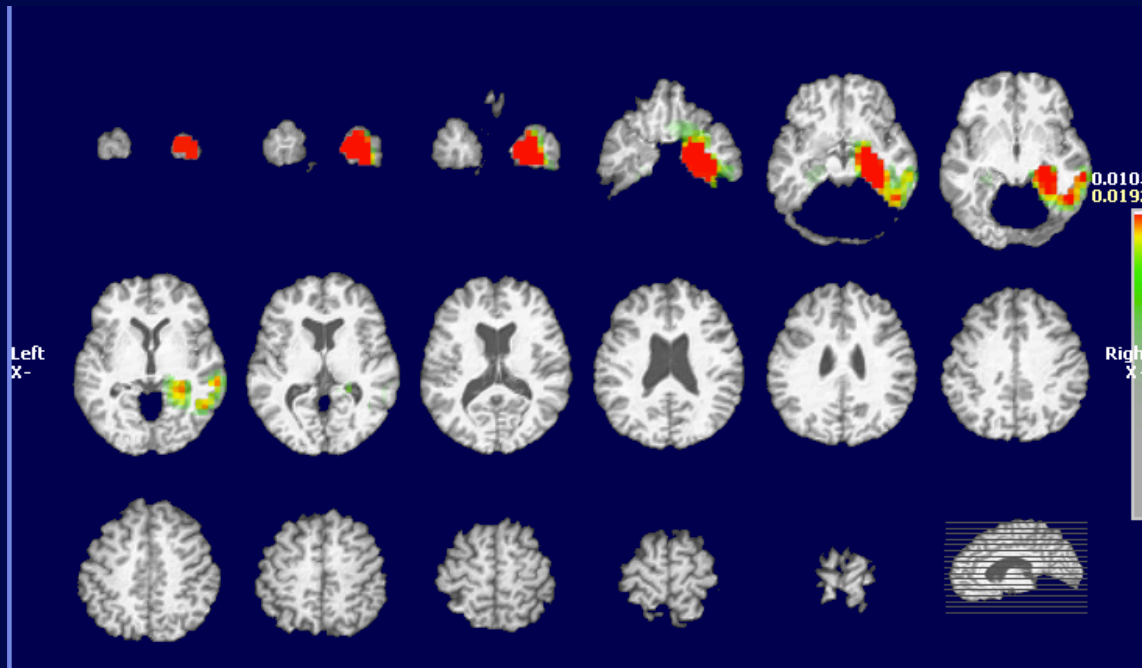
MRI (brain and grey matter extraction): issues

3. Skull-stripped brain should contain grey and white matters and void of cerebellum

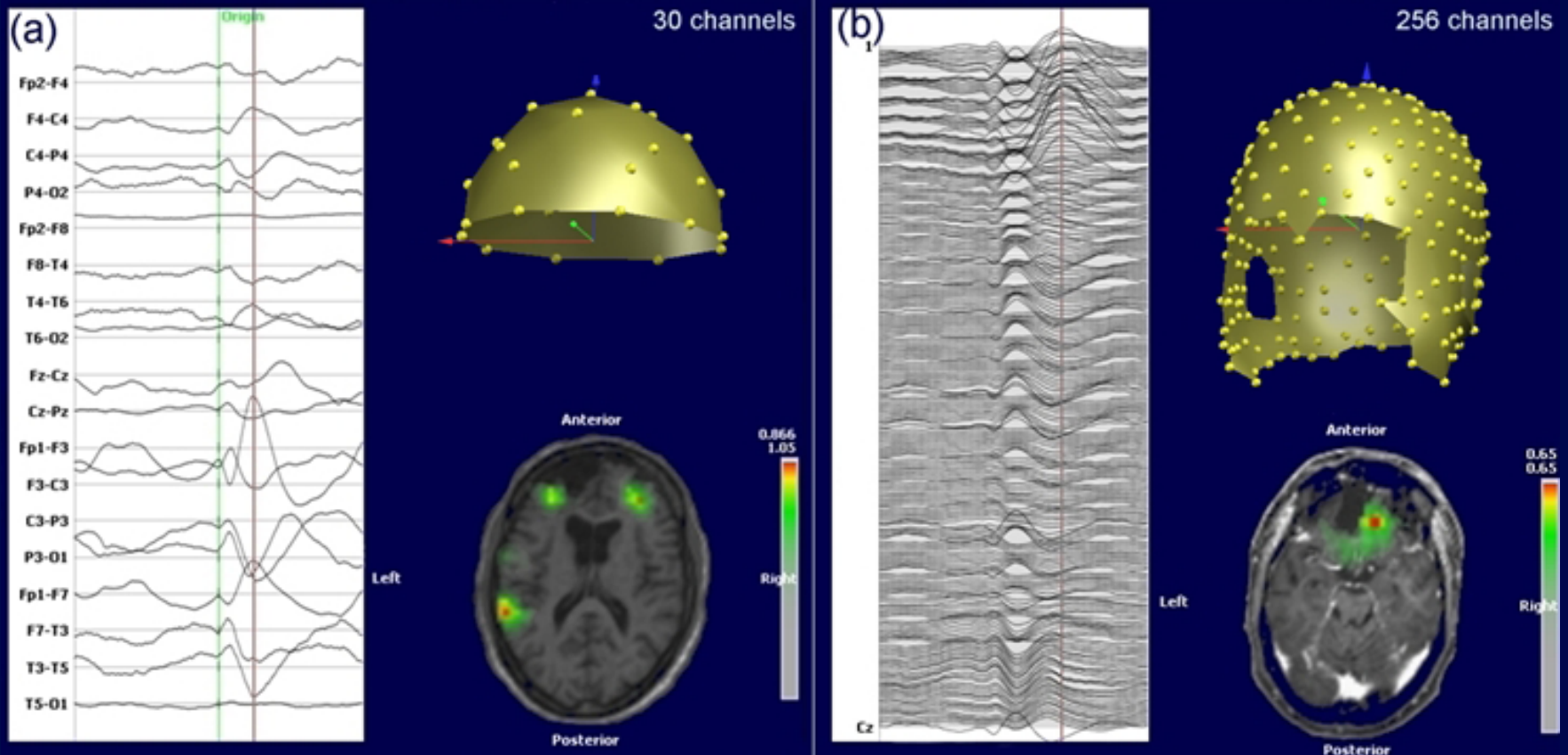


MRI (brain and grey matter extraction): issues

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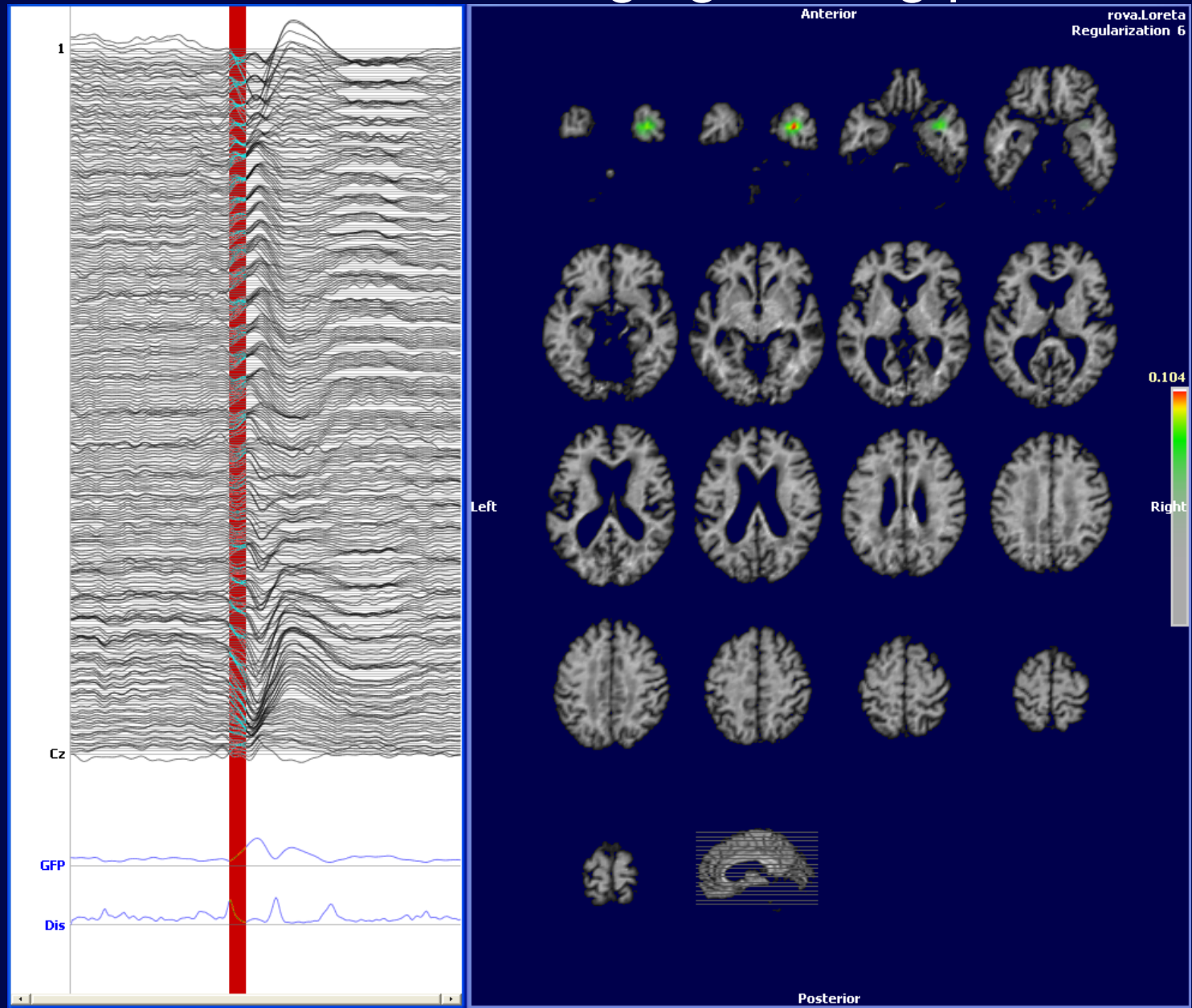


Effect of the number of electrodes on the estimation of the source

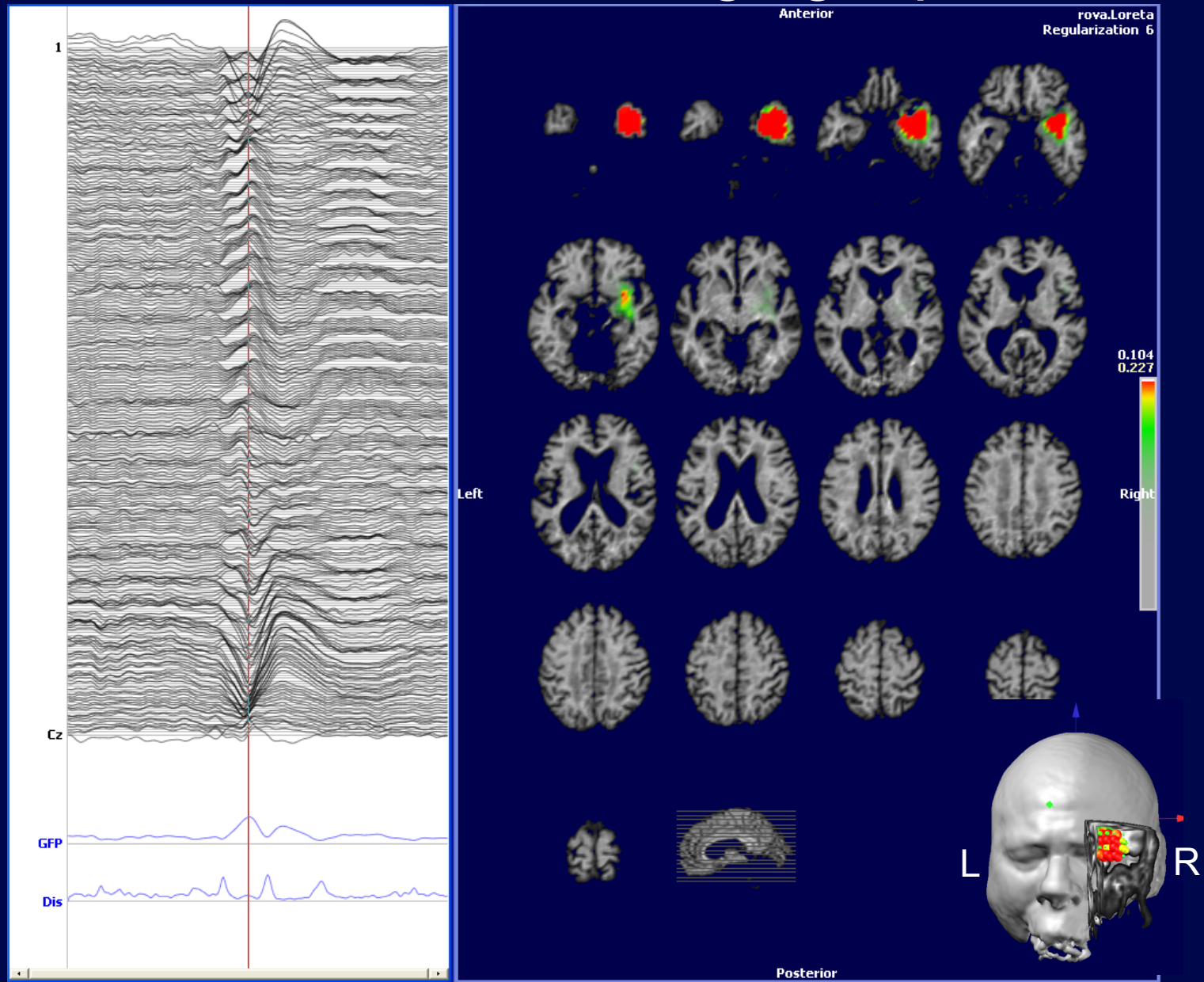


The source localization can be biased by a low number of electrodes [Michel et al., 2004] → increasing the number of electrodes the localization can be improved.

Electrical source imaging – rising phase

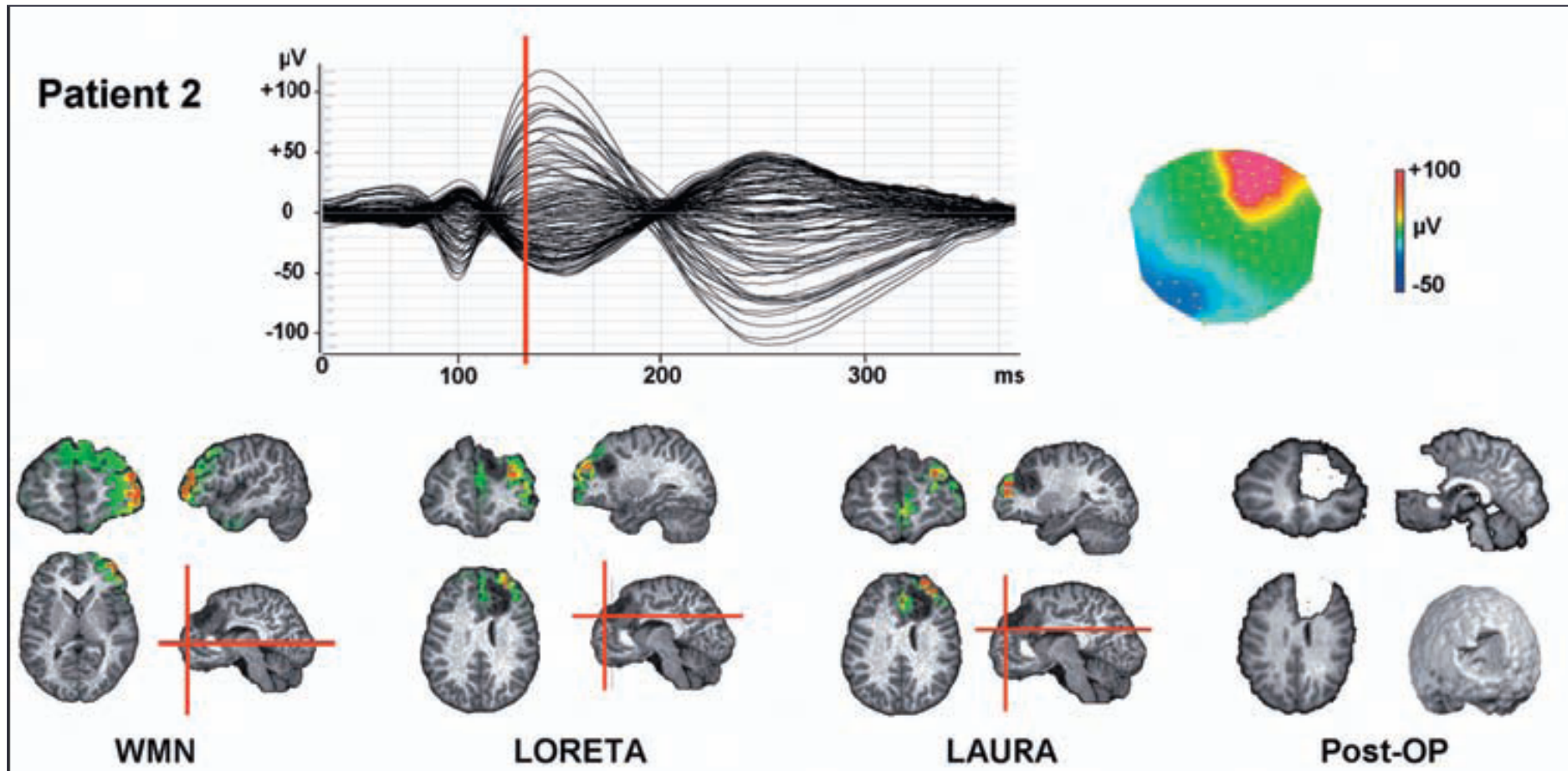


Electrical source imaging – peak



ESI and Clinical Validation

Differences between inverse solution algorithms and the post-surgical MRI



Electrical Source Imaging: clinical applications

Identification of spontaneous EEG activity:

1. Interictal activity of epileptic patients
- 2. Brain rhythm** in resting state (e.g. alpha rhythm)
3. Sleep waves (spindle)

And evoked:

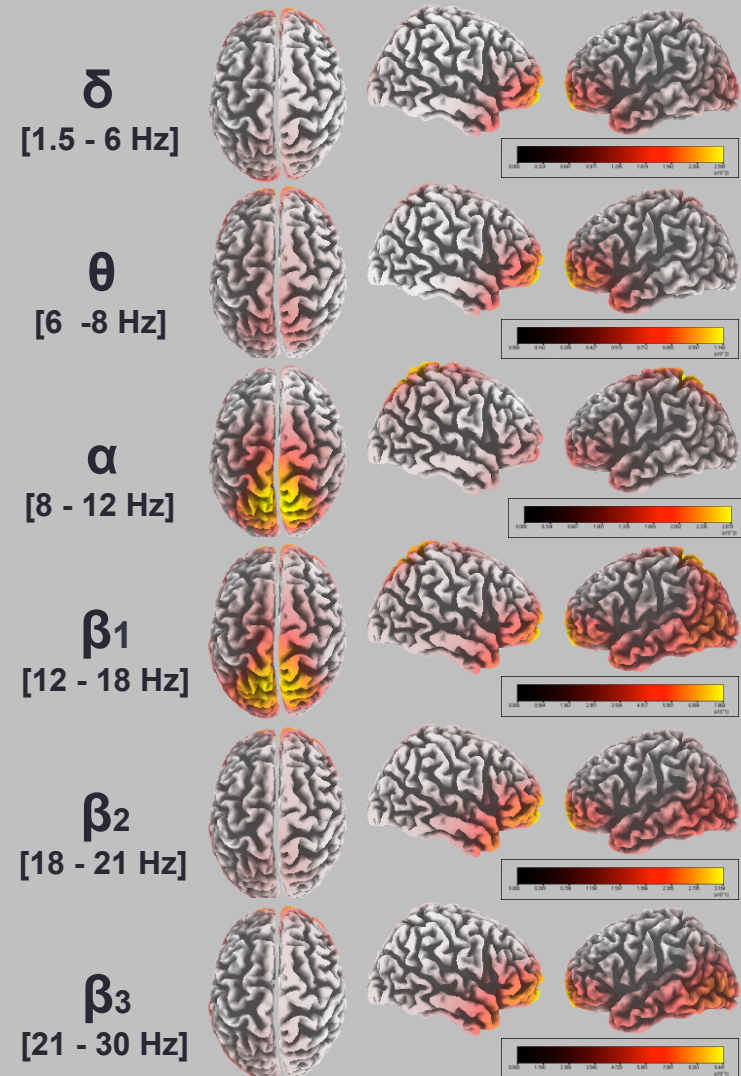
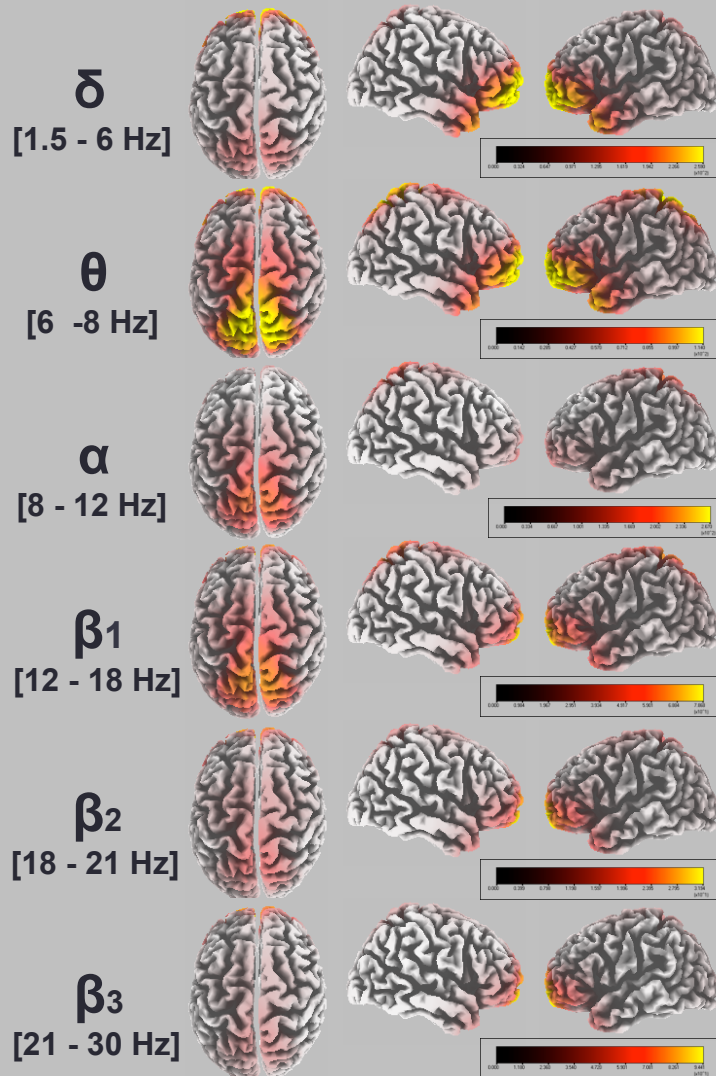
4. Evoked potential (EP)

Electrical Source Imaging of Alpha Rhythm

Scalp EEG activity shows oscillations at a variety of frequencies. Several of these oscillations have characteristic frequency ranges, spatial distributions and are associated with different states of brain functioning (e.g. waking and the various sleep stages). These oscillations represent synchronized activity over a network of neurons.

The localization of EEG rhythms in normal subjects, without any paradigm (attention, visual and auditory stimuli) are obtained from the EEG signal filtered for specific frequency bands.

Electrical Source Imaging of Brain Rhythms



Electrical Source Imaging: clinical applications

Identification of spontaneous EEG activity:

1. Interictal activity of epileptic patients
2. Brain rhythm in resting state (e.g. alpha rhythm)
- 3. Sleep waves (spindle)**

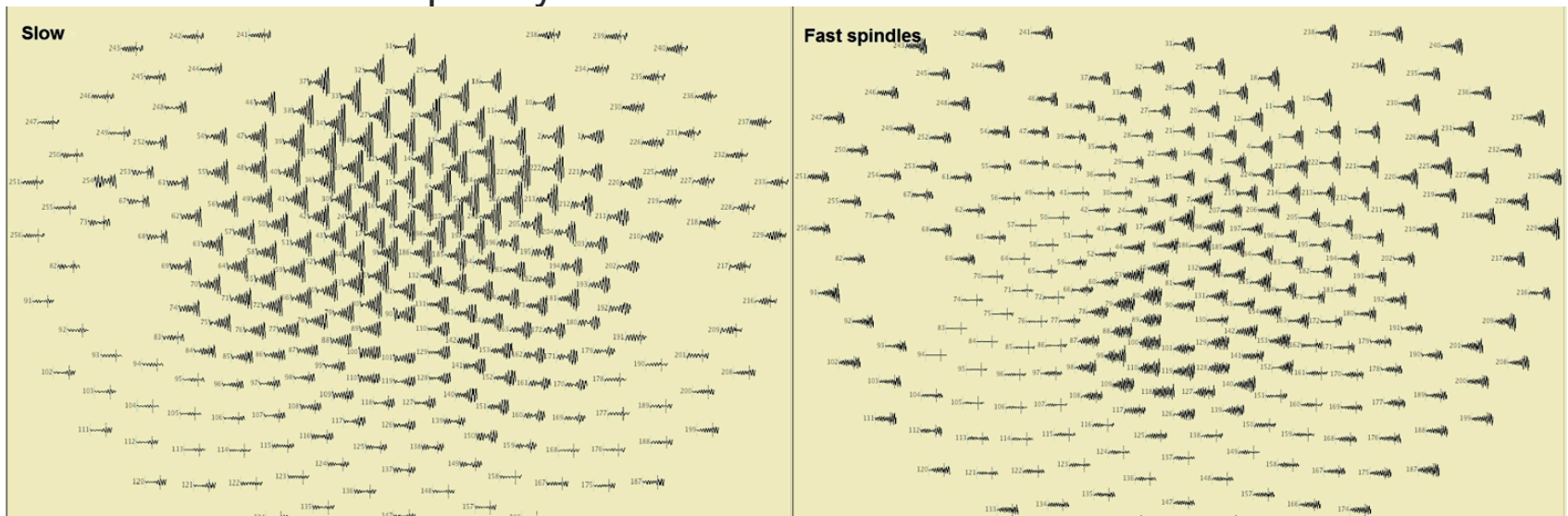
And evoked:

4. Evoked potential (EP)

Sleep

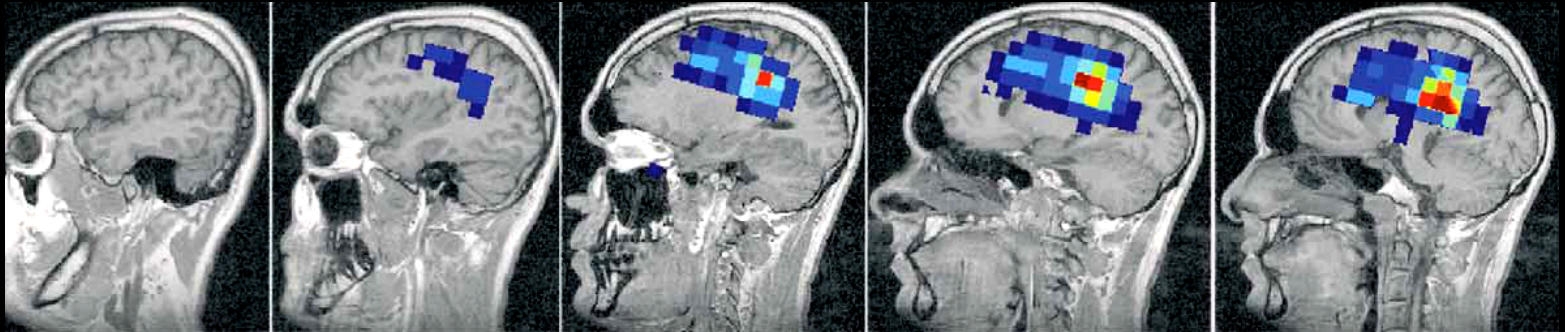
Stage	Frequency (Hz)	Amplitude (micro Volts)	Waveform type
awake	15-50	<50	
pre-sleep	8-12	50	alpha rhthym
1	4-8	50-100	theta
2	4-15	50-150	splindle waves
3	2-4	100-150	spindle waves and slow waves
4	0.5-2	100-200	slow waves and delta waves
REM	15-30	<50	

A **sleep spindle** is a burst of oscillatory brain activity visible on an EEG that occurs during stage 2 sleep. Sleep spindles are bursts of waxing and waning oscillations in the frequency of 10 to 15 Hz and last from 0.5 to 2 s.

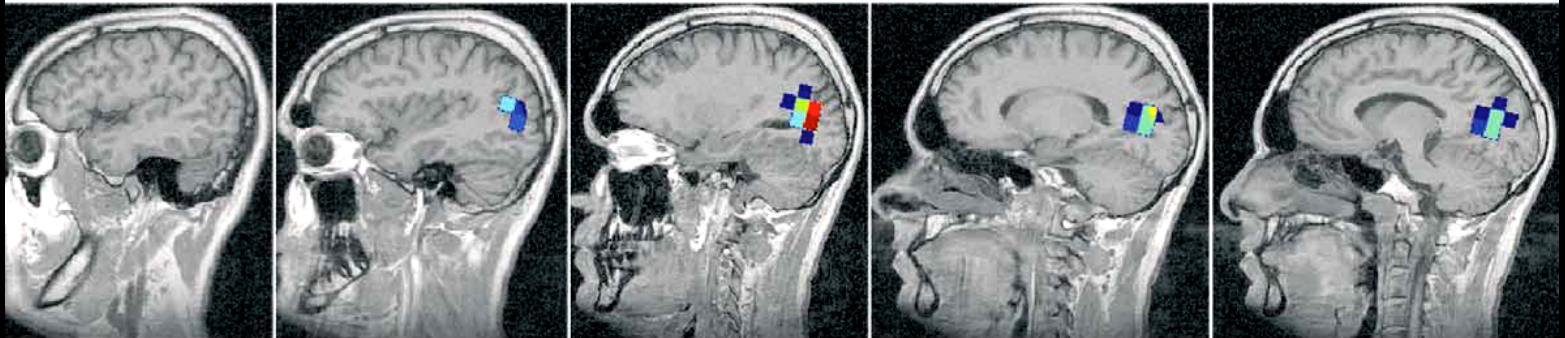


Electrical Source Imaging of Brain Rhythm

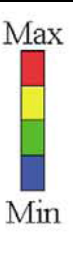
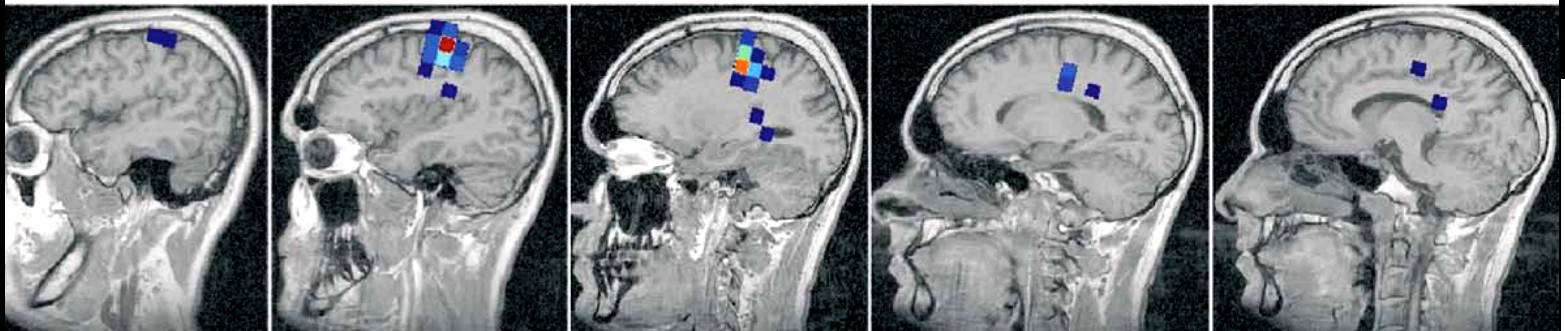
Spindle



Alpha
rhythm



Mu
rhythm



Electrical Source Imaging: clinical applications

Identification of spontaneous EEG activity:

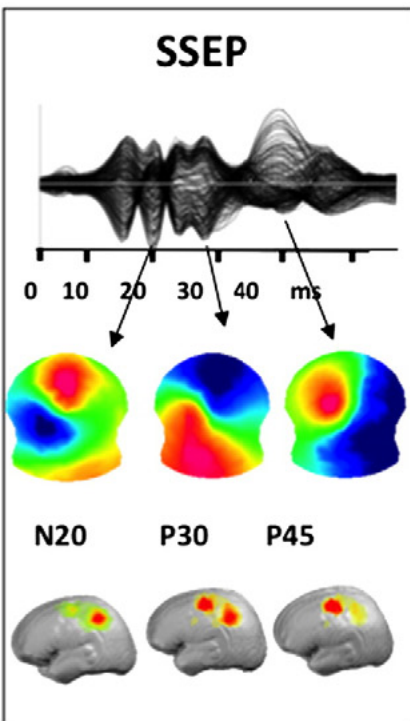
1. **Interictal activity** of epileptic patients
2. **Brain rhythm** in resting state (e.g. alpha rhythm)
3. **Sleep waves** (spindle)

And evoked:

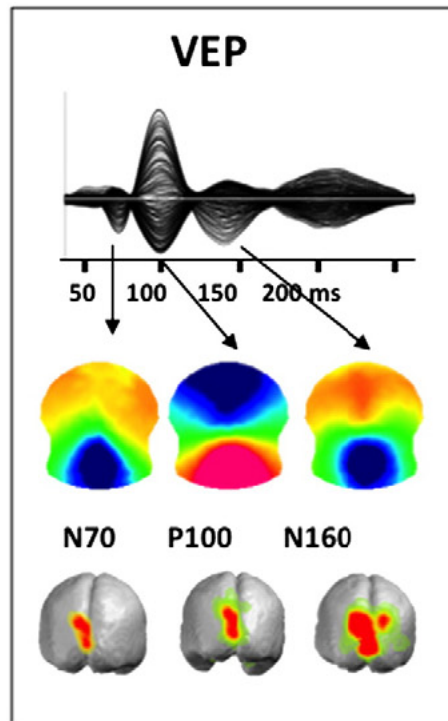
4. **Evoked potential (EP)**

Electrical Source Imaging of EP

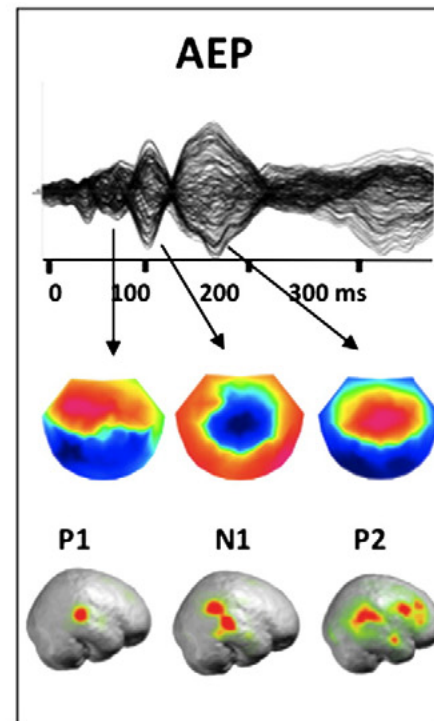
256-channel somatosensory evoked potential (SSEP) after right median nerve stimulation



256-channel visual evoked potential (VEP) after full-field checkerboard reversal.



192-channel auditory evoked potential (AEP) after short tones.



64-channel olfactory evoked potential after unilateral nostril stimulation with hydrogen sulfide.

